Introduction to Financial Forecasting in Investment 1 Analysis 2

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Introduction to Financial Forecasting in Investment Analysis



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Preface

An Introduction to Financial Forecasting in Investment Analysis

The objective of this proposed text is a 250–300 page introductory financial 41 forecasting text that exposes the reader to applications of financial forecasting 42 and the use of financial forecasts in making business decisions. The primary 43 forecasts examined in this text are earnings per shares (eps). This text will make 44 extensive use of I/B/E/S data, both historic income statement and balance sheet 45 data and analysts' forecasts of eps. We calculate financial ratios that are useful in 46 creating portfolios that have generated statistically significant excess returns in the 47 world of business. The intended audience is investment students in universities and 48 investment professionals who are not familiar with many applications of financial 49 forecasting. This text is a data-oriented text on financial forecasting, understanding 50 financial data, and creating efficient portfolios. Many regression and time series 51 examples use E-Views, OxMetrics, Scientific Computing Associates (SCA), and 52 SAS software.

The first chapter is an introduction to financial forecasting. We tell the reader 54 why one needs to forecast. We introduce the reader to the moving average and 55 exponential smoothing models to serve as forecasting benchmarks. 56

The second chapter introduces the reader to the regression analysis and forecasting. 57 In the third chapter, we use regression analysis to examine the forecasting effectivesess of the composite index of leading economic indicators, LEI. Economists have constructed leading economic indicator series to serve as a business barometer of the changing US economy since the time of Wesley C. Mitchell (1913). The purpose of this study is to examine the time series forecasts of composite economic indexes, 62 produced by The Conference Board (TCB) and test the hypothesis that the leading indicators are useful as an input to a time series model to forecast real output in the 4 USA. Economic indicators are descriptive and anticipatory time-series data are used to analyze and forecast changing business conditions. Cyclical indicators are comprehensive series that are systemically related to the business cycle.

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The third chapter introduces the reader to the forecasting process and illustrates 68 exponential smoothing and (Box-Jenkins) time series model estimations and 69 forecasts using the US Real Gross Domestic Product (GDP). The chapter is a 70 "hands-on" exercise in model estimating and forecasting. In this chapter, we 71 examine the forecasting effectiveness of the composite index of leading economic 72 indicators, LEI. The leading indicators can be an input to a transfer function model 73 of real Gross Domestic Product, GDP. The transfer function model forecasts are 74 compared to several naïve models in terms of testing which model produces the 75 most accurate forecast of real GDP. No-change forecasts of real GDP and random 76 walk with drift models may be useful as a forecasting benchmark (Mincer and 77 Zarnowitz 1969; Granger and Newbold 1977). 78

The fourth chapter addresses the issue of composite forecasting using equally 79 80 weighted and regression-weighted models. We discuss the use of GDP forecasts. We analyze a model of United States equity returns, the USER Model, to address 81 issues of outliers and multicollinearity. The USER Model combines Graham & 82 83 Dodd variables, such as earnings, book value, cash flow, and sales with analysts' revisions, breadth, and yields and price momentum to rank US equities and identify 84 85 undervalued securities. Expected returns modeling has been analyzed with a regression model in which security returns are functions of fundamental stock 86 data, such as earnings, book value, cash flow, and sales, relative to stock prices, 87 and forecast earnings per share (Fama and French 1992, 1995; Bloch et al 1993; 88 Haugen and Baker 2010; Stone and Guerard 2010). 89

In Chap. 5, we expand upon the time series models of Chap. 2 and introduce the
reader to multiple time series model and Granger causality testing as in the Ashley,
Granger, and Schmalensee (1980) and Chen and Lee (1990) tests. We illustrate
causality testing with mergers, stock prices, and LEI data in the USA in the postwar
period.

In Chap. 6, we examine analysts' forecasts in portfolio construction and management. We use the Barra risk optimization analysis system, the standard portfolio risk model in industry, to create efficient portfolios. The Barra Aegis system produces statistically significant asset selection using the USER Model for the 1980–2009 period.

In Chap. 7, we show how US, Non-US, and Global portfolio returns can be enhanced by use of eps forecasts and revisions. We use the Sungard APT and Axioma systems to create efficient portfolios using principal components-based risk models.

We illustrate global market timing and tactical asset management in Chap. 8. The ability to forecast market shifts allows the manager to increase his or her risk acceptance and enhance the risk-return tradeoff.

107 We summarize our processes, tests, and results in Chap. 9. We produce 108 conclusions that are relevant to the individual investor and portfolio manager.

The author acknowledges the support of his wife of 30-plus years, Julie, and their three children, Richard, Katherine, and Stephanie. The author gratefully acknowledges the comments and suggestions of several gentlemen who each read several chapters of this monograph. Professors Derek Bunn, of the London Business School, Martin Gruber, of New York University, Dimitrios Thomakos, of113the University of Peloponnese (Greece). Any errors remaining are the responsibility114of the author.115

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Chapter 1 Forecasting: Its Purpose and Accuracy

The purpose of this monograph is to concisely convey forecasting techniques to 3 applied investment analysis. People forecast when they make an estimate as to the 4 future value of a time series. That is, if I observe that IBM has a stock price of 5 \$205.48, as of March 23, 2012, and earned an earnings per share (eps) of \$13.06 for 6 fiscal year 2011, then I might wonder at what price IBM would trade for on 7 December 31, 2012, if it achieved the \$14.85 eps that 21 analysts, on average, 8 expect it to earn in 2012 (source: MSN, Money, March 23, 2012, 1:30 p.m., AST). 9 The low estimate is \$14.18 and the high estimate is \$15.28. Ten stock analysts 10 currently recommend IBM as a "Strong Buy," one as a "Moderate Buy," and ten 11 analysts recommend "Hold." Moreover, if IBM achieves its forecasted \$16.36 eps 12 average estimate for December 2013, when could be its stock price and should an 13 investor purchase the stock? One sees several possible outcomes; can IBM achieve 14 its forecasted eps figure? How accurate are the analysts' forecasts? Second, should 15 an investor purchase the stock on the basis of an earnings forecast? Is there a 16 relationship between eps forecasts and stock prices? How accurate is it necessary 17 for analysts to be for investors to make excess returns (stock market profits) trading 18 on the forecasts? 19

Granger (1980a, b) differentiated between an event outcome such as to forecast 20 IBM eps (at a future date), event time, such as whether the US economy will 21 completely recover from the 2008 to 2009 recession and IBM realize its forecasted 22 eps, and time series forecasts, generating the forecasts and confidence intervals of 23 IBM earnings at future dates. In this monograph, we concentrate on using eps 24 forecasts for IBM and approximately 16,000 other firms in stock selection modeling 25 and portfolio management and construction strategies to generate portfolio returns 26 that outperform the portfolio manager benchmark. To access the effectiveness of 27 producing and using forecasts, it is necessary to establish forecast benchmarks, 28 measures of forecast accuracy, and methods to test for effective forecast 29 implementation. 30

One can establish several reasonable benchmarks for forecasting. First, the use 31 of a no-change model, in which last period's value is used as the forecast for the 32 current period forecast, has a long and well-recognized history [Theil (1966) 33

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and Mincer and Zarnowitz (1969)]. Second, one can establish several criteria for

35 forecast accuracy. The forecast error, e_t , is equal to the actual value, A_t , less the

36 forecasted value, F_t . One can seek to produce and use forecasts that have the lowest

37 errors on the following measurements:

Mean Error
$$= \frac{\Sigma_{t=1}^{T} e_{T}}{T};$$

Mape = Mean Absolute Percentage Error =
$$\frac{\sum_{t=1}^{1} |e_t|}{T}$$

38 and

Mean Squared Forecast Error =
$$MSFE = \sum_{t=1}^{T} e_t^2$$
.

There are obviously advantages and disadvantages to these measures. First, in 39 the mean error, small positive and negative values may "cancel" out implying that 40 the forecasts are "perfect." Makridakis et al. (2000) remind us that the mean error is 41 only useful in determining whether the forecaster over-forecasts, producing posi-42 tive forecast errors; that is, the forecaster has a positive forecast bias. The MAPE is 43 the most commonly used forecast error efficiency criteria [Makridakis et al. 44 (1984)]. The MAPE recognizes the need of the forecast to be as close as possible 45 to the realized value. Thus, the sign of the forecast error, whether positive or 46 negative, is not the primary concern. Finally, the mean squared forecast error is 47 assuming a quadratic loss function, that is, a large positive forecast error is not 48 preferred to a large negative forecast error. In this monograph, we examine the 49 implications of the three primary measures of forecast accuracy. We are concerned 50 with two types of forecasts: the economy (the United States and the World, 51 particularly the Euro zone) and analysts forecasts of corporate eps. Why? We 52 believe, and will demonstrate, that a reasonable economic forecast of the direction 53 of the economic strength is significant in allowing an asset manager or an investor 54 to participate in economic growth. Second, we find that firms achieving the highest 55 growth in eps generate the highest stock holder returns during the 1980–2009 56 period; moreover, we will demonstrate that the securities that achieve the highest 57 eps growth and hence returns are not those forecast to have the highest eps, but are 58 not that have the highest eps forecast revisions and that it is equally important for 59 analysts to agree on the eps revisions. That is, the larger the number of analysts that 60 61 raise their respective eps forecasts, the highest will be stockholder returns.

The purpose of this monograph is to introduce the reader to a variety of financial techniques and tools to produce forecasts, test for forecasting accuracy, and demonstrate the effectiveness of financial forecasts in stock selection, portfolio construction and management, and portfolio attribution. We believe that financial markets are very near to being efficient, but statistically significant excess returns can be earned. AU1

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Let us discuss several aspects to forecast accuracy: forecast rationality, turning 68 point analysis, and absolute and relative accuracy. 69

Forecast Rationality

One of the most important aspects of forecast accuracy is forecast rationality. 71 Clements and Hendry (1998) discuss rationality in several levels. "Weak" rational-72 AU3 ity is associated with the concept of biasedness. A test of unbiasedness is generally 73 written in the form 74

 $A_t = \alpha + \beta P_t + \varepsilon_t,$

where

 A_t , actual value at time t;

 P_t , predicted value (forecast) at time t;

 ε_t , error term at time *t*.

In (1.1), we have only assumed a one-step-ahead forecast horizon. One can 79 replace t with t + k to address the issues of k = Period ahead periods. Unbiasedness 80 is defined in (1.1) with the null hypothesis that $\alpha = 0$ and $\beta = 1$. The requirement 81 for unbiasedness is that $E(\varepsilon_t) = 0$. In expectational terms 82

$$E[A_t] = \alpha + \beta E[P_t]. \tag{1.2}$$

One expects $\beta = 1$ and $\alpha = 0$, a sufficient, but not necessary condition for 83 unbiasedness. "Strong" rationality or efficiency requires that the forecast errors are 84 uncorrelated with other data or information available at the time of the forecast, 85 Clements and Hendry (1998). 86

Much of forecasting analysis, measurement, and relative accuracy was devel- 87 oped in Theil (1961) and Mincer and Zarnowitz (1969). Theil discussed several 88 aspects of the quality of forecasts. Theil (p. 29) discussed the issue of turning points, 89 or one-sided movements, correctly. Theil produced a two-by-two dichotomy of 90 turning point forecasting. The Theil turning point analysis is well worth reviewing. 91 A turning point is correctly predicted; that is, a turning point is predicted and an 92 actual turning point occurs (referred as "i"). In a second case, a turning point is 93 predicted, but does not occur ("ii"). In the third case, a turning point actually occurs, 94 but was not predicted ("iii"); the turning point is incorrectly predicted. In the fourth 95 and final case, a turning point is not predicted and not recorded. Thus, "i" and "iv" 96 are regarded as forecast successes and "ii" and "iii" are regarded as forecast 97 failures. The Theil turning point table is written as 98

Actual turning points	Predicted turning points		
	Turning point	No turning point	
Turning point	i	iii	100
No turning point	ii	iv	101

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(1.1)

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1 Forecasting: Its Purpose and Accuracy

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102 The Theil turning point failure measures:

$$\phi_1 = \frac{iii}{i+ii}; \quad \phi_2 = \frac{iii}{i+iii}.$$

Small values of ϕ_1 and ϕ_2 indicate successful turning point forecasting. The turning point errors are often expressed graphically, where



Regions A and D represent overestimates of changes whereas regions B and C represent underestimates of changes. The 45° line represents the line of perfect forecasts. Elton et al. (2009) make extensive use of the Theil graphical chart in their analysis of analysts' forecasts of eps.

A line of perfect forecasting is shown in Chart 2, where U = 0.



A line of maximum inequality is shown in Chart 3 where U = 1.



of forecasting are shown in Chart 4 and Chart 5 where the respective μ are small and 113 large, respectively. 114







115

116 Theil (1961, p. 30) analyzed the relationship between predicted and actual 117 values of individual *i*.

$$\mathbf{P}_i = \alpha + \beta A_i, \quad \beta > 0. \tag{1.3}$$

118 Perfect forecasting requires that $\alpha = 0$ and $\beta = 1$. An alternative representation 119 of (1.3) can be represented by the now familiar inequality coefficient, now known 120 as Theil's *U*, or Theil Inequality coefficient, TIC.

$$\frac{\mu = \sqrt{\frac{1}{T}\Sigma(P_i - A_i)^2}}{\sqrt{\frac{1}{T}\Sigma P_i^2} + \sqrt{\frac{1}{T}\Sigma A_i^2}}.$$
(1.4)

121 If U = 0, then $P_i = A_i$ for all *I*, and there is perfect forecasting. If U = 1, then 122 the TIC reaches its "maximum in equality" and this represents very bad forecasting. 123 Theil broke down the numerator of μ into sources or proportions of inequality.

$$\frac{1}{T}\Sigma(P_i - A_i)^2 = (\bar{P} - \bar{A})^2 + (S_P - S_A)^2 + 2(1 - r)S_PS_A,$$
(1.5)

124 where

125 \bar{P} = mean of predicted values;

Forecast Rationality

\bar{A} = mean of actual values;	126
$S_{\rm P}$ = standard deviation of predicted values;	127
$S_{\rm A}$ = standard deviation of actual values;	128
and	129
r = correlation coefficient of predicted and actual values.	130
Let D represent the denominator of (1.4) .	131

$$U_{M} = \frac{\bar{P} - \bar{A}}{D};$$

$$U_{S} = \frac{S_{P} - S_{A}}{D};$$

$$U_{C} = \frac{\sqrt{2(1 - r)S_{P}S_{A}}}{D};$$

$$U_{M}^{2} + U_{S}^{2} + U_{C}^{2} = U^{2}.$$
(1.6)

The term $U_{\rm M}$ is a measure of forecast bias. The term $U_{\rm S}$ represents the variance 132 proportion and $U_{\rm C}$ represents the covariance proportion. $U_{\rm M}$ is bounded within plus 133 and minus 1; that is, $U_{\rm M} = 1$ indicates no variation of *P* and *A* or perfect correlation 134 with slope of 1. 135

$$U^{M} = \frac{U^{2}M}{U^{2}}; \quad U^{S} = \frac{U_{S}^{2}}{U^{2}} = U^{C} = \frac{U_{C}^{2}}{U^{2}}.$$

Theil refers to U^{M} , U^{S} , and U^{C} as partial coefficients of inequality due to unequal 136 central tendency, unequal variation, and imperfect correlation, respectively. 137

$$U^M + U^S + U^C = 1. (1.7)$$

Theil (1961, p. 39) decomposes (1.5) into

$$\frac{1}{T}\Sigma(P_i - A_i)^2 = (\bar{P} - \bar{A})^2 + (S_P - S_A)^2 + (1 - r^2)S_A^2.$$
(1.8)

If a forecast is unbiased, then $E(\bar{P}) = E(\bar{A})$ and, in the regression of 139

$$A_i = P_i + U_i,$$

where U_i = regression error term, the slope of A on P is $\frac{rS_A}{S_P}$. $U^2 = U_M^2 + U_R^2 + U_D^2$, 140

141 where $U_R^2 = \left(\frac{S_P - rS_A}{D}\right)^2$;

$$U_D^2 = \left(\frac{\sqrt{(1-r^2)}S_A}{D}\right)^2.$$

 $U_{\rm R}$ is inequality due to an incorrect regression slope and $U_{\rm D}$ is inequality due to 142 143 nonzero regression error terms (disturbances).

$$U^R = \frac{U_R^2}{U^2}$$
 and $U^D = \frac{U_D^2}{U^2}$.

The U^{R} term is the regression proportion of inequality. The U^{D} term is the 144 145 disturbance proportion of inequality.

$$U^M + U^R + U^D = 1$$

The modern version of the TIC is written as the Theil U as 146

$$U = \sqrt{\frac{\sum_{t=1}^{T-1} \left(\frac{F_{t+1} - Y_t - Y_{t+1} + Y_t}{Y_t}\right)^2}{\sum_{t=1}^{T-1} \left(\frac{Y_{t+1} - Y_t}{Y_t}\right)^2}}$$
(1.9)
147 or

$$U = \sqrt{\frac{\sum_{t=1}^{T-1} \left(FPE_{t+1} - APE_{t+1}\right)^2}{\sum_{t=1}^{T-1} \left(APE_{t+1}\right)^2}},$$
148 where
149
150

$$FPE_{t+1} = \frac{F_{t+1} - Y_t}{Y_t} \text{ and}$$

$$APE_{t+1} = \frac{Y_{t+1} - Y_t}{Y_t},$$

4

147 or

149

150

where F = forecast and A = Actual values, 151

where FPE is the forecast relative change and APE is the actual relative change. 152

153 Absolute and Relative Forecast Accuracy

Mincer and Zarnowitz (1969) built upon the TIC analysis and discussed absolute 154 155 and relative forecasting accuracy in a more intuitive manner.



The line of perfect, LPF, is of course where P = A, as was the case with Theil. 157 Mincer and Zarnowitz (1969) write the mean square error of forecast, $M_{\rm P}$, as 158

$$M_P = E(A - P)^2,$$
 (1.10)

where *E* denotes expected value. In the Mincer–Zarnowitz Prediction–Realization 159 diagram, shown in Chart 6, the line $E - E^{C}$ denotes forecast bias. Thus, E(A) - 160 E(P) = E(U) denotes forecast bias. 161

Let us return for the actual-predicted value regression analysis:

$$A_t = P_t + u_t \tag{1.11}$$

which is estimated with an ordinary least squares regression of

$$A_t = \alpha + \beta P_t + v_t. \tag{1.12}$$

It is necessary for the forecast error, u_t , to be uncorrelated with forecast values, P_t , 164 for the regression slope β to equal unity (1.0). The residual variance in the regression 165 $\sigma^2(v)$ equals the variance of the forecast error $\sigma^2(u)$. Forecasts are efficient if $\sigma^2(u)$ 166 $= \sigma^2(v)$. If the forecast is unbiased, $\alpha = 0$, and $\sigma^2(v) = \sigma^2(u) = M_{\rm P}$. 167

Mincer and Zarnowitz (1969) discuss economic forecasts in terms of predictions 168 of changes (not absolute levels). The mean square error is 169

$$(A_t - A_{t-1}) - (P_t - A_{t-1}) = A_t - P_t = u_t.$$
(1.13)

162

170 The relevant Mincer–Zarnowitz regression slope is

$$\beta_{\Delta} = \frac{cov(A_t - A_{t-1}, P_t - A_{t-1})}{\sigma^2(P_t - A_{t-1})}$$

171 If the level forecast is efficient, then $\beta = 1$ (*cov* (u_t , P_t) = 0). The $\beta_{\Delta} = 1$ and 172 only if *cov* ($u_tA_{t-1} = 0$. The extrapolative value of A_{t-1} must be incorporated 173 into the forecasts. Underestimation of change occurs when the predicted change 174 ($P_t - A_{t-1}$) is of the same size, but smaller size than the actual change ($A_t - A_{t-1}$).

$$E|P_t - A_{t-1}| < E|A_t - A_{t-1}| \tag{1.14}$$

175 or

$$E(P_t - A_{t-1})^2 < E(A_t - A_{t-1})^2.$$

$$[E(P_t) - E(A_{t-1})]^2 + \sigma^2 (P_t - A_{t-1}) < [E(A_t) - E(A_{t-1})]^2 + \sigma^2 (A_t - A_{t-1})^2.$$
(1.15)

176 Underestimation of changes occurs if

$$E(P_t) < E(A_t), \text{ when } A_t \text{ and } P_t > A_{t-1},$$

$$E(P_t) < E(A_t), \text{ when } A_t \text{ and } P_t < A_{t-1},$$

177 and or

$$\sigma^2(P_t - A_{t-1}) < \sigma^2(A_t - A_{t-1}).$$
(1.16)

178 In (1.16), when predictions of changes are efficient, $\beta_{\Delta} = 1$, then 179 $\sigma^2(A_t - A_{t-1}) = \sigma^2(P_t - A_{t-1}) + \sigma^2(U_t)$.

Mincer and Zarnowitz (1969) decomposed the mean square error to create an index of forecasting quality, $R_{\rm M}$. The index of forecasting quality is the ratio of the mean square error of forecast and the mean square error of extrapolation, the relative mean square error. If forecasts are "good" and are superior to extrapolated values, then $0 < R_{\rm M} < 1$. If $R_{\rm M} > 1$, then the forecast is inferior.

$$R_{M} = \frac{M_{P}}{M_{X}} = \frac{1 - \frac{U_{X}}{M_{X}}}{1 - \frac{U_{P}}{M_{P}}} \times \frac{M_{P}^{C}}{M_{X}^{C}} = gRM^{C}.$$
 (1.17)

185 If x is a best, unbiased, and efficient extrapolation then $M_X^C = M_X$ and $g = \frac{M_P}{M^C P}$ 186 >1 and RM^C \leq RM. Mincer and Zarnowtiz found that autoregressive 187 extrapolations were not optimal; however, RM^C < RM in twelve of 18 cases. 188 Mincer and Zarnowitz found that inefficiency was primarily due to bias.

Mincer and Zarnowitz put for the r a theory that if RM_C , the forecast is superior relative to an extrapolative forecast benchmark, then "useful autonomous information enhanced the forecast." Autoregressive extrapolations showed substantial improvement over naïve (average) models, and while not optimal, were thus more 192 efficient. A small number of lags produced satisfactory extrapolative benchmarks. 193

The Mincer–Zarnowitz approach was important, not only because of its nochange benchmarks but (benchmark method of forecast) also because of its use of 195 an extrapolative forecast which should incorporate the history of the series. Mincer and Zarnowitz concluded that the underestimation of changes reflects the conservative prediction of growth rates in series with upward trends. 198

Granger and Newbold (1986) addressed two aspects of Mincer and Zarnowitz. 199 AUG First in the Mincer and Zarnowitz forecast efficiency regression: 200

$$X_t = \alpha + \beta f_t + e_t. \tag{1.18}$$

A forecast is efficient if $\alpha = 0$ and $\beta = 1$. However, the forecast, f_t , must be 201 uncorrelated with the error term, e_t . Granger and Newbold question this assumption 202 in practical applications. Second, it is essential the e_i , the error term be white noise- 203 AUT suboptimal forecasts (whether one-step-ahead or k-step-ahead) are not white noise. 204 For a forecast to be optimal, the expected squared error must have zero mean and be 205 uncorrelated with the predictor-series. Unless the error term series takes on the 206 value "zero" with probability of one, the predictor series will have a smaller 207 variance than the real series. Second, random walk series appear to give reasonable 208 predictors of another independent random walk series. A random walk with drift 209 forecast is the approximate form as a first-order exponential smoothing model 210 shown in the appendix. We show the first-order and second-order exponential 211 smoothing model, the linear, trend, and seasonal models, the Holt (1957) and 212 AU8 Winters (1960), because Makridakis and Hibon (2000) report that simple, seasonal 213 AU9 exponential smoothing models with seasonality continue to outperform more 214 advanced time series models for large economic time series. Moreover, Makridakis 215 and Hibon (2000) report that equally weighted composite forecasts outperform 216 individual forecasts, a conclusion consistent with Makridakis and Hibon (1979) 217 AU10 and Makridakis et al. (1984). We review the Clemen and Winkler (1986) GNP 218 AU11 forecasts in Chap. 4 that examine composite forecasting. 219

Granger and Newbold (1977, 1986) restate the forecast and realization problem. 220 The series to be analyzed and forecast has a fixed mean and variance: 221

$$E(x_t) = \mu_x$$
$$E(x - \mu_x)^2 = \sigma_x^2$$

The predictor series, f_2 , has mean, f_x , variance σ_x^2 , and a correlation ρ with x. The 222 expected squared forecast error is 223

$$E(x_t - f_t)^2 = (\mu_f - \mu_x)^2 + (\sigma_f - \rho\sigma_x)^2 + (1 - \rho^2)\sigma_x^2.$$
(1.19)

A large correlation, ρ , minimizes the expected squared error. If

$$\mu_f = \mu_x$$
 and $\sigma_f = \rho \sigma_x$

then for optimal forecasts, the variance of the predictor series is less than the variance of the actual series. The population correlation coefficient is a measure of forecast quality. Granger and Newbold (1986) stated that it is "trivially easy" to obtain a predictor series "highly correlated" with the level of any economic time series.

Granger and Newbold (1986) restated Theil's decomposition of average squared forecast errors. Defining:

$$D_N^2 = \frac{1}{T} \sum_{t=1}^T (x_t - f_t)^2 = (\bar{f} - \bar{x})^2 + (s_f - s_x)^2 + 2(1 - r)s_f s_x$$
(1.20)

232 and

Ì

$$D_N^2 = (\bar{f} - \bar{x})^2 + (s_f - rs_x)^2 + (1 - r^2)s_x^2.$$
(1.21)

If \overline{f} and \overline{x} are sample means of the predictor and predicted series, s_f and s_x are the respective sample standard deviations, and r is the sample correlation coefficient of x and f.

$$U^m = rac{(ar{f} - ar{x})^2}{D_N^2}, \quad U^s = rac{(s_f - s_x)^2}{D_N^2}$$
 $U^c = 2(1 - r)s_f s_x \Big/ D_N^2.$

236 As with Theil, $U^{M} + U^{S} + U^{C} = 1$.

237 If *x* is a first-order autoregressive process,

$$x_t = a x_{t-1} + \varepsilon_t.$$

An optimal forecast, $f_t = ax_{t-1}$, produces $U^{M} = 0$, and $U^{S} + U^{C} = 1$. A high correlation between predictor and predicted series will most likely not be achieved. The standard deviation of the forecast series is less than the actual series and U^{S} is substantially different from zero. Granger and Newbold suggest testing for randomness of forecast errors.

243 Cragg and Malkiel (1968) created a database of five forecasters of long-term earnings forecasts for 185 companies in 1962 and 1963. These five forecast firms 244 included two New York City banks (trust departments), an investment banker, a 245 mutual fund manager, and the final firm was a broker and an investment advisor. 246 The Cragg and Malkiel (1968) forecasts were 5-year average annual growth rates. 247 The earnings forecasts were highly correlated with one another; the highest paired 248 correlation was 0.889 (in 1962) and the lowest paired correlation was 0.450 (in 249 1963) with most correlations exceeding 0.7. Cragg and Malkiel examined the 250 earnings forecasts among eight "sectors" and found smaller correlation coefficients 251

among the paired correlations within sectors. The correlations of forecasts for 1963 252 were very highly correlated with 1962 forecasts, exceeding 0.88, for the forecasters. 253 Furthermore, Cragg and Malkiel found that the financial firms' forecasts of earnings 254 were lowly correlated, 0.17–0.45, with forecasts created from time series 255 regressions of earnings over time. Cragg and Malkiel (1968) used the TIC (1966) 256 to measure the efficiency of the financial forecasts and found that the correlations of 257 predicted and realized earnings growth were low, although most were statistically 258 greater than zero. The TICs were large, according to Cragg and Malkiel (1968), 259 although they were less than 1.0 (showing better than no-change forecasting). The 260 TICS were lower (better) within sectors; the forecasts in electronics and electric 261 utility firms were best and foods and oils were the worst firms to forecast earnings 262 growth. Cragg and Malkiel (1968) concluded that their forecasts were little better 263 than past growth than the financial analysts' forecasts. 265

The Cragg and Malkiel (1968) study was one of the first and most-cited studies 266 of earnings forecasts. 267

Elton and Gruber (1972) built upon the Cragg and Malkiel study and found 268 similar results. That is, a simple exponentially weighted moving average was a 269 better forecasting model of annual earnings than additive or multiplicative expo- 270 nential smoothing models with trend or regression models using time as an inde- 271 pendent variable. Indeed, a very good model was a naïve model, which assumed a 272 no-change in annual eps with the exception of the prior change that had occurred in 273 earnings. One can clearly see the random walk with drift concept of earnings in the 274 Elton and Gruber (1972). Elton and Gruber compared the naïve and time series 275 forecasts to three financial service firms, and found for their 180 firm sample that 276 two of the three firms were better forecasters than the naïve models. Elton et al. 277 (1981) build upon the Cragg and Malkiel (1968) and Elton and Gruber (1972) 278 results and create an earnings forecasting database that evolves to include over 279 16,000 companies, the Institutional Brokerage Estimation Services, Inc. (I/B/E/S). 280 Elton et al. (1981) find that earnings revisions, more than the earnings forecasts, 281 determine the securities that will outperform the market. Guerard and Stone (1992) 282 [AU12] found that the I/B/E/S consensus forecasts were not statistically different than 283 random walk with drift time series forecasts for 648 firms during the 1982–1985 284 period. Guerard and Stone ran annual eps forecast regressions for rationality and 285 rejected the null hypothesis that analysts' forecasts were rational. Analysts' 286 forecasts were optimistic, producing negative intercepts in the rationality 287 regressions. Analysts' forecasts became less biased during the year and by the 288 third quarter of the year, the bias was essentially zero. Analysts' forecasts were 289 highly correlated with the time series forecasts and latent root regression, used in 290 Chap. 4, reduced forecasting errors in composite earnings forecasting models. Lim 291 (2001), using the I/B/E/S Detailed database from 1984 to December 1996, found 292 forecast bias associated with small and more volatile stocks, experienced poor past 293 stock returns, and had prior negative earnings surprises. Moreover, Lim (2001) 294 found that relative bias was negatively associated with the size of the number of 295 analysts in the brokerage firm. That is, smaller firms with fewer analysts, often with 296

297 more stale data, produced more optimistic forecasts. Keane and Runkle (1998) found during the 1983-1991 period that analysts' forecasts were rational, once 298 discretionary special charges are removed. The Keane and Runkle (1998) study is 299 one of the very few studies finding rationality of analysts' forecasts; most find 300 analysts to be optimistic. Further work by Wheeler (1994) will find that firms where 301 analysts agree with the direction of earnings revisions, denoted breadth, will 302 outperform stocks with lesser agreement of earnings revisions. Guerard et al. 303 (1997) combined the work of Elton et al. (1981) and Wheeler (1994) to create a 304 better earnings forecasting model, CTEF, which we use in Chaps. 6 and 7. The 305 CTEF variable continues to produce statistically significant excess return in 306 backtest and in identifying real-time security mispricing. 307

308 Appendix

309 Exponential Smoothing

The most simple forecast of a time series can be estimated from an arithmetic mean of the data Davis and Nelson (1937). If one defines f as frequencies, or occurrences of the data, and x as the values of the series, then the arithmetic mean is

$$A = \frac{f_1 x_1 + f_2 x_2 + f_3 x_3 + \ldots + f_t x_t}{T}$$
(1.22)

313 where $T = f_1 + f_2 + f_3 + \ldots + f_t$.

$$A = \frac{\Sigma f_i x_i}{T}.$$

314 Alternatively,

$$\frac{\Sigma f_i(x_i - x)}{T}$$

$$A = x + \frac{\Sigma f_i(x_i - x)}{T}.$$
(1.23)

315 The first moment, mean, is

$$A = \frac{\sum f_i x_i}{T} = \frac{m_1}{m_0}$$
$$m_0 = \sum f_i = T, m_1 = \sum f_i x_i$$

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Appendix

If x = 0, then

$$\sigma^{2} = \frac{\Sigma f_{i} x_{i}^{2}}{T} - A^{2}$$

$$\sigma^{2} = \frac{m_{2}}{m_{o}} - \frac{m_{1}^{2}}{m_{o}^{2}} = (m_{0}m_{2} - m_{1}^{2})m_{0}^{2}.$$
(1.24)

Time series models often involve trend, cycle seasonal, and irregular 317 components, Brown (1963). An upward-moving or increasing series over time 318 AU14 could be modeled as 319

$$x_t = a + bt, \tag{1.25}$$

where a is the mean and b is the trend, or rate at which the series increases over 320 time, t. Brown (1963, p. 61) uses the closing price of IBM common stock as his 321 example of an increasing series. One could use a quadrant term, c. If c is positive, 322 then the series 323

$$x_t = a + bt + ct^2 \tag{1.26}$$

trend is changing toward an increasing trend, whereas a negative c denotes a 324 decreasing rate of trend, from upward to downward. 325

In an exponential smoothing model, the underlying process is locally constant, $326 x_t = a$, plus random noise, ε_t . 327

$$x_t = a\varepsilon_t. \tag{1.27}$$

The average value of $\varepsilon = 0.$ 328A moving average can be estimated over a portion of the data:329

$$M_t = \frac{x_1 + x_{t-1} + \ldots + x_{t-N} + 1}{N},$$
(1.28)

where M_t is the actual average of the most recent N observations. 330

$$M_t = M_{t-1} + \frac{x_t - x_{t-N}}{N}.$$
 (1.29)

An exponential smoothing forecast builds upon the moving average concept. 331

$$s_t(x) = \alpha x_t + (1 - \alpha) s_{t-1}(x),$$

where α = smoothing constant, which is similar to the fraction 1/T in a moving 332 average. 333

15

1 Forecasting: Its Purpose and Accuracy

$$s_t(x) = \alpha x_t + (1 - \alpha)[\alpha x_{t-1} + (1 - \alpha)s_{t-2}(x)] = \alpha \sum_{k_0}^{t-1} (1 - \alpha)^k x_{t-k} + (1 - \alpha)^t x_o,$$
(1.30)

where $s_t(x)$ is a linear combination of all past observations. The smoothing constant must be estimated. In a moving average process, the *N* most recent observations are weighted (equally) by 1/N and the average age of the data is

$$k = \frac{0+1+2+\ldots+N-1}{N} = \frac{N-1}{2}.$$

An *N*-period moving average is equivalent to an exponential smoothing model having an average age of the data. The one-period forecast for an exponential smoothing model is

$$F_{t+1} = F_t + \alpha (y_t - F_t),$$
 (1.31)

340 where α is the constant, $0 < \alpha < 1$.

Intuitively, if α is near zero, then the forecast is very close to the previous value's forecast. Alternatively,

$$F_{t+1} = \alpha y_t + (1 - \alpha) F_t$$

$$F_{t+1} = \alpha y_t + \alpha (1 - \alpha) y_{t-1} + (1 - \alpha) 2 F_{t-1}.$$
(1.32)

343 Makridakis et al. (1998) express F_{t-1} in terms of F_{t-2} and, over time,

$$F_{t-1} = \alpha y_t + \alpha (1-\alpha) y_{t-1} + \alpha (a-\alpha)^2 y_{t-2} + a(1-\alpha)^3 y_{t-3} + \alpha (1-\alpha)^4 y_{t-4} + \alpha (1-\alpha)^5 y_{t-5} + \dots + \alpha (1-\alpha)^{t-1} y_t + (1-\alpha)^t F_1.$$
(1.33)

³⁴⁴ Different values of α produce different mean squared errors. If one sought to ³⁴⁵ minimize the mean absolute percentage error, the adaptive exponential smoothing ³⁴⁶ can be rewritten as

$$F_{t+1} = \alpha y_t + (1 - \alpha) F_t \qquad (1.34)$$
$$\alpha t + 1 = \left| \frac{A_t}{M_t} \right|,$$

where

$$A_t = \beta E_t + (1 - \beta)A_{t-1}$$
$$M_t = \beta |E_t| + (1 - \beta)M_{t-1}$$
$$E_t = y_t - F_t.$$

References

 A_t is a smoothed estimate of the forecast error and a weighted average of A_{t-1} 348 and the last forecast error, E_t . 349

One of the great forecasting models is the Hold (1957) model that allowed 350 AU15 forecasting of data with trends. Holt's linear exponential smoothing forecast is 351

$$L_{t} = \alpha y_{t} + (1 - \alpha)(L_{t-1} + b_{t-1})$$

$$b_{t} = \beta(L_{t} - L_{t-1}) + (1 - \beta)b_{t-1}$$

$$F_{t+m} = L_{t} + b_{t}m.$$
(1.35)

 L_t is the level of the series at time t, and b_t is the estimate of the slope of the series 352 at time t. The Holt model forecast should be better forecasts than adaptive expo- 353 nential smoothing models, which lack trends. Makridakis et al. (1998) remind the 354 reader that the Holt model is often referred to as "double exponential smoothing." If 355 $\alpha = \beta$, then the Holt model is equal to Brown's double exponential smoothing 356 model. 357

The Hold (1957) and Winters (1960) seasonal model can be written as 358

(Level)
$$L_t = \alpha \frac{y_t}{s_{t-s}} + (1-\alpha)(L_{t-1}+b_{t-1})$$

(Trend) $b_t + \beta(L_t - L_{t-1}) + (a-\beta)b_{t-1}$
(Seasonal) $s_t = \gamma \frac{y_t}{L_t} + (a-\gamma)s_{t-s}$
(Forecast) $F_{t+m} = (L_t + b_t m)S_{t-s+m}$.

Seasonality is the number of months or quarters, L_t is the level of the series, b_t is 359 the trend of the series, and s_t is the seasonal component. 360

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Chapter 2 Regression Analysis and Forecasting Models

A forecast is merely a prediction about the future values of data. However, most 3 extrapolative model forecasts assume that the past is a proxy for the future. That is, 4 the economic data for the 2012–2020 period will be driven by the same variables as 5 was the case for the 2000–2011 period, or the 2007–2011 period. There are many 6 traditional models for forecasting: exponential smoothing, regression, time series, 7 and composite model forecasts, often involving expert forecasts. Regression analy- 8 sis is a statistical technique to analyze quantitative data to estimate model 9 parameters and make forecasts. We introduce the reader to regression analysis in 10 this chapter.

The horizontal line is called the *X*-axis and the vertical line the *Y*-axis. Regres- 12 sion analysis looks for a relationship between the *X* variable (sometimes called the 13 "independent" or "explanatory" variable) and the *Y* variable (the "dependent" 14 variable). 15



For example, X might be the aggregate level of personal disposable income in 16 the United States and Y would represent personal consumption expenditures in the 17 United States. By looking up these numbers for a number of years in the past, we 18 can plot points on the graph. More specifically, regression analysis seeks to find the 19 "line of best fit" through the points. Basically, the regression line is drawn to best 20 approximate the relationship between the two variables. Techniques for estimating 21

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the regression line (i.e., its intercept on the Y-axis and its slope) are the subject of 22 this chapter. Forecasts using the regression line assume that the relationship which 23 existed in the past between the two variables will continue to exist in the future. 24 There may be times when this assumption is inappropriate, such as the "Great 25 Recession" of 2008 when the housing market bubble burst. The forecaster must be 26 aware of this potential pitfall. Once the regression line has been estimated, the 27 forecaster must provide an estimate of the future level of the independent variable. 28 The reader clearly sees that the forecast of the independent variable is paramount to 29 an accurate forecast of the dependent variable. 30

Regression analysis can be expanded to include more than one independent variable. Regressions involving more than one independent variable are referred to as multiple regression. For example, the forecaster might believe that the number of cars sold depends not only on personal disposable income but also on the level of interest rates. Historical data on these three variables must be obtained and a plane of best fit estimated. Given an estimate of the future level of personal disposable income and interest rates, one can make a forecast of car sales.

Regression capabilities are found in a wide variety of software packages and 38 hence are available to anyone with a microcomputer. Microsoft Excel, a popular 39 spreadsheet package, SAS, SCA, RATS, and EViews can do simple or multiple 40 regressions. Many statistics packages can do not only regressions but also other 41 quantitative techniques such as those discussed in Chap. 3 (Time Series Analysis 42 and Forecasting). In simple regression analysis, one seeks to measure the statistical 43 association between two variables, X and Y. Regression analysis is generally used to 44 measure how changes in the independent variable, X, influence changes in the 45 dependent variable, Y. Regression analysis shows a statistical association or corre-46 lation among variables, rather than a causal relationship among variables. 47

48 The case of simple, linear, least squares regression may be written in the form

$$Y = \alpha + \beta X + \varepsilon, \tag{2.1}$$

where Y, the dependent variable, is a linear function of X, the independent variable. 49 The parameters α and β characterize the population regression line and ε is the 50 51 randomly distributed error term. The regression estimates of α and β will be derived from the principle of least squares. In applying least squares, the sum of the squared 52 regression errors will be minimized; our regression errors equal the actual depen-53 dent variable minus the estimated value from the regression line. If Y represents the 54 actual value and Y the estimated value, their difference is the error term, e. Least 55 squares regression minimized the sum of the squared error terms. The simple 56 regression line will yield an estimated value of Y, \hat{Y} , by the use of the sample 57 regression: 58

$$\hat{Y} = a + \beta X. \tag{2.2}$$

In the estimation (2.2), *a* is the least squares estimate of α and *b* is the estimate of β . Thus, *a* and *b* are the regression constants that must be estimated. The least

AU2

squares regression constants (or statistics) α and β are unbiased and efficient 61 (smallest variance) estimators of α and β . The error term, e_i , is the difference 62 between the actual and estimated dependent variable value for any given indepen-63 dent variable values, X_i .

$$e_i = \hat{Y}_i - Y_i. \tag{2.3}$$

The regression error term, e_i , is the least squares estimate of ε_i , the actual 65 error term.¹ 66

To minimize the error terms, the least squares technique minimizes the sum of $_{67}$ the squares error terms of the *N* observations, $_{68}$

$$\sum_{i=1}^{N} e_i^2.$$
 (2.4)

The error terms from the N observations will be minimized. Thus, least squares 69 regression minimizes: 70

$$\sum_{i=1}^{N} e_i^2 = \sum_{i=1}^{N} \left[Y_i - \hat{Y}_i \right]^2 = \sum_{i=1}^{N} \left[Y_i - (\alpha + b X_i) \right]^2.$$
(2.5)

.

To assure that a minimum is reached, the partial derivatives of the squared error 71 terms function 72

$$\sum_{i=1}^{N} = \left[Y_i - \left(\alpha + b X_i\right)\right]^2$$

will be taken with respect to a and b.

$$\frac{\partial \sum_{i=1}^{N} e_i^2}{\partial a} = 2 \sum_{i=1}^{N} (Y_i - a - bX_i)(-1)$$
$$= -2 \left(\sum_{i=1}^{N} Y_i - \sum_{i=1}^{N} a - b \sum_{i=1}^{N} X_i \right)$$

¹ The reader is referred to an excellent statistical reference, S. Makridakis, S.C. Wheelwright, and R. J. Hyndman, *Forecasting: Methods and Applications*, Third Edition (New York; Wiley, 1998), Chapter 5.

$$\frac{\partial \sum_{i=1}^{N} e_i^2}{\partial b} = 2 \sum_{i=1}^{N} (Y_i - a - bX_i)(-X_i) \\ = -2 \left(\sum_{i=1}^{N} Y_i X_i - \sum_{i=1}^{N} X_i - b \sum_{i=1}^{N} X_1^2 \right).$$

The partial derivatives will then be set equal to zero. 74

$$\frac{\partial \sum_{i=1}^{N} e_i^2}{\partial a} = -2\left(\sum_{i=1}^{N} Y_i - \sum_{i=1}^{N} a - b \sum_{i=1}^{N} X_i\right) = 0$$

$$\frac{\partial \sum_{i=1}^{N} e_i^2}{\partial b} = -2\left(\sum_{i=1}^{N} YX_i - \sum_{i=1}^{N} X_i - b \sum_{i=1}^{N} X_1^2\right) = 0.$$
(2.6)

Rewriting these equations, one obtains the normal equations: 75

$$\sum_{i=1}^{N} Y_i = \sum_{i=1}^{N} a + b \sum_{i=1}^{N} X_i$$

$$\sum_{i=1}^{N} Y_i X_i = a \sum_{i=1}^{N} X_i + b \sum_{i=1}^{N} X_1^2.$$
(2.7)

Solving the normal equations simultaneously for a and b yields the least squares 76 77 regression estimates:

$$\hat{a} = \frac{\left(\sum_{i=1}^{N} X_i^2\right) \left(\sum_{i=1}^{N} Y_i\right) - \left(\sum_{i=1}^{N} X_i Y_i\right)}{N\left(\sum_{i=1}^{N} X_i^2\right) - \left(\sum_{i=1}^{N} X_i\right)^2},$$

$$\hat{b} = \frac{\left(\sum_{i=1}^{N} X_i Y_i\right) - \left(\sum_{i=1}^{N} X_i\right) \left(\sum_{i=1}^{N} Y_i\right)}{N\left(\sum_{i=1}^{N} X_i^2\right) - \left(\sum_{i=1}^{N} X_i\right)^2}.$$
(2.8)

An estimation of the regression line's coefficients and goodness of fit also can be 78

found in terms of expressing the dependent and independent variables in terms of 79 80 deviations from their means, their sample moments. The sample moments will be denoted by M. 81
$$M_{XX} = \sum_{i=1}^{N} x_i^2 = \sum_{i=1}^{N} (x_i - \bar{x})^2$$

= $N \sum_{i=1}^{N} X_i - \left(\sum_{i=1}^{N} X_i\right)^2$
$$M_{XY} = \sum_{i=1}^{N} x_i y_i = \sum_{i=1}^{N} (X_i - \bar{X})(Y_i - \bar{Y})$$

= $N \sum_{i=1}^{N} X_i Y_i - \left(\sum_{i=1}^{N} X_i\right) \left(\sum_{i=1}^{N} Y_i\right)$
$$M_{YY} = \sum_{i=1}^{N} y_i^2 = \sum_{i=1}^{N} (Y - \bar{Y})^2$$

= $N \left(\sum_{i=1}^{N} Y_i^2\right) - \sum_{i=1}^{N} (Y_i)^2$.

The slope of the regression line, b, can be found by

$$b = \frac{M_{XY}}{M_{XX}} \tag{2.9}$$

$$a = \frac{\sum_{i=1}^{N} Y_i}{N} - b \frac{\sum_{i=1}^{N} X_i}{N} = \bar{y} - b\bar{X}.$$
 (2.10)

The standard error of the regression line can be found in terms of the sample 83 moments. 84

$$S_{e}^{2} = \frac{M_{XX}(M_{YY}) - (M_{XY})^{2}}{N(N-2)M_{XX}}$$

$$S_{e} = \sqrt{S_{e}^{2}}.$$
(2.11)

The major benefit in calculating the sample moments is that the correlation 85 coefficient, *r*, and the coefficient of determination, r^2 , can easily be found. 86

$$r = \frac{M_{XY}}{(M_{XX})(M_{YY})}$$

$$R^{2} = (r)^{2}.$$
(2.12)

The coefficient of determination, R^2 , is the percentage of the variance of the dependent variable explained by the independent variable. The coefficient of determination cannot exceed 1 nor be less than zero. In the case of $R^2 = 0$, the regression line's Y = Y and no variation in the dependent variable are explained. If the dependent variable pattern continues as in the past, the model with time as the independent variable should be of good use in forecasting.

The firm can test whether the a and b coefficients are statistically different from zero, the generally accepted null hypothesis. A *t*-test is used to test the two null hypotheses:

96
$$H_{0_1}: a = 0$$

97 $H_{A_1}: a \text{ ne } 0$

98
$$H_{0_2}: \beta = 0$$

99
$$H_{A_2}$$
: β ne 0

100 where ne denotes not equal.

101 The H_0 represents the null hypothesis while H_A represents the alternative 102 hypothesis. To reject the null hypothesis, the calculated *t*-value must exceed the 103 critical *t*-value given in the *t*-tables in the appendix. The calculated *t*-values for *a* 104 and *b* are found by

$$t_{a} = \frac{a - \alpha}{S_{e}} \sqrt{\frac{N(M_{XX})}{M_{XX} + (N\bar{X})^{2}}}$$

$$t_{b} = \frac{b - \beta}{S_{e}} \sqrt{\frac{(M_{XX})}{N}}.$$
(2.13)

The critical *t*-value, t_c , for the 0.05 level of significance with N - 2 degrees of freedom can be found in a *t*-table in any statistical econometric text. One has a statistically significant regression model if one can reject the null hypothesis of the estimated slope coefficient.

We can create 95% confidence intervals for a and b, where the limits of a and b are

$$a + ta/{}_{2}S_{e}^{+}\sqrt{\frac{(N\bar{X})^{2} + M_{XX}}{N(M_{XX})}}$$

$$b + ta/{}_{2}S_{e}\sqrt{\frac{N}{M_{XX}}}.$$
(2.14)

111 To test whether the model is a useful model, an *F*-test is performed where

112 $H_0 = \alpha = \beta = 0$ 113 $H_A = \alpha$ ne β ne 0

$$F = \frac{\sum_{i=1}^{N} Y^2 \div 1 - \beta^2 \sum_{i=1}^{N} X_i^2}{\sum_{i=1}^{N} e^2 \div N - 2}.$$
 (2.15)

As the calculated *F*-value exceeds the critical *F*-value with (1, N - 2) degrees of 114 freedom of 5.99 at the 0.05 level of significance, the null hypothesis must be 115 rejected. The 95% confidence level limit of prediction can be found in terms of 116 the dependent variable value: 117

$$(a+bX_0) + ta/{}_2S_e\sqrt{\frac{N(X_0-\bar{X})^2}{1+N+M_{XX}}}.$$
(2.16)

Examples of Financial Economic Data

118

The most important use of simple linear regression as developed in (2.9) and (2.10) 119 is the estimation of a security beta. A security beta is estimated by running a 120 regression of 60 months of security returns as a function of market returns. The 121 market returns are generally the Standard & Poor's 500 (S&P500) index or a 122 capitalization-weighted index, such as the value-weighted Index from the Center 123 for Research in Security Prices (CRSP) at the University of Chicago. The data for 124 beta estimations can be downloaded from the Wharton Research Data Services 125 (WRDS) database. The beta estimation for IBM from January 2005 to December 126 2009, using monthly S&P 500 and the value-weighted CRSP Index, produces a beta 127 of approximately 0.80. Thus, if the market is expected to increase 10% in the 128 coming year, then one would expect IBM to return about 8%. The beta estimation of 129 IBM as a function of the S&P 500 Index using the SAS system is shown in 130 Table 2.1. The IBM beta is 0.80. The *t*-statistic of the beta coefficient, the slope 131 of the regression line, is 5.56, which is highly statistically significant. The critical 132 5% t-value is with 30 degrees of freedom 1.96, whereas the critical level of the t- 133 statistic at the 10% is 1.645. The IBM beta is statistically different from zero. The 134 IBM beta is not statistically different from one; the normalized z-statistical is 135 significantly less than 1. That is, 0.80 - 1.00 divided by the regression coefficient 136 standard error of 0.144 produces a Z-statistic of -1.39, which is less than the critical 137 level of -1.645 (at the 10% level) or -1.96 (at the 5% critical level). The IBM beta 138 is 0.78 (the corresponding *t*-statistic is 5.87) when calculated versus the value- 139 weighted CRSP Index.² 140

² See Fama, *Foundations of Finance*, 1976, Chapter 3, p. 101–2, for an IBM beta estimation with an equally weighted CRSP Index.

t1.1	Table 2.1 WRDS	IBM Beta 1/20	005-12/2009					
t1.2	Dependent variable: ret							
t1.3	Number of observations read: 60							
t1.4	Number of observa	tions used: 60						
t1.5	Analysis of variance	e						
t1.6	Source	DF	Sum of squares	Mean square	F-value	$\Pr > F$		
t1.7	Model	1	0.08135	0.08135	30.60	< 0.0001		
t1.8	Error	58	0.15419	0.00266				
t1.9	Corrected total	59	0.23554					
t1.10	Root MSE	0.05156	R^2	0.3454				
t1.11	Dependent mean	0.00808	Adjusted R^2	0.3341				
t1.12	Coeff var	638.12982				~		
t1.13	Parameter estimate	s						
t1.14	Variable	DF	Parameter estimate	Standard error	t-Value	$\Pr > t $		
t1.15	Intercept	1	0.00817	0.00666	1.23	0.2244		
t1.16	Sprtrn	1	0.80063	0.14474	5.53	< 0.0001		
t2.1	Table 2.2 An Esti	mated Consum	ption Function, 1947-	2011				
t2.2	Dependent variable	: RPCE						
t2.3	Method: least square	res						

12.0	Method. Iedst squares			- · ·	
t2.4	Sample(adjusted): 1,259				
t2.5	Included observations: 259	after adjusting endpo	oints		
t2.6	Variable	Coefficient	Std. error	t-Statistic	Prob.
t2.7	С	-120.0314	12.60258	-9.524349	0.0000
t2.8	RPDI	0.933251	0.002290	407.5311	0.0000
t2.9	R^2	0.998455	Mean dependent	var	4,319.917
t2.10	Adjusted R^2	0.998449	S.D. dependent v	ar	2,588.624
t2.11	S.E. of regression	101.9488	Akaike info crite	rion	12.09451
t2.12	Sum squared resid	2,671,147	Schwarz criterion		12.12198
t2.13	Log likelihood	-1,564.239	F-statistic		166,081.6
t2.14	Durbin-Watson stat	0.197459	Prob(F-statistic)		0.000000

Let us examine another source of real-business economic and financial data. The 141 142 St. Louis Federal Reserve Bank has an economic database, denoted FRED, containing some 41,000 economic series, available at no cost, via the Internet, at 143 http://research.stlouisfed.org/fred2. Readers are well aware that consumption 144 makes up the majority of real Gross Domestic Product, denoted GDP, the accepted 145 146 measure of output in our economy. Consumption is the largest expenditure, relative to gross investment, government spending, and net exports in GDP data. If we 147 download and graph real GDP and real consumption expenditures from FRED from 148 1947 to 2011, shown in Chart 2, one finds that real GDP and real consumption 149 expenditures, in 2005 \$, have risen substantially in the postwar period. Moreover, 150 there is a highly statistical significant relationship between real GDP and consump-151 tion if one estimates an ordinary least squares (OLS) line of the form of (2.8) with 152 real GDP as the dependent variable and real consumption as the independent 153 variable. The reader is referred to Table 2.2. 154

26

t3.1

Table 2.3	An estimated consumpti-	on function, with	lagged income

Dependent variable: RP	CE				t3.2
Method: least squares					t3.3
Sample(adjusted): 2,259)				t3.4
Included observations:	258 after adjusting en	ndpoints			t3.5
Variable	Coefficient	Std. error	t-Statistic	Prob.	t3.6
С	-118.5360	12.73995	-9.304274	0.0000	t3.7
RPDI	0.724752	0.126290	5.738800	0.0000	t3.8
LRPDI	0.209610	0.126816	1.652864	0.0996	t3.9
R^2	0.998470	Mean depend	Mean dependent var		t3.10
Adjusted R^2	0.998458	S.D. depende	nt var	2,585.986	t3.1′
S.E. of regression	101.5529	Akaike info c	riterion	12.09060	t3.12
Sum squared resid	2,629,810	Schwarz crite	Schwarz criterion		t3.13
Log likelihood	-1,556.687	F-statistic	<i>F</i> -statistic 83,1		t3.14
Durbin-Watson stat	0.127677	Prob(F-statist	tic)	0.000000	t3.1





The slope of consumption function is 0.93, and is highly statistically significant.³

The introduction of current and lagged income variables in the consumption 158 function regression produces statistically significant coefficients on both current 159 and lagged income, although the lagged income variable is statistically significant 160 at the 10% level. The estimated regression line, shown in Table 2.3, is highly 161 statistically significant. 162

³ In recent years the marginal propensity to consume has risen to the 0.90 to 0.97 range, see Joseph Stiglitz, *Economics*, 1993, p.745.

156 157 AU3

4.1	Table 2.4	An estimated	consumption	function,	with	twice-lagged	consump	otior

t4.2	Dependent variable: RP	CE			
t4.3	Method: least squares				
t4.4	Included observations: 2	257 after adjusting en	ndpoints		
t4.5	Variable	Coefficient	Std. error	t-Statistic	Prob.
t4.6	С	-120.9900	12.92168	-9.363331	0.0000
t4.7	RPDI	0.736301	0.126477	5.821607	0.0000
t4.8	LRPDI	0.229046	0.177743	1.288633	0.1987
t4.9	L2RPDI	-0.030903	0.127930	-0.241557	0.8093
t4.10	R^2	0.998474	Mean depend	ent var	4,344.661
t4.11	Adjusted R^2	0.998456	S.D. depende	nt var	2,583.356
t4.12	S.E. of regression	101.5049	Akaike info c	riterion	12.09353
t4.13	Sum squared resid	2,606,723	Schwarz crite	rion	12.14877
t4.14	Log likelihood	-1,550.019	F-statistic		55,188.63
t4.15	Durbin-Watson stat	0.130988	Prob(F-statist	ic)	0.000000

The introduction of current and once- and twice-lagged income variables in the consumption function regression produces statistically significant coefficients on both current and lagged income, although the lagged income variable is statistically significant at the 20% level. The twice-lagged income variable is not statistically regression line, shown in Table 2.4, is highly statistically significant.

169 Autocorrelation

170 An estimated regression equation is plagued by the first-order correlation of 171 residuals. That is, the regression error terms are not white noise (random) as is 172 assumed in the general linear model, but are serially correlated where

$$\varepsilon_t = \rho \varepsilon_{t=1} + U_t, \quad t = 1, 2, \dots, N \tag{2.17}$$

173 ε_t = regression error term at time t, ρ = first-order correlation coefficient, and 174 U_t = normally and independently distributed random variable.

The serial correlation of error terms, known as autocorrelation, is a violation of a regression assumption and may be corrected by the application of the Cochrane–Orcutt (CORC) procedure.⁴ Autocorrelation produces unbiased, the respected value of parameter is the population parameter, but inefficient parameters. The variances of the parameters are biased (too low) among the set of linear unbiased estimators and the sample *t*- and *F*-statistics are too large. The CORC

⁴ D. Cochrane and G.H. Orcutt, "Application of Least Squares Regression to Relationships Containing Autocorrelated Error Terms," *Journal of the American Statistical Association*, 1949, 44: 32–61.

Autocorrelation

procedure was developed to produce the best linear unbiased estimators (BLUE) 181 given the autocorrelation of regression residuals. The CORC procedure uses the 182 information implicit in the first-order correlative of residuals to produce unbiased 183 and efficient estimators: 184

$$Y_t = \alpha + \beta X_t + \varepsilon_t$$
$$\hat{\rho} = \frac{\sum e_t, e_t - 1}{\sum e_t^2 - 1}.$$

The dependent and independent variables are transformed by the estimated rho, 185 $\hat{\rho}$, to obtain more efficient OLS estimates: 186

$$Y_t - \rho Y_{t-1} = \alpha (l - \rho) + \beta (X_t - \rho X_{t-1}) + ut.$$
(2.19)

The CORC procedure is an iterative procedure that can be repeated until the 187 coefficients converge. One immediately recognizes that as ρ approaches unity the 188 regression model approaches a first-difference model.

The Durbin–Watson, D-W, statistic was developed to test for the absence of 190 autocorrelation: 191

$$H_0: \rho = 0.$$
 192

One generally tests for the presence of autocorrelation ($\rho = 0$) using the 193 Durbin–Watson statistic: 194

$$D - W = d = \frac{\sum_{t=2}^{N} (e_t = e_{t-1})^2}{\sum_{t=2}^{N} e_t^2}.$$
 (2.20)

The *es* represent the OLS regression residuals and a two-tailed tail is employed 195 to examine the randomness of residuals. One rejects the null hypothesis of no 196 statistically significant autocorrelation if 197

$$d < d_{\rm L}$$
 or $d > 4 - d_{\rm U}$,

where $d_{\rm L}$ is the "lower" Durbin–Watson level and $d_{\rm U}$ is the "upper" Durbin–Watson 198 level.

The upper and lower level Durbin–Watson statistic levels are given in Johnston 200 (1972). The Durbin–Watson statistic is used to test only for first-order correlation 201 among residuals. 202

$$D = 2(1 - \rho). \tag{2.21}$$

If the first-order correlation of model residuals is zero, the Durbin–Watson 203 statistic is 2. A very low value of the Durbin–Watson statistic, $d < d_L$, indicates 204

t5.1 Table 2.5 An estimated consumption function, 1947–2011

t5.2	Dependent variable: D(RPC	CE)								
t5.3	Method: least squares									
t5.4	Included observations: 258	after adjusting endpo	oints							
t5.5	Variable	Coefficient	Std. error	t-Statistic	Prob.					
t5.6	C	22.50864	2.290291	9.827849	0.0000					
t5.7	D(RPDI)	0.280269	0.037064	7.561802	0.0000					
t5.8	R^2	0.182581	Mean dependent	var	32.18062					
t5.9	Adjusted R^2	0.179388	S.D. dependent var		33.68691					
t5.10	S.E. of regression	30.51618	Akaike info criterion		9.682113					
t5.11	Sum squared resid	238,396.7	Schwarz criterion		9.709655					
t5.12	Log likelihood	-1,246.993	F-statistic		57.18084					
t5.13	Durbin-Watson stat	1.544444	Prob(F-statistic)		0.000000					

205 positive autocorrelation between residuals and produces a regression model that is 206 not statistically plagued by autocorrelation.

207 The inconclusive range for the estimated Durbin–Watson statistic is

$$d_{\rm L} < d < d_{\rm U}$$
 or $4 - d_{\rm U} < 4 - d_{\rm U}$.

One does not reject the null hypothesis of no autocorrelation of residuals if 209 $d_{\rm U} < d < 4 - d_{\rm U}$.

210 One of the weaknesses of the Durbin–Watson test for serial correlation is that 211 only first-order autocorrelation of residuals is examined; one should plot the 212 correlation of residual with various time lags

$$\operatorname{corr}(e_t, e_{t-k})$$

213 to identify higher-order correlations among residuals.

The reader may immediately remember that the regressions shown in Tables 2.1–2.3 had very low Durbin–Watson statistics and were plagued by autocorrelation. We first-difference the consumption function variables and rerun the regressions, producing Tables 2.5–2.7. The R^2 values are lower, but the regressions are not plagued by autocorrelation. In financial economic modeling, one generally first-differences the data to achieve stationarity, or a series with a constant standard deviation.

The introduction of current and lagged income variables in the consumption function regression produces statistically significant coefficients on both current and lagged income, although the lagged income variable is statistically significant at the 10% level. The estimated regression line, shown in Table 2.6, is highly statistically significant, and is not plagued by autocorrelation.

The introduction of current and lagged income variables in the consumption function regression produces statistically significant coefficients on both current and lagged income, statistically significant at the 1% level. The estimated regression line, shown in Table 2.5, is highly statistically significant, and is not plagued by autocorrelation.

Table 2.0 An estimated consumption function, with lagged incom	Table 2.6	An estimated	consumption	function.	with lagged incon
---	-----------	--------------	-------------	-----------	-------------------

Dependent variable: D(RPCE)				t6.2		
Method: least squares							
Included observations:	ncluded observations: 257 after adjusting endpoints						
Variable	Coefficient	Std. error	t-Statistic	Prob.	t6.5		
С	14.20155	2.399895	5.917570	0.0000	t6.6		
D(RPDI)	0.273239	0.034027	8.030014	0.0000	t6.7		
D(LRPDI)	0.245108	0.034108	7.186307	0.0000	t6.8		
R^2	0.320314	Mean depende	Mean dependent var		t6.9		
Adjusted R^2	0.314962	S.D. depender	S.D. dependent var		t6.10		
S.E. of regression	27.92744	Akaike info c	riterion	9.508701	t6.11		
Sum squared resid	198,105.2	Schwarz crite	Schwarz criterion		t6.12		
Log likelihood	-1,218.868	F-statistic	F-statistic		t6.13		
Durbin-Watson stat	1.527716	Prob(F-statist	ic)	0.000000	t6.14		

Table 2.7	An estimated	consumption	function.	with twice-	lagged	consumption	

Dependent variable: D(RPCE) t7						
Method: least squares						
Included observations: 25	6 after adjusting en	dpoints			t7.4	
Variable	Coefficient	Std. error	t-Statistic	Prob.	t7.5	
С	12.78746	2.589765	4.937692	0.0000	t7.6	
D(RPDI)	0.262664	0.034644	7.581744	0.0000	t7.7	
D(LRPDI)	0.242900	0.034162	7.110134	0.0000	t7.8	
D(L2RPDI)	0.054552	0.034781	1.568428	0.1180	t7.9	
R^2	0.325587	Mean depende	Mean dependent var		t7.10	
Adjusted R^2	0.317558	S.D. depender	nt var	33.76090	t7.11	
S.E. of regression	27.88990	Akaike info ci	riterion	9.509908	t7.12	
Sum squared resid	196,017.3	Schwarz criter	rion	9.565301	t7.13	
Log likelihood	-1,213.268	F-statistic		40.55269	t7.14	
Durbin-Watson stat	1.535845	Prob(F-statisti	ic)	0.000000	t7.15	

The introduction of current and once- and twice-lagged income variables in the 231 consumption function regression produces statistically significant coefficients on 232 both current and lagged income, although the twice-lagged income variable is 233 statistically significant at the 15% level. The estimated regression line, shown in 234 Table 2.7, is highly statistically significant, and is not plagued by autocorrelation. 235

Many economic time series variables increase as a function of time. In such 236 cases, a nonlinear least squares (NLLS) model may be appropriate; one seeks to 237 estimate an equation in which the dependent variable increases by a constant 238 growth rate rather than a constant amount.⁵ The nonlinear regression equation is 239 AU4

t6.1

t7.1

⁵ The reader is referred to C.T. Clark and L.L. Schkade, Statistical Analysis for Administrative Decisions (Cincinnati: South-Western Publishing Company, 1979) and Makridakis, Wheelwright, and Hyndman, *Op. Cit.*, 1998, pages 221–225, for excellent treatments of this topic.

2 Regression Analysis and Forecasting Models

$$Y = ab^{x}$$

or log $Y = \log a + \log BX$. (2.22)

The normal equations are derived from minimizing the sum of the squared error terms (as in OLS) and may be written as

$$\sum (\log Y) = N(\log a) + (\log b) \sum X$$

$$\sum (X \log Y) = (\log a) \sum X + (\log b) \sum X^{2}.$$
 (2.23)

242 The solutions to the simplified NLLS estimation equation are

$$\log a = \frac{\sum (\log Y)}{N}$$

$$\log b = \frac{\sum (X \log Y)}{\sum X^2}.$$
(2.24)
(2.25)

X

243 Multiple Regression

It may well be that several economic variables influence the variable that one is interested in forecasting. For example, the levels of the Gross National Product (GNP), personal disposable income, or price indices can assert influences on the firm. Multiple regression is an extremely easy statistical tool for researchers and management to employ due to the great proliferation of computer software. The general form of the two-independent variable multiple regression is

$$Y_t = \beta_1 + \beta_2 X_{2t} + \beta_3 X_{3t} + \varepsilon_t, \quad t = 1, \dots, N.$$
 (2.26)

250 In matrix notation multiple regression can be written:

$$Y = X\beta + \varepsilon. \tag{2.27}$$

Multiple regression requires unbiasedness, the expected value of the error term is zero, and the *X*'s are fixed and independent of the error term. The error term is an identically and independently distributed normal variable. Least squares estimation of the coefficients yields

$$\hat{\beta} = (\hat{\beta}_1, \, \hat{\beta}_2, \, \hat{\beta}_3)$$

$$Y = X\hat{\beta} + e.$$
(2.28)

Multiple regression, using the least squared principle, minimizes the sum of the 255 squared error terms: 256

$$\sum_{i=1}^{N} e_{1}^{2} = e'e$$

$$(Y - X\hat{\beta})'(Y - X\hat{\beta}).$$
(2.29)

To minimize the sum of the squared error terms, one takes the partial derivative 257 of the squared errors with respect to $\hat{\beta}$ and the partial derivative set equal to zero. 258

$$\partial \frac{(e'e)}{\partial \beta} = -2X'Y + 2X'X\hat{\beta} = 0$$

$$\hat{\beta} = (X'X)^{-1}X'Y.$$
(2.30)

Alternatively, one could solve the normal equations for the two-variable to 259 determine the regression coefficients. 260

$$\sum Y = \beta_1 N + \hat{\beta}_2 \sum X_2 + \hat{\beta}_3 \sum X_3$$

$$\sum X_2 Y = \hat{\beta}_1 \sum X_2 + \hat{\beta}_2 X_2^2 + \hat{\beta}_3 \sum X_3^2$$

$$\sum X_3 Y = \hat{\beta}_1 \sum X_3 + \hat{\beta}_2 \sum X_2 X_3 + \hat{\beta}_3 \sum X_3^2.$$
(2.31)

When we solved the normal equation, (2.7), to find the *a* and *b* that minimized 261 the sum of our squared error terms in simple liner regression, and when we solved 262 the two-variable normal equation, equation (2.31), to find the multiple regression 263 estimated parameters, we made several assumptions. First, we assumed that the 264 error term is independently and identically distributed, i.e., a random variable with 265 an expected value, or mean of zero, and a finite, and constant, standard deviation. 266 The error term should not be a function of time, as we discussed with the 267 Durbin–Watson statistic, equation (2.21), nor should the error term be a function 268 of the size of the independent variable(s), a condition known as heteroscedasticity. 269 One may plot the residuals as a function of the independent variable(s) to be certain 270 that the residuals are independent of the independent variables. The error term 271 should be a normally distributed variable. That is, the error terms should have an 272 expected value of zero and 67.6% of the observed error terms should fall within the 273 mean value plus and minus one standard deviation of the error terms (the so-called 274 Bell Curve or normal distribution). Ninety-five percent of the observations should 275 fall within the plus or minus two standard deviation levels, the so-called 95% 276 confidence interval. The presence of extreme, or influential, observations may 277 distort estimated regression lines and the corresponding estimated residuals. 278 Another problem in regression analysis is the assumed independence of the 279

independent variables in equation (2.31). Significant correlations may produce estimated regression coefficients that are "unstable" and have the "incorrect" signs, conditions that we will observe in later chapters. Let us spend some time discussing two problems discussed in this section, the problems of influential observations, commonly known as outliers, and the correlation among independent variables, known as multicollinearity.

There are several methods that one can use to identify influential observations or 286 outliers. First, we can plot the residuals and 95% confidence intervals and examine 287 how many observations have residuals falling outside these limits. One should 288 289 expect no more than 5% of the observations to fall outside of these intervals. One may find that one or two observations may distort a regression estimate even if there 290 291 are 100 observations in the database. The estimated residuals should be normally distributed, and the ratio of the residuals divided by their standard deviation, known 292 as standardized residuals, should be a normal variable. We showed, in equation 293 (2.31), that in multiple regression 294

$$\hat{\beta} = (X'X)X'Y$$

²⁹⁵ The residuals of the multiple regression line are given by

$$e=Y'-\hat{\beta}X.$$

The standardized residual concept can be modified such that the reader can calculate a variation on that term to identify influential observations. If we delete observation i in a regression, we can measure the change in estimated regression coefficients and residuals. Belsley et al. (1980) showed that the estimated regression coefficients change by an amount, DFBETA, where

DFBETA_i =
$$\frac{(X'X)^{-1}X'e_i}{1-h_i}$$
, (2.32)

301 where $h_i = X_i (X'X)^{-1} X'_i$.

The h_i or "hat" term is calculated by deleting observation *i*. The corresponding residual is known as the studentized residual, sr, and defined as

$$\mathrm{sr}_i = \frac{e_i}{\hat{\sigma}\sqrt{1-h_i}},\tag{2.33}$$

where $\hat{\sigma}$ is the estimated standard deviation of the residuals. A studentized residual that exceeds 2.0 indicates a potential influential observation (Belsley et al. 1980). Another distance measure has been suggested by Cook (1977), which modifies the studentized residual, to calculate a scaled residual known as the Cook distance measure, CookD. As the researcher or modeler deletes observations, one needs to

AU5

compare the original matrix of the estimated residual's variance matrix. The 309 COVRATIO calculation performs this calculation, where 310

COVRATIO =
$$\frac{1}{\left[\frac{n-p-1}{n-p} + \frac{e_i^*}{(n-p)}\right]^p (1-h_i)}$$
, (2.34)

where n = number of observations, p = number of independent variables, and 311 $e_i^* =$ deleted observations. 312

If the absolute value of the deleted observation >2, then the COVRATIO 313 calculation approaches 314

$$1 - \frac{3p}{n}.\tag{2.35}$$

A calculated COVRATIO that is larger than 3p/n indicates an influential obser- 315 vation. The DFBETA, studentized residual, CookD, and COVRATIO calculations 316 may be performed within SAS. The identification of influential data is an important 317 component of regression analysis. One may create variables for use in multiple 318 regression that make use of the influential data, or outliers, to which they are 319 commonly referred. 320

The modeler can identify outliers, or influential data, and rerun the OLS 321 regressions on the re-weighted data, a process referred to as robust (ROB) regres-322 sion. In OLS all data is equally weighted. The weights are 1.0. In ROB regression 323 one weights the data universally with its OLS residual; i.e., the larger the residual, 324 the smaller the weight of the observation in the ROB regression. In ROB regression, 325 several weights may be used. We will see the Huber (1973) and Beaton-Tukey 326 (1974) weighting schemes in our analysis. In the Huber robust regression proce-327 dure, one uses the following calculation to weigh the data: 328

$$w_i = \left(1 - \left(\frac{|e_i|}{\sigma_i}\right)^2\right)^2, \qquad (2.36)$$

where e_i = residual *i*, σ_i = standard deviation of residual, and w_i = weight of 329 observation *i*. 330

The intuition is that the larger the estimated residual, the smaller the weight. 331 A second robust re-weighting scheme is calculated from the Beaton-Tukey 332 biweight criteria where 333

$$w_{i} = \left(1 - \left(\frac{\frac{|e_{i}|}{\sigma_{e}}}{4.685}\right)^{2}\right)^{2}, \quad \text{if } \frac{|e_{i}|}{\sigma_{e}} > 4.685;$$

$$1, \quad \text{if } \frac{|e_{i}|}{\sigma_{e}} < 4.685.$$
(2.37)

2 Regression Analysis and Forecasting Models

A second major problem is one of multicollinearity, the condition of correlations 334 among the independent variables. If the independent variables are perfectly 335 correlated in multiple regression, then the (X'X) matrix of (2.31) cannot be inverted 336 and the multiple regression coefficients have multiple solutions. In reality, highly 337 correlated independent variables can produce unstable regression coefficients due 338 to an unstable $(X'X)^{-1}$ matrix. Belsley et al. advocate the calculation of a condition 339 number, which is the ratio of the largest latent root of the correlation matrix relative 340 to the smallest latent root of the correlation matrix. A condition number exceeding 341 30.0 indicates severe multicollinearity. 342

The latent roots of the correlation matrix of independent variables can be used to state setimate regression parameters in the presence of multicollinearity. The latent roots, $l_1, l_2, ..., l_p$ and the latent vectors $\gamma_1, \gamma_2, ..., \gamma_p$ of the *P* independent variables can describe the inverse of the independent variable matrix of (2.29).

(

$$X'X)^{-1} = \sum_{j=1}^p l_j^{-1} \gamma_j \gamma'_j.$$

Multicollinearity is present when one observes one or more small latent vectors. If one eliminates latent vectors with small latent roots (l < 0.30) and latent vectors ($\gamma < 0.10$), the "principal component" or latent root regression estimator may be written as

$$\hat{\beta}_{\text{LRR}} = \sum_{j=0}^{P} f_j \delta_j$$

where
$$f_j = \frac{-\eta}{\sum}$$

where n^2

 $= \Sigma(v - \bar{v})$

351 352

and λ are the "nonzero" latent vectors. One eliminates the latent vectors with non-predictive multicollinearity. We use latent root regression on the Beaton-Tukey weighted data in Chap. 4.

The Conference Board Composite Index of Leading Economic Indicators and Real US GDP Growth: A Regression Example

The composite indexes of leading (leading economic indicators, LEI), coincident, and lagging indicators produced by The Conference Board are summary statistics for the US economy. Wesley Clair Mitchell of Columbia University constructed the indicators in 1913 to serve as a barometer of economic activity. The leading indicator series was developed to turn upward before aggregate economic activity increased, and decrease before aggregate economic activity diminished. AU7

AU6

Historically, the cyclical turning points in the leading index have occurred before 364 those in aggregate economic activity, cyclical turning points in the coincident index 365 have occurred at about the same time as those in aggregate economic activity, and 366 cyclical turning points in the lagging index generally have occurred after those in 367 aggregate economic activity. 368

The Conference Board's components of the composite leading index for the 369 year 2002 reflects the work and variables shown in Zarnowitz (1992) list, which 370 continued work of the Mitchell (1913, 1927, 1951), Burns and Mitchell (1946), and 371 AU8 Moore (1961). The Conference Board index of leading indicators is composed of 372

1.	Average weekly hours (mfg.)	373
2.	Average weekly initial claims for unemployment insurance	374
3.	Manufacturers' new orders for consumer goods and materials	375
4.	Vendor performance	376
5.	Manufacturers' new orders of nondefense capital goods	377
6.	Building permits of new private housing units	378
7.	Index of stock prices	379
8.	Money supply	380
9.	Interest rate spread	381
10.	Index of consumer expectations	382

The Conference Board composite index of LEI is an equally weighted index in 383 which its components are standardized to produce constant variances. Details of the 384 LEI can be found on The Conference Board Web site, www.conference-board.org, 385 and the reader is referred to Zarnowitz (1992) for his seminal development of 386 underlying economic assumption and theory of the LEI and business cycles 387 AU9 (Table 2.8). 388

Let us illustrate a regression of real US GDP as a function of current and lagged 389 LEI. The regression coefficient on the LEI variable, 0.232, in Table 2.9, is highly 390 statistically significant because the calculated *t*-value of 6.84 exceeds 1.96, the 5% 391 critical level. One can reject the null hypothesis of no association between the 392 growth rate of US GDP and the growth rate of the LEI. The reader notes, however, 393 that we estimated the regression line with current, or contemporaneous, values of 394 the LEI series. 395

The LEI series was developed to "forecast" future economic activity such that 396 current growth of the LEI series should be associated with future US GDP growth 397 rates. Alternatively, one can examine the regression association of the current 398 values of real US GDP growth and previous or lagged values, of the LEI series. 399 How many lags might be appropriate? Let us estimate regression lines using up to 400 four lags of the US LEI series. If one estimates multiple regression lines using the 401 EViews software, as shown in Table 2.10, the first lag of the LEI series is statistically significant, having an estimated *t*-value of 5.73, and the second lag is also 403 statistically significant, having an estimated *t*-value of 4.48. In the regression 404 analysis using three lags of the LEI series, the first and second lagged variables 405 are highly statistically significant, and the third lag is not statistically significant 406 because third LEI lag variable has an estimated *t*-value of only 0.12. The critical 407

t8.1 Table 2.8 The conference board leading, coincident, and lagging indicator components

				-
t8.2	Lead	ding index		Standardization factor
t8.3	1	BCI-01	Average weekly hours, manufacturing	0.1946
t8.4	2	BCI-05	Average weekly initial claims for unemployment insurance	0.0268
t8.5	3	BCI-06	Manufacturers' new orders, consumer goods and materials	0.0504
t8.6	4	BCI-32	Vendor performance, slower deliveries diffusion index	0.0296
t8.7	5	BCI-27	Manufacturers' new orders, nondefense capital goods	0.0139
t8.8	6	BCI-29	Building permits, new private housing units	0.0205
t8.9	7	BCI019	Stock prices, 500 common stocks	0.0309
t8.10	8	BCI-106	Money supply, M2	0.2775
t8.11	9	BCI-129	Interest rate spread, 10-year Treasury bonds less federal funds	0.3364
t8.12	10	BCI-83	Index of consumer expectations	0.0193
t8.13	Coir	ncident inde	X	
t8.14	1	BCI-41	Employees on nonagricultural payrolls	0.5186
t8.15	2	BCI-51	Personal income less transfer payments	0.2173
t8.16	3	BCI-47	Industrial production	0.1470
t8.17	4	BCI-57	Manufacturing and trade sales	0.1170
t8.18	Lag	ging index		
t8.19	1	BCI-91	Average duration of unemployment	0.0368
t8.20	2	BCI-77	Inventories-to-sales ratio, manufacturing and trade	0.1206
t8.21	3	BCI-62	Labor cost per unit of output, manufacturing	0.0693
t8.22	4	BCI-109	Average prime rate	0.2692
t8.23	5	BCI-101	Commercial and industrial loans	0.1204
t8.24	6	BCI-95	Consumer installment credit-to-personal income ratio	0.1951
t8.25	7	BCI-120	Consumer price index for services	0.1886

t9.1 Table 2.9 Real US GDP and the leading indicators: A contemporaneous examination

t9.2	Dependent variable: DLOG(RGDP)									
t9.3	Sample(adjusted): 2,210									
t9.4	Included observations: 209	after adjusting endp	oints							
t9.5	Variable	Coefficient	Std. error	t-Statistic	Prob.					
t9.6	С	0.006170	0.000593	10.40361	0.0000					
t9.7	DLOG(LEI)	0.232606	0.033974	6.846529	0.0000					
t9.8	R^2	0.184638	Mean dependent	var	0.007605					
t9.9	Adjusted R^2	0.180699	S.D. dependent v	ar	0.008860					
t9.10	S.E. of regression	0.008020	Akaike info crite	rion	-6.804257					
t9.11	Sum squared resid	0.013314	Schwarz criterior	1	-6.772273					
t9.12	Log likelihood	713.0449	F-statistic		46.874971					
t9.13	Durbin-Watson stat	1.594358	Prob(F-statistic)		0.000000					

408 *t*-level at the 10% level is 1.645, for 30 observations, and statistical studies often use 409 the 10% level as a minimum acceptable critical level. The third lag is not statisti-410 cally significant in the three quarter multiple regression analysis. In the four quarter

411 lags analysis of the LEI series, we report that the lag one variable has a *t*-statistic of

Table 2.10 Real GDP and the conference board leading economic indicators

1959 Q1	l–2011 Q2								t10.2
			Lags (LEI)						t10.3
Model	Constant	LEI	One	Two	Three	Four	R^2	F-statistic	t10.4
RGDP	0.006	0.232					0.181	46.875	t10.5
(<i>t</i>)	10.400	6.850							t10.6
RGDP	0.056	0.104	0.218				0.285	42.267	t10.7
	9.910	2.750	5.730						t10.8
RGDP	0.005	0.095	0.136	0.162			0.353	38.45	t10.9
	9.520	2.600	3.260	4.480					t10.1
RGDP	0.005	0.093	0.135	0.164	0.005		0.351	28.679	t10.1
	9.340	2.530	3.220	3.900	0.120			6	t10.1
RGDP	0.005	0.098	0.140	0.167	-0.041	0.061	0.369	24.862	t10.1
	8.850	2.680	3.360	4.050	-0.990	1.670			t10.1

Table 2.11 The REG procedure

Table 2.11 The REG p	orocedure				t11.1
Dependent variable: DL	USGDP		\sim		t11.2
Sample(adjusted): 6,210)				t11.3
Included observations: 2	205 after adjusting e	ndpoints			t11.4
Variable	Coefficient	Std. error	t-Statistic	Prob.	t11.5
С	0.004915	0.000555	8.849450	0.0000	t11.6
DLOG(LEI)	0.098557	0.036779	2.679711	0.0080	t11.7
DLOG(L1LEI)	0.139846	0.041538	3.366687	0.0009	t11.8
DLOG(L2LEI)	0.167168	0.041235	4.054052	0.0001	t11.9
DLOG(L3LEI)	-0.041170	0.041305	-0.996733	0.3201	t11.1
DLOG(L4LEI)	0.060672	0.036401	1.666786	0.0971	t11.1
R^2	0.384488	Mean depend	ent var	0.007512	t11.1
Adjusted R^2	0.369023	S.D. depende	nt var	0.008778	t11.1
S.E. of regression	0.006973	Akaike info c	riterion	-7.064787	t11.1
Sum squared resid	0.009675	Schwarz crite	Schwarz criterion		t11.1
Log likelihood	730.1406	F-statistic		24.86158	t11.1
Durbin-Watson stat	1.784540	Prob(F-statist	ic)	0.000000	t11.1

3.36, highly significant; the second lag has a *t*-statistic of 4.05, which is statistically 412 significant; the third LEI lag variable has a *t*-statistic of -0.99, not statistically 413 significant at the 10% level; and the fourth LEI lag variable has an estimated 414 t-statistic of 1.67, which is statistically significant at the 10% level. The estimation 415 of multiple regression lines would lead the reader to expect a one, two, and four 416 variable lag structure to illustrate the relationship between real US GDP growth and 417 The Conference Board LEI series. The next chapter develops the relationship using 418 time series and forecasting techniques. This chapter used regression analysis to 419 illustrate the association between real US GDP growth and the LEI series. 420

The reader is referred to Table 2.11 for EViews output for the multiple regres- 421 sion of the US real GDP and four quarterly lags in LEI. 422

39

t10.1

t12.1 Table 2.12	The REG proc	edure model: MC	JDELI						
t12.2 Dependent v	t12.2 Dependent variable: dlRGDP								
t12.3 Number of o	observations rea	nd: 209							
t12.4 Number of o	observations use	ed: 205							
t12.5 Number of o	observations wi	th missing values	s: 4						
t12.6 Analysis of	variance								
t12.7 Source	DF	Sum of squares	Mean square	<i>F</i> -value	$\Pr > F$				
t12.8 Model	5	0.00604	0.00121	24.85	< 0.0001				
t12.9 Error	199	0.00968	0.00004864						
t12.10 Corrected total	204	0.01572							
t12.11	Root MSE	0.00697	R^2	0.3844		X			
t12.12	Dependent mean	0.00751	Adjusted R^2	0.3689					
t12.13	Coeff. var	92.82825							
t12.14 Parameter e	stimates								
Variable	DF	Parameter	Standard	t-Value	$\Pr > t $	Variance			
t12.15		estimate	error			inflation			
t12.16 Intercept	1	0.00492	0.00055545	8.85	< 0.0001	0			
t12.17 dlLEI	1	0.09871	0.03678	2.68	0.0079	1.52694			
t12.18 dlLEI_1	1	0.13946	0.04155	3.36	0.0009	1.94696			
t12.19 dlLEI_2	1	0.16756	0.04125	4.06	< 0.0001	1.92945			
t12.20 dlLEI_3	1	-0.04121	0.04132	-1.00	0.3198	1.93166			
t12.21 dlLEI_4	1	0.06037	0.03641	1.66	0.0989	1.50421			
t12.22 Collinearity	diagnostics	(
t12.23 Number	Eigenvalue	Condition index							
t12.24 1	3.08688	1.00000							
t12.25 2	1.09066	1.68235							
t12.26 3	0.74197	2.03970							
t12.27 4	0.44752	2.62635							
t12.28 5	0.37267	2.87805							
t12.296	0.26030	3.44367							
t12.30 Proportion of	of variation								
t12.31 Number	Intercept	dILEI	dlLEI_1	dlLEI_2	dlLEI_3	dlLEI_4			
t12.32 1	0.02994	0.02527	0.02909	0.03220	0.02903	0.02481			
t12.33 2	0.00016369	0.18258	0.05762	0.00000149	0.06282	0.19532			
t12.34 3	0.83022	0.00047128	0.02564	0.06795	0.02642	0.00225			
t12.354	0.12881	0.32579	0.00165	0.38460	0.00156	0.38094			
t12.36 5	0.00005545	0.25381	0.41734	0.00321	0.44388	0.19691			
t12.37 <u>6</u>	0.01081	0.21208	0.46866	0.51203	0.43629	0.19977			

t12.1 Table 2.12 The REG procedure model: MODEL1

We run the real GDP regression with four lags of LEI data in SAS. We report the SAS output in Table 2.12. The Belsley et al. (1980) condition index of 3.4 reveals little evidence of multicollinearity and the collinearity diagnostics reveal no two variables in a row exceeding 0.50. Thus, SAS allows the researcher to specifically address the issue of multicollinearity. We will return to this issue in Chap. 4.

Table 2.13 Mod	leling dlRGDP by OLS				
	Coefficient	Std. error	<i>t</i> -Value	t-Prob	Part. R^2
Constant	0.00491456	0.0005554	8.85	0.0000	0.2824
dILEI	0.0985574	0.03678	2.68	0.0080	0.0348
dlLEI_1	0.139846	0.04154	3.37	0.0009	0.0539
dlLEI_2	0.167168	0.04123	4.05	0.0001	0.0763
dlLEI_3	-0.0411702	0.04131	-0.997	0.3201	0.0050
dlLEI_4	0.0606721	0.03640	1.67	0.0971	0.0138
Sigma	0.00697274	RSS	0.00967519164		
R^2	0.384488; F(5,199) = 24.	86 [0.000]**			
Adjusted R^2	0.369023	Log-likelihood	730.141		
No. of observations	205	No. of parameters	6	X	
Mean(dlRGDP)	0.00751206	S.E.(dlRGDP)	0.00877802		×
AR 1–2 test:	F(2,197) = 3.6873 [0.0268]*				
ARCH 1-1 test:	F(1,203) = 1.6556 [0.1997]		\sim		
Normality test:	Chi-squared(2) = 17.824 [0.0001]**		X		
Hetero test:	F(10,194) = 0.86780 [0.5644]				
Hetero-X test:	F(20,184) = 0.84768 [0.6531]	xO	7		
RESET23 test:	F(2,197) = 2.9659 [0.0538]				

The SAS estimates of the regression model reported in Table 2.12 would lead the 428 reader to believe that the change in real GDP is associated with current, lagged, and 429 twice-lagged LEI. 430

Alternatively, one could use Oxmetrics, an econometric suite of products for 431 data analysis and forecasting, to reproduce the regression analysis shown in 432 Table 2.13.⁶ 433

An advantage to Oxmetrics is its Automatic Model selection procedure that 434 addresses the issue of outliers. One can use the Oxmetrics Automatic Model 435 selection procedure and find two statistically significant lags on LEI and three 436 outliers: the economically volatile periods of 1971, 1978, and (the great recession 437 of) 2008 (Table 2.14). 438 [AU11]

The reader clearly sees the advantage of the Oxmetrics Automatic Model 439 selection procedure. 440

⁶Ox Professional version 6.00 (Windows/U) (C) J.A. Doornik, 1994–2009, PcGive 13.0.See Doornik and Hendry (2009a, b).

t14.2	Coefficient	Std. error	t-Value	t-Prob	Part. R^2
t14.3 Constant	0.00519258	0.0004846	10.7	0.0000	0.3659
t14.4 dlLEI_1	0.192161	0.03312	5.80	0.0000	0.1447
t14.5 dlLEI_2	0.164185	0.03281	5.00	0.0000	0.1118
t14.6 I:1971-01-01	0.0208987	0.006358	3.29	0.0012	0.0515
t14.7 I:1978-04-01	0.0331323	0.006352	5.22	0.0000	0.1203
t14.8 I:2008-10-01	-0.0243503	0.006391	-3.81	0.0002	0.0680
t14.9 Sigma	0.00633157	RSS	0.007977675	502	
t14.10 <i>R</i> ²	0.49248	F(5,199) = 38.62 [0.000]**			
t14.11 Adjusted R^2	0.479728	Log-likelihood	749.915	X	
t14.12 No. of	205	No. of parameters	6		
observations					*
t14.13 Mean(dlRGDP)	0.00751206	se(dlRGDP)	0.00877802		
t14.14 AR 1–2 test:	F(2,197) = 3.2141 [0.0423]*		~		
t14.15 ARCH 1-1 test:	F(1,203) = 2.3367 [0.1279]		\bigcirc		
t14.16 Normality test:	Chi-squared (2) = 0.053943 [0.9734]	6			
t14.17 Hetero test:	F(4,197) = 3.2294 [0.0136]*	ר			
t14.18 Hetero-X test:	F(5,196) = 2.5732 [0.0279]*				
t14.19 RESET23 test:	F(2,197) = 1.2705 [0.2830]				

t14.1 Table 2.14 Modeling dlRGDP by OLS

441 Summary

In this chapter, we introduced the reader to regression analysis and various estimation procedures. We have illustrated regression estimations by modeling consumption functions and the relationship between real GDP and The Conference Board LEI. We estimated regressions using EViews, SAS, and Oxmetrics. There are many advantages with the various regression software with regard to ease of use, outlier estimations, collinearity diagnostics, and automatic modeling procedures. We will use the regression techniques in Chap. 4.

449 Appendix

450 Let us follow The Conference Board definitions of the US LEI series and its 451 components:

Leading Index Components

452

BCI-01 Average weekly hours, manufacturing. The average hours worked per week 453 by production workers in manufacturing industries tend to lead the business cycle 454 because employers usually adjust work hours before increasing or decreasing their 455 workforce. 456

BCI-05 Average weekly initial claims for unemployment insurance. The number of 457 new claims filed for unemployment insurance is typically more sensitive than either 458 total employment or unemployment to overall business conditions, and this series 459 tends to lead the business cycle. It is inverted when included in the leading index; 460 the signs of the month-to-month changes are reversed, because initial claims 461 increase when employment conditions worsen (i.e., layoffs rise and new hirings 462 fall).

BCI-06 Manufacturers' new orders, consumer goods and materials (in 1996 \$). 464 These goods are primarily used by consumers. The inflation-adjusted value of new 465 orders leads actual production because new orders directly affect the level of both 466 unfilled orders and inventories that firms monitor when making production 467 decisions. The Conference Board deflates the current dollar orders data using 468 price indexes constructed from various sources at the industry level and a chainweighted aggregate price index formula. 470

BCI-32 Vendor performance, slower deliveries diffusion index. This index 471 measures the relative speed at which industrial companies receive deliveries from 472 their suppliers. Slowdowns in deliveries increase this series and are most often 473 associated with increases in demand for manufacturing supplies (as opposed to a 474 negative shock to supplies) and, therefore, tend to lead the business cycle. Vendor 475 performance is based on a monthly survey conducted by the National Association 476 of Purchasing Management (NAPM) that asks purchasing managers whether their 477 suppliers' deliveries have been faster, slower, or the same as the previous month. 478 The slower-deliveries diffusion index counts the proportion of respondents 479 reporting slower deliveries, plus one-half of the proportion reporting no change in 480 delivery speed. 481

BCI-27 Manufacturers' new orders, nondefense capital goods (in 1996 \$). New 482 orders received by manufacturers in nondefense capital goods industries (in 483 inflation-adjusted dollars) are the producers' counterpart to BCI-06. 484

BCI-29 Building permits, new private housing units. The number of residential 485 building permits issued is an indicator of construction activity, which typically 486 leads most other types of economic production. 487

BCI-19 Stock prices, *500 common stocks*. The Standard & Poor's 500 stock index 488 reflects the price movements of a broad selection of common stocks traded on the 489 New York Stock Exchange. Increases (decreases) of the stock index can reflect both 490

491 the general sentiments of investors and the movements of interest rates, which is492 usually another good indicator for future economic activity.

493 *BCI-106 Money supply (in 1996 \$).* In inflation-adjusted dollars, this is the M2 494 version of the money supply. When the money supply does not keep pace with 495 inflation, bank lending may fall in real terms, making it more difficult for the 496 economy to expand. M2 includes currency, demand deposits, other checkable 497 deposits, travelers checks, savings deposits, small denomination time deposits, 498 and balances in money market mutual funds. The inflation adjustment is based on 499 the implicit deflator for personal consumption expenditures.

BCI-129 Interest rate spread, 10-year Treasury bonds less federal funds. The 500 501 spread or difference between long and short rates is often called the yield curve. This series is constructed using the 10-year Treasury bond rate and the federal funds 502 rate, an overnight interbank borrowing rate. It is felt to be an indicator of the stance 503 of monetary policy and general financial conditions because it rises (falls) when 504 505 short rates are relatively low (high). When it becomes negative (i.e., short rates are higher than long rates and the yield curve inverts) its record as an indicator of 506 recessions is particularly strong. 507

BCI-83 Index of consumer expectations. This index reflects changes in consumer 508 attitudes concerning future economic conditions and, therefore, is the only indicator 509 510 in the leading index that is completely expectations-based. Data are collected in a monthly survey conducted by the University of Michigan's Survey Research 511 Center. Responses to the questions concerning various economic conditions are 512 classified as positive, negative, or unchanged. The expectations series is derived 513 from the responses to three questions relating to (1) economic prospects for the 514 respondent's family over the next 12 months; (2) economic prospects for the Nation 515 over the next 12 months; and (3) economic prospects for the Nation over the next 516 5 years. 517

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Author Queries

Chapter No.: 2

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Chapter 3 An Introduction to Time Series Modeling and Forecasting

An important aspect of financial decision making may depend on the forecasting 4 effectiveness of the composite index of leading economic indicators, LEI. The 5 leading indicators can be used as an input to a transfer function model of real Gross 6 Domestic Product, GDP. The previous chapter employed four quarterly lags of the 7 LEI series to estimate regression models of association between current rates of 8 growth of real US GDP and the composite index of LEI. This chapter asks the 9 question as to whether changes in forecasted economic indexes help forecast 10 changes in real economic growth. The transfer function model forecasts are com- 11 pared to several naïve models in terms of testing which model produces the most 12 accurate forecast of real GDP. No-change (NoCH) forecasts of real GDP and 13 random walk with drift (RWD) models may be useful forecasting benchmarks 14 (Mincer and Zarnowitz 1969; Granger and Newbold 1977). Economists have 15 constructed LEI series to serve as a business barometer of the changing US 16 economy since the time of Mitchell (1913). The purpose of this study is to examine 17 the time series forecasts of composite economic indexes produced by The Confer- 18 ence Board (TCB), and test the hypothesis that the leading indicators are useful as 19 an input to a time series model to forecast real output in the United States. 20

Economic indicators are descriptive and anticipatory time series data used to 21 analyze and forecast changing business conditions. Cyclical indicators are compre-22 hensive series that are systemically related to the business cycle. Business cycles 23 are recurrent sequences of expansions and contractions in aggregate economic 24 activity. Coincident indicators have cyclical movements that approximately corre-25 spond with the overall business cycle expansions and contractions. Leading 26 indicators reach their turning points before the corresponding business cycle 27 turns. The lagging indicators reach their turning points after the corresponding 28 turns in the business cycle.

An example of business cycles can be found in the analysis of Irving Fisher 30 (1911), who discussed how changes in the money supply lead to rising prices and an 31 initial fall in the rate of interest, and how this results in raising profits, creating 32 a boom. The interest rate later rises, reducing profits, and ending the boom. 33 A financial crisis ensues when businessmen, whose loan collateral is falling as 34

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1 AU1

interest rates rise, run to cash and banks fail. The money supply is one series in TCB
 index of leading economic indexes, LEI.

AU2

Section "ARMA Model Identification in Practice" of this chapter presents an 37 introduction to the models that are estimated and tested in the analysis of the 38 forecasting effectiveness of the leading indicators. Section "Modeling Real GDP: 39 An Example" presents the empirical evidence to support the time series models and 40 reports how models adequately describe the data. Out-of-sample forecasting results 41 are shown in Section "Leading Economic Indicators (LEI) and Real GDP Analysis: 42 The Statistical Evidence, 1970–2002" for the United States and the G7 nations.¹ We 43 present additional evidence on out-of-sample forecasting for the Yen exchange, 44 consumption-income relationship, and Real GDP and LEI transfer function 45

46 modeling.

47 Basic Statistical Properties of Economic Series

This chapter develops and forecasts models of economic time series in which we 48 initially use only the past history of the series. The chapter later explores explana-49 tory variables in the forecast models. The time series modeling approach of Box and 50 Jenkins involves the identification, estimation, and forecasting of stationary (or 51 series transformed to stationarity) series through the analysis of the series autocor-52 relation and partial autocorrelation (PAC) functions.² The autocorrelation function 53 examines the correlations of the current value of the economic times series and its 54 previous k-lags. That is, one can measure the correlation of a daily series, of shares, 55

56 or other assets, by calculating

$$p_{jt} = a + bp_{jt-1},$$
 (3.1)

where $p_{jt} = \text{today's price of stock } j$; $p_{jt-1} = \text{yesterday's price of stock } j$; and b is the correlation coefficient.

In a daily shares price series, *b* is quite large, often approaching a value of 1.00.
As the number of lags or previous number of periods increases, the correlation tends
to fall. The decrease is usually very gradual.

The PAC function examines the correlation between p_{jt} and p_{jt-2} , holding constant the association between p_{jt} and p_{jt-1} . If a series follows a random walk, the correlation between p_{jt} and p_{jt-1} is one, and the correlation between p_{jt} and p_{jt-2} , holding constant the correlation of p_{jt} and p_{jt-1} , is zero. Random walk series are characterized with decaying autocorrelation functions and a PAC function with a "spike" at lag one, and zeros thereafter. Stationarity implies that the joint

¹ Section "ARMA Model Identification in Practice" can be omitted with little loss of continuity with readers more interested in the application of time series models.

² This section draws heavily from Box and Jenkins (1970, Chaps. 2 and 3).

probability [p(Z)] distribution $P(Z_{t1}, Z_{t2})$ is the same for all times t, t_1 , and t_2 where 68 the observations are separated by a constant time interval. The autocovariance of a 69 time series at some lag or interval, k, is defined to be the covariance between Z_t and 70 Z_{t+k} :

$$y_k = \operatorname{cov}[Z_t, Z_{t+k}] = E[(Z_t - \mu)(Z_{t+k} - \mu)].$$
(3.2)

One must standardize the autocovariance, as one standardizes the covariance in 72 traditional regression analysis, before one can quantify the statistically significant 73 association between Z_t and Z_{t+k} . The autocorrelation of a time series is the 74 standardization of the autocovariance of a time series relative to the variance of 75 the time series, and the autocorrelation at lag k, ρ_k , is bounded between +1 and -1: 76

$$\rho_{k} = \frac{E[(Z_{t} - \mu)(Z_{t+k} - \mu)]}{\sqrt{E[(Z_{t} - \mu)^{2}]E[(Z_{t+k} - \mu)^{2}]}}$$
$$= \frac{E[(Z_{t} - \mu)(Z_{t+k} - \mu)]}{\sigma_{Z}^{2}} = \frac{r_{k}}{r_{0}}.$$
(3.3)

The autocorrelation function of the process, $\{\rho_k\}$, represents the plotting of r_k 77 versus time, the lag of k. The autocorrelation function is symmetric about series and 78 thus $\rho_k = \rho_{-k}$; thus, time series analysis normally examines only the positive 79 segment of the autocorrelation function. One may also refer to the autocorrelation 80 function as the correlogram. The statistical estimates of the autocorrelation function 81 are calculated from a finite series of N observations, $Z_1, Z_2, Z_3, \ldots, Z_n$. The 82 statistical estimate of the autocorrelation function at lag k, r_k , is found by 83

$$r_k = \frac{C_k}{C_0}$$

84

$$C_k = \frac{1}{N} \sum_{t=1}^{N-k} (Z_t - \bar{Z})(Z_{t+k} - \bar{Z}), \quad k = 0, 1, 2, \dots, K.$$

 C_k is, of course, the statistical estimate of the autocovariance function at lag *k*. 85 In identifying and estimating parameters in a time series model, one seeks to 86 identify orders (lags) of the time series that are statistically different from zero. 87 The implication of testing whether an autocorrelation estimate is statistically 88 different from zero leads one back to the *t*-tests used in regression analysis to 89 examine the statistically significant association between variables. One must 90 develop a standard error of the autocorrelation estimate such that a formal *t*-test 91 can be performed to measure the statistical significance of the autocorrelation 92 estimate. Such a standard error, S_e , estimate was found by Bartlett and, in large 93 samples, is approximated by 94

where

3 An Introduction to Time Series Modeling and Forecasting

C

$$Var[r_k] \cong \frac{1}{N}$$
 and $S_e[r_k] \cong \frac{1}{\sqrt{N}}$. (3.4)

An autocorrelation estimate is considered statistically different from zero if it exceeds approximately twice its standard error.

A second statistical estimate useful in time series analysis is the PAC estimate of coefficient *j* at lag *k*, ϕ_{kj} . The PAC are found in the following manner:

$$\rho_j = \phi_{kl} p_{j-1} + \phi_{k2} p_{j-2} + \ldots + \phi_{k(k-1)} p_{jk-1} + \phi_{kk} p_{j-k}, \quad j = 1, 2, \ldots, k$$

99 or

$$\begin{bmatrix} 1 & \rho_1 & \rho_2 & \dots & \rho_{k-1} \\ \rho_1 & 1 & \rho_1 & \dots & \rho_{k-2} \\ \vdots & \vdots & \vdots & \dots & \vdots \\ \rho_{k-1} & \rho_{k-2} & \rho_{k-3} & \dots & 1 \end{bmatrix} \begin{bmatrix} \phi_{k-1} \\ \phi_{k2} \\ \vdots \\ \phi_{kk} \end{bmatrix} \begin{bmatrix} \rho_1 \\ \rho_2 \\ \vdots \\ \phi_{kk} \end{bmatrix}.$$

The PAC estimates may be found by solving the above equation systems for k = 1, 2, 3, ..., k:

$$\phi_{11} = \rho_1,$$

$$\phi_{22} = \frac{\rho_2 - \rho_1^2}{1 - \rho_1^2} = \frac{\begin{vmatrix} 1 & \rho_1 \\ \rho_2 & \rho_2 \end{vmatrix}}{\begin{vmatrix} 1 & \rho_1 \\ \rho_1 & 1 \end{vmatrix},$$

$$\phi_{33} = \frac{\begin{vmatrix} 1 & \rho_1 & \rho_1 \\ \rho_1 & 1 & \rho_2 \\ \rho_2 & \rho_1 & \rho_3 \end{vmatrix}}{\begin{vmatrix} 1 & \rho_1 & \rho_2 \\ \rho_1 & 1 & \rho_1 \\ \rho_2 & \rho_1 & 1 \end{vmatrix}.$$

The PAC function is estimated by expressing the current autocorrelation function estimates as a linear combination of previous orders of autocorrelation estimates:

$$\hat{r}_1 = \hat{\phi}_{k1^r j-1} + \hat{\phi}_{k2^2 j-2} + \ldots + \hat{\phi}_{k(k-1)^r j+k-1} + \hat{\phi}_{kk^2 j-k}, \quad j = 1, 2, \ldots, k.$$

105 The standard error of the PAC function is approximately

$$Var[\hat{\phi}_{kk}] \cong \frac{1}{N}$$
 and $S_e[\phi_{kk}] \cong \frac{1}{\sqrt{N}}$.

The Autoregressive and Moving Average Processes

A stochastic process, or time series, can be repeated as the output resulting from a 107 white noise input, α_t :³

$$\tilde{Z}_t = \alpha_t + \Psi_1 \alpha_{t-1} + \Psi_2 \alpha_{t-2} + \dots$$

= $\alpha_t + \sum_{j=1}^{\infty} \Psi_j a_{t-j}$ (3.5)

The filter weight, Ψ_j , transforms input into the output series. One normally 109 expresses the output, \tilde{Z}_t , as a deviation of the time series from its mean, μ , or origin 110

$$\tilde{Z}_t = Z_t - \mu.$$

The general linear process leads one to represent the output of a time series, \tilde{Z}_t , as 111 a function of the current and previous value of the white noise process, α_t , which 112 may be represented as a series of shocks. The white noise process, α_t , is a series of 113 random variables characterized by 114

$$E[\alpha_t] \cong 0$$

$$Var[\alpha_t] = \sigma_{\alpha}^2$$

$$\gamma_k = E[\alpha_t \alpha_{t+k}] = \sigma_{\alpha}^2 \quad k \neq 0$$

$$0 \quad k = 0$$

The autocorrelation function of a linear process may be given by

$$\gamma_k = \sigma_{\alpha}^2 \sum_{j=0}^{\infty} \Psi_j \Psi_{j+k}.$$

The backward shift operator, *B*, is defined as $BZ_t = Z_{t-1}$ and $B^j Z_t = Z_{t-j}$. 116 The autocorrelation generating function may be written as

$$\gamma(B) = \sum_{k=-\infty}^{\infty} \gamma_k B^k.$$

For stationarity, the ψ weights of a linear process must satisfy that $\psi(B)$ 118 converges on or lies within the unit circle. 119

³ Please see Box and Jenkins, *Time Series Analysis*, Chap. 3, for the most complete discussion of the ARMA (p,q) models.

In an autoregressive, AR, model, the current value of the time series may be expressed as a linear combination of the previous values of the series and a random shock, α_t :

$$\tilde{Z}_t = \phi_1 \tilde{Z}_{t-1} + \phi_2 \tilde{Z}_{t-2} + \ldots + \phi_p \tilde{Z}_{t-p} + \alpha_t.$$

123 The autoregressive operator of order P is given by

$$\phi(B) = 1 - \phi_1 B^1 - \phi_2 B^2 - \ldots - \phi_p B^p$$

124 or

$$\phi(B)\tilde{Z}_t = \alpha_t. \tag{3.6}$$

AU3

In an autoregressive model, the current value of the time series, \tilde{Z}_t , is a function of previous values of the time series, \tilde{Z}_{t-1} , \tilde{Z}_{t-2} , ..., and is similar to a multiple regression model. An autoregressive model of order *p* implies that only the first *p* order weights are nonzero. In many economic time series, the relevant autogressive order is one and the autoregressive process of order *p*, AR(*p*) is written as

130 or

$$(1 - \phi_1 B)\tilde{Z}_t = \alpha_t$$
 implying
 $\tilde{Z}_t = \phi^{-1}(B)\alpha_t.$

 $\tilde{Z}_t = \phi_1 \tilde{Z}_{t-1} + \alpha_t$

The relevant stationarity condition is |B| < 1 implying that $|\phi_1| < 1$. The autocorrelation function of a stationary autoregressive process

$$\tilde{Z}_t = \phi_1 \tilde{Z}_{t-1} + \phi_2 \tilde{Z}_{t-2} + \ldots + \phi_p \tilde{Z}_{t-p} + \alpha_t$$

133 may be expressed by the difference equation

$$P_k = \phi_1 \rho_{k-1} + \phi_2 \rho_{k-2} + \ldots + \phi_k \rho_{k-p}, \quad k > 0.$$

134 Or expressed in terms of the Yule-Walker equation as

$$\rho_1 = \phi_1 + \phi_2 \rho_1 + \ldots + \phi_p \rho_{p-1},$$

 $\rho_2 = \phi_1 \rho_1 + \phi_2 + \ldots + \phi_p \rho_{p-2},$

$$\bar{\bar{\rho}}_p = \phi_1 \rho_{p-1} + \phi_2 \rho_{p-2} + \ldots + \bar{\phi}_p.$$

For the first-order AR process, AR(1)

$$\rho_k = \phi_1 \rho_{k-1} = \bar{\bar{\phi}}_p.$$

 $P_1 = \phi_1$

The autocorrelation function decays exponentially to zero when ϕ_1 is positive 136 and oscillates in sign and decays exponentially to zero when ϕ_1 is negative: 137

and

 $\sigma_2 = \frac{\sigma_\alpha^2}{1 - \phi_1^2}.$

The PAC function cuts off after lag one in an AR(1) process. For a second-order 139 AR process, AR(2) 140

$$\tilde{Z}_t = \phi_1 \tilde{Z}_{t-1} + \phi_2 \tilde{Z}_{t-k} + \alpha_t$$
141

with roots

$$\phi(B) = 1 - \phi_1 B - \phi_2 B^2 = 0$$

and, for stationarity, roots lying outside the unit circle, ϕ_1 and ϕ_2 , must obey the 142 following conditions: 143

$$\phi_2 + \phi_1 < 1,$$

 $\phi_2 - \phi_1 < 1,$
 $- 1 < \phi_2 < 1.$

The autocorrelation function of an AR(2) model is

$$\rho_k = \phi_1 \rho_{k-1} + \phi_2 \rho_{k-2}. \tag{3.7}$$

The autocorrelation coefficients may be expressed in terms of the Yule-Walker 145 equations as 146

$$\rho_1 = \phi_1 + \phi_2 \rho_2,$$
$$\rho_2 = \phi_1 \rho_1 + \phi_2,$$

135

147 which implies

.

$$\begin{split} \varphi_1 &= \frac{\rho_1(1-\rho_2)}{1-\rho_1^2},\\ \varphi_2 &= \frac{\rho_2(1-\rho_1^2)}{1-\rho_1^2}, \end{split}$$

148 and

$$\rho_1 = \frac{\phi_1}{1 - \phi_2} \quad \text{and} \quad \rho_2 = \phi_2 + \frac{\phi_1^2}{1 - \phi_2}$$

149

150 For a stationary AR(2) process,

$$-1 < \phi_1 < 1,$$

-1 < \rho_2 < 1,
$$\rho_1^2 < \frac{1}{2}(\rho_2 + 1).$$

In an AR(2) process, the autocorrelation coefficients tail off after order two and the PAC function cuts off after the second order (lag).⁴

In a q-order moving average (MA) model, the current value of the series can be expressed as a linear combination of the current and previous shock variables:

$$\tilde{Z}_t = \alpha_1 - \theta_1 \alpha_{t-1} - \ldots - \alpha_q \theta_{t-q}$$

= $(1 - \theta_1 B_1 - \ldots - \theta_q B_q) \alpha_t$.
= $\theta(B) \alpha_t$

155 The autocovariance function of a q-order moving average model is

$$\gamma_k = E[(\alpha_t - \theta_1 \alpha_{t-1} - \ldots - \theta_q \alpha_{t-q})(\alpha_{t-k} - \theta_1 \alpha_{t-k-1} - \ldots - \theta_q \alpha_{t-k-q})].$$

⁴ A stationary AR(p) process can be expressed as an infinite weighted sum of the previous shock variables

$$\tilde{Z}_t = \phi^{-1}(B)\alpha_t.$$

In an invertible time series, the current shock variable may be expressed as an infinite weighted sum of the previous values of the series

$$\theta^{-1}(B)\tilde{Z}_t = \alpha_t.$$

The autocorrelation function, ρ_k , is

$$\rho_k = \frac{-\theta_k + \theta_1 \theta_{k+1} + \ldots + \theta_{q-k} \theta_q}{1 + \theta_1^2 + \ldots + \theta_q^2} \quad k = 1, 2, \dots, q$$
$$0 \qquad k > q$$

The autocorrelation function of an MA(q) model cuts off, to zero, after lag q and 157 its PAC function tails off to zero after lag q. There are no restrictions on the moving 158 average model parameters for stationarity; however, moving average parameters 159 must be invertible. Invertibility implies that the π weights of the linear filter 160 transforming the input into the output series, the π weights lie outside the unit circle: 161

$$\pi(B) = \Psi^{-1}(B) = \sum_{j=0}^a \phi^j B^j.$$

In a first-order moving average model, MA(1)

$$\tilde{Z}_t = (1 - \theta_1 B) \alpha_t$$

and the invertibility condition is $| heta_1| < 1$. The autocorrelation function of the MA $\,$ 163 (1) model is 164

$$\rho_k = \frac{-\theta_1}{1+\theta_1^2} \quad k = 1, \ k > 2.$$

The PAC function of an MA(1) process tails off after lag one and its autocorre-	165
lation function cuts off after lag one.	166
In a second-order moving average model, MA(2)	167

ag

$$\tilde{Z}_t = \alpha_t - \theta_1 \alpha_{t-1} - \theta_2 \alpha_{t-2}$$

the invertibility conditions require

 $\theta_2 < \theta_1 < 1$, $\theta_2 - \theta_1 < 1$, $-1 < \theta_2 < 1.$

The autocorrelation function of the MA(2) is

$$\rho_1 = \frac{-\theta_1(1-\theta_2)}{1+\theta_1^2+\theta_1^2},$$

55

162

168

$$\rho_2 = \frac{-\theta_2}{1+\theta_1^2+\theta_1^2},$$

170 and

$$\rho_k = \theta \quad for k > 3.$$

171 The PAC function of an MA(2) tails off after lag two.

In many economic time series, it is necessary to employ a mixed autoregressivemoving average (ARMA) model of the form

$$\tilde{Z}_t = \phi_1 \tilde{Z}_{t-1} + \ldots + \phi_p \tilde{Z}_{t-p} + \alpha_t - \theta_1 \alpha_{t-1} - \ldots - \theta_q \alpha_{t-q}$$
(3.8)

174 or

$$(1 - \phi_1 B - \phi_2 B^2 - \ldots - \theta_p B^p) \tilde{Z}_t = (1 - \theta_1 B - \theta_2 B^2 - \ldots - \theta_q B^q) \alpha_t$$

175 that may be more simply expressed as

$$\phi(B)\tilde{Z}_t=\theta(B)\alpha_t.$$

176 The autocorrelation function of the ARMA model is

$$\rho_k = \phi_1 \rho_{k-1} + \phi_2 \rho_{k-2} + \ldots + \phi_p \rho_{k-p}$$

177 or

$$\phi(B)\rho_k=0.$$

~

The first-order autoregressive–first-order moving average operator ARMA (1,1) process is written as

$$\ddot{Z}_t - \phi_1 \ddot{Z}_{t-1} = \alpha_t - \theta_1 \alpha_{t-1}$$

180 or

$$(1-\phi_1)\tilde{Z}_t = (1-\theta 1B)\alpha_t.$$

The stationary condition is $-1 < \phi_1 < 1$ and the invertibility condition is -182 $< \phi_1 < 1$. The first two autocorrelations of the ARMA (1,1) model are

$$\rho_1 = \frac{(1 - \phi_1 \theta_1)(\phi_1 - \theta_1)}{1 + \theta_1^2 - 2\phi_1 \theta_1}$$

and

$$\rho_2 = \phi_1 \rho_1.$$

The PAC function consists only of $\phi_{11} = \rho_1$ and has a damped exponential. 184 An integrated stochastic progress generates a time series if the series is made 185 stationary by differencing (applying a time-invariant filter) the data. In an 186 integrated process, the general form of the time series model is 187

$$\phi(B)(1-B)^d X_t = \theta(B)\varepsilon_t, \tag{3.9}$$

where $\phi(B)$ and $\theta(B)$ are the autoregressive and moving average polynominals in 188 *B* of orders *p* and *q*, ε_t is a white noise error term, and *d* is an integer representing the 189 order of the data differencing. In economic time series, a first-difference of the data 190 is normally performed.⁵ The application of the differencing operator, *d*, produces a 191 stationary ARMA(*p*,*q*) process. The autoregressive integrated moving average, 192 ARIMA, model is characterized by orders *p*, *d*, and *q* [ARIMA (*p*,*d*,*q*)]. Many 193 economics series follow an RWD, and an ARMA (1,1) may be written as 194

$$\bar{V}^d X_t = X_t - X_{t-1} = \varepsilon_t + b\varepsilon_{t-l}.$$

An examination of the autocorrelation function estimates may lead one to 195 investigate using a first-difference model when the autocorrelation function 196 estimates decay slowly. In an integrated process, the $corr(X_t, X_{t-\tau})$ is approximately 197 unity for small values of time, τ . 198

ARMA Model Identification in Practice

Time series specialists use many statistical tools to identify models; however, the 200 sample autocorrelation and PAC function estimates are particularly useful in 201 modeling. Univariate time series modeling normally requires larger data sets than 202 regression and exponential smoothing models. It has been suggested that at least 203 30-50 observations be used to obtain reliable estimates.⁶ One normally calculates 204 the sample autocorrelation and PAC estimates for the raw time series and its first 205 (and possibly second) differences. The failure of the autocorrelation function 206 estimates of the raw data series to die out as large lags implies that a first difference 207 is necessary. The autocorrelation function estimates of a MA(*q*) process should cut 208

183

⁵ Box and Jenkins, *Time Series Analysis*. Chapter 6; C.W.J. Granger and Paul Newbold, *Forecasting Economic Time Series*. Second Edition (New York: Academic Press, 1986), pp. 109–110, 115–117, 206.

⁶ Granger and Newbold, Forecasting Economic Time Series. pp. 185–186.

209 off after q. To test whether the autocorrelation estimates are statistically different 210 from zero, one uses a *t*-test where the standard error of $v\tau$ is⁷

$$n^{-1/2}[1+2(\rho_1^2+\rho_2^2+\ldots+\rho_q^2)]^{1/2}$$
 for $\tau > q$.

The PAC function estimates of an AR(p) process cut off after lag p. A *t*-test is used to statistically examine whether the PAC are statistically different from zero. The standard error of the PAC estimates is approximately

$$\frac{1}{\sqrt{N}}$$
 for $K > p$.

One can use the normality assumption of large samples in the *t*-tests of the autocorrelation and PAC estimates. The identified parameters are generally considered statistically significant if the parameters exceed twice the standard errors. The ARMA model parameters may be estimated using nonlinear least squares.

The ARMA model parameters may be estimated using nonlinear least squares. Given the following ARMA framework generally pack-forecasts the initial parameter estimates and assumes that the shock terms are to be normally distributed:

$$\alpha_t = \tilde{W}_t - \phi_1 \tilde{W}_{t-1} - \phi_2 \tilde{W}_{t-2} - \dots - \phi_p \tilde{W}_{t-p} + \theta_1 \alpha_{t-1} + \dots + \theta_q \alpha_{t-q},$$

220 where

$$W_t = \overline{V}^d Z_t$$
 and $\widetilde{W}_t = W_t - \mu$.

The minimization of the sum of squared errors with respect to the autoregressive and moving average parameter estimates produces starting values for the p order AR estimates and q order MA estimates:

$$\frac{\partial e_t}{-\partial \phi_j}\Big|_{\beta_0} = \mu_{j,t} \text{ and } \frac{\partial e_t}{-\partial \theta_i}\Big|_{\beta_0} = X_{j,t}.$$

It may be appropriate to transform a series of data such that the residuals of a fitted model have a constant variance, or are normally distributed. The log transformation is such a data transformation that is often used in modeling economic time series. Box and Cox (1964) put forth a series of power transformations useful in modeling time series.⁸ The data is transformed by choosing a value of λ that is

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⁷ Box and Jenkins, *Time Series Analysis*. pp. 173–179.

⁸G.E. Box and D.R. Cox, "An Analysis of Transformations," *Journal of the Royal Statistical Society*, B 26 (1964), 211–243.
suggested by the relationship between the series amplitude (which may be 229 approximated by the range of subsets) and mean:⁹ 230

$$X_t^{\lambda} = \frac{X_t^{\lambda} - 1}{\bar{X}^{\lambda - 1}},\tag{3.10}$$

where X is the geometric mean of the series. One immediately recognizes that if 231 $\lambda = 0$, the series is a logarithmic transformation. The log transformation is appro-232 priate when there is a positive relationship between the amplitude and mean of the 233 series. A $\lambda = 1$ implies that the raw data should be analyzed and there is no 234 relationship between the series range and mean subsets. One generally selects the 235 λ that minimizes the smallest residual sum of squares, although an unusual value of 236 λ may make the model difficult to interpret. Some authors may suggest that only 237 values of λ of -0.5, 0, 0.5, and 1.0 be considered to ease in the model building 238 process.¹⁰

Many time series, involving quarterly or monthly data, may be characterized by 240 rather large seasonal components. The ARIMA model may be supplemented with 241 seasonal autoregressive and moving average terms: 242

$$(1 - \phi_1 B - \phi_2 B^2 - \dots - \phi_p B^p)(1 - \phi_{1,s} B^s - \dots - \phi_{p,s} B^p S^s)(1 - B)^d$$

$$(1 - B^s)^{ds} X_t$$

$$= (1 - \theta_1 B - \dots - \theta_q B^q)(1 - \theta_{1,s} B^s - \dots - \theta_{q,s} B^{q,s}) \alpha_t \text{ or } \theta_p(B) \Phi_p(B^s) \quad (3.11)$$

$$\bar{V}^d \bar{V}_x^D Z_t$$

$$= \theta_q(B) \theta_Q(B^s) \alpha_t.$$

One recognizes seasonal components by an examination of the autocorrelation 243 and PAC function estimates. That is, the autocorrelation and PAC function 244 estimates should have significantly large values at lags 1 and 12 as well as smaller 245 (but statistically significant) values at lag 13 for monthly data.¹¹ One seasonally 246 differences the data (a 12th-order seasonal difference for monthly data and 247 estimates the seasonal AR or MA parameters). An RWD model with a monthly 248 component may be written as 249

$$\bar{V}\bar{V}_{12}Z_t = (1-B)(1-\theta B^{12})\alpha_t.$$
(3.12)

The multiplicative form of the $(0,1,1) \times (0,1,1)$ model has a moving average 250 operator that may be written as 251

⁹ G.M. Jenkins, "Practical Experience with Modeling and Forecasting Time Series," *Forecasting* (Amsterdam: North-Holland Publishing Company, 1979).

¹⁰ Jenkins, op. cit., pp. 135–138.

¹¹ Box and Jenkins, *Time Series Analysis*, pp. 305–308.

3 An Introduction to Time Series Modeling and Forecasting

$$(1 - \theta B)(1 - \theta B^{12}) = 1 - \theta B - \theta B^{12} + \theta B^{13}.$$

The RWD with the monthly seasonal adjustments is the basis of the "airline model" in honor of the analysis by Professors Box and Jenkins of total airline passengers during the 1949–1960 period.¹² The airline passenger data analysis employed the natural logarithmic transformation.

There are several tests and procedures that are available for checking the adequacy of fitted time series models. The most widely used test is the Box–Pierce test, where one examines the autocorrelation among residuals, α_t :

$$\hat{v}_k = \frac{t = \sum_{k=1}^n \alpha_t \alpha_{t-k}}{\sum_{t=1}^n \alpha_t^2}, \quad k = 1, 2, \dots$$

The test statistic, Q, should be X^2 distributed with (m-p-q) degrees of freedom:

$$Q = n \sum_{k=1}^{m} \hat{v}_k^2.$$

The Ljung–Box statistic is a variation on the Box–Pierce statistic and the Ljung–Box Q statistic tends to produce significance levels closer to the asymptotic levels than the Box–Pierce statistic for first-order moving average processes. The Ljung–Box statistic, the model adequacy check reported in the SAS system, can be written as

$$Q = n(n+2) \sum_{k=1}^{m} (n=k)^{-1} \hat{v}_k^2.$$
(3.13)

Residual plots are generally useful in examining model adequacy; such plots may identify outliers as we noted in the chapter. The normalized cumulative periodogram of residuals should be examined.

Granger and Newbold (1977) and McCracken (2002) use several criteria to 268 evaluate the effectiveness of the forecasts with respect to the forecast errors. 269 In this chapter, we use the root mean square error (RMSE) criteria. One seeks to 270 minimize the square root of the sum of the absolute value of the forecast errors 271 squared. That is, we calculate the absolute value of the forecast error, square the 272 error, sum the squared errors, divided by the number of forecast periods, and 273 take the square root of the resulting calculation. Intuitively, one seeks to minimize 274 275 the forecast errors. The absolute value of the forecast errors is important because if

¹² Box and Jenkins, op. cit.

one calculated only a mean error, a 5% positive error could "cancel out" a 5% 276 negative error. Thus, we minimize the out-of-sample forecast errors. We need a 277 benchmark for forecast error evaluation. An accepted benchmark (Mincer and 278 Zarnowitz 1969) for forecast evaluation is a NoCH. A forecasting model should 279 produce a lower RMSE than the NoCH model. If several models are tested, the 280 lowest RMSE model is preferred. 281

In the world of business and statistics, one often speaks of autoregressive, 282 moving average, and RWD models, or processes, as we have just introduced. 283

It is well known that the majority of economic series, including real Gross 284 National Product (GDP) in the United States, follow an RWD, and are represented 285 AU5 with ARIMA model with a first-order moving average operator applied to the first-286 difference of the data. The data is differenced to produce stationary, where a 287 process has a (finite) mean and variance that do not change over time and the 288 covariance between data points of two series depends upon the distance between the 289 data points, not on the time itself. The RWD process, estimated with an ARIMA 290 (0,1,1) model, is approximately equal to a first-order exponential smoothing model 291 (Cogger 1974). The RWD model has been supported by the work of Nelson and 292 Plosser (1982). 293

In a transfer function model, one models the dynamic relationship between the 294 deviations of input X and output Y. One is concerned with estimating the delay 295 between the input and output. The set of weights is often referred to as the impulse 296 response function: 297

$$Y_t = V_0 \tilde{X}_t + V_1 \tilde{X}_{t-1} + V_2 \tilde{X}_{t-2}.$$
(3.14)

$$V(B)\tilde{X}_t.$$
(3.15)

Modeling Real GDP: An Example

GDP is the market value of all goods and services produced within a country in a 299 given period. The expenditure approach holds that GDP is the sum of personal 300 consumption, gross investment, government spending, and net exports (exports less 301 imports). Let us go to a source of real-business economic and financial data. The St. 302 Louis Federal Reserve Bank has an economic database, denoted FRED, containing 303 some 41,000 economic series, available at no cost, via the Internet, at http:// 304 research.stlouisfed.org/fred2. 305

If one downloaded and graphed quarterly real (in 2005 dollars) GDP data from 306 1947 to 2011Q1 (April 1, 2011), one sees in Chart 1 that the postwar period has 307 been one of great, fairly consistent growth. 308



The recession of 2007–2008 is pronounced and notable, the most obvious contraction of the postwar period.

Let us examine the autocorrelation (AC) and PAC functions of the quarterly data. The raw data AC and PAC function estimates, estimated in EViews, are shown in Table 3.1, and indicate the need to (first) difference the data. One can apply the Box–Jenkins time series methodology to the real GDP data and estimate several basic models. We can take the difference of the logarithm of the series to produce stationarity and estimate a first-order autoregressive parameter to approximate the data (Table 3.2).

We estimate an RWD model, an ARIMA (0,1,1), in Table 3.3 for the US real GDP, 1947–2011Q1. The drift term, a first-order moving average term with a 0.289 coefficient, is statistically significant, having a *t*-statistic of 4.89. The overall *F*statistic of 31.12 indicates that the model is adequate fit. The RWD model is an adequate representation of the real GDP data generating process. One can, and should, fit other ARIMA models.¹³

The author fits an ARIMA (1,1,0) model as an additional ARIMA benchmark at the suggestion of Professor Victor Zarnowitz.¹⁴ The ARIMA (1,1,0) has a higher *F*-statistics than the ARIMA (1,1,0) and a higher *t*-statistic on the first-order autoregressive parameter, 6.50. The author used the ARIMA (1,1,0) benchmark is AU6

¹³ The EViews software, EViews4, in this chapter is an extremely easy system to use. The author first worked with Box–Jenkins time series model using the Nelson (1973) and Jenkins (1979) monographs and the ARIMA programs of David Pack (1982).

¹⁴ Victor Zarnowitz was formerly emeritus of the University of Chicago, Senior Economist at TCB, and a long-term fellow Associate Editor of the author at *The International Journal of Forecasting*.

Table	3.1	Autocorrelation	and	partial	autocorrelation	function	estimates	of	Real	GDP,	t1.1
1947-2	20110	Q1									

Autocorrelation	Partial correlation		AC	PAC	Q-Stat	Prob	t1.2
	. ******	1	0.990	0.990	256.60	0.000	t1.3
*****		2	0.979	-0.013	508.73	0.000	t1.4
*****		3	0.968	-0.013	756.34	0.000	t1.5
*****		4	0.958	-0.012	999.38	0.000	t1.6
*****		5	0.947	-0.005	1237.9	0.000	t1.7
******		6	0.936	-0.002	1471.9	0.000	t1.8
******		7	0.925	-0.001	1701.6	0.000	t1.9
*****		8	0.915	-0.001	1926.9	0.000	t1.10
*****		9	0.904	-0.003	2148.0	0.000	t1.11
*****		10	0.894	-0.010	2364.8	0.000	t1.12
******		11	0.883	-0.015	2577.3	0.000	t1.13
*****		12	0.871	-0.036	2785.1	0.000	t1.14
*****		13	0.859	-0.037	2988.0	0.000	t1.15
*****		14	0.847	-0.021	3186.0	0.000	t1.16
*****		15	0.835	-0.004	3379.0	0.000	t1.17
*****		16	0.822	-0.017	3567.0	0.000	t1.18
*****		17	0.810	-0.008	3750.1	0.000	t1.19
*****		18	0.797	-0.004	3928.2	0.000	t1.20
*****		19	0.785	-0.001	4101.6	0.000	t1.21
*****		20	0.772	-0.014	4270.2	0.000	t1.22
*****		21	0.760	-0.006	4434.1	0.000	t1.23
*****		22	0.747	-0.014	4593.2	0.000	t1.24
*****		23	0.734	-0.008	4747.6	0.000	t1.25
*****		24	0.722	0.007	4897.5	0.000	t1.26
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a study of the effectiveness of TCB LEI (Guerard 2001). Both ARIMA models are 328 [AU7] adequately fit (Table 3.4). 329

If one chose not to difference the real GDP data and fit a first-order 330 autoregressive model, one finds an AR(1) parameter near 1, see Table 3.5. 331

The initial view of the adjusted R-square and F-statistic might lead the reader to 332 believe that the AR(1) model was almost "truth." One must model changes in 333 financial economic data. 334

Leading Economic Indicators and Real GDP Analysis: 335 The Statistical Evidence, 1970–2002 336

We introduce the time series modeling process in this study because we will use 337 TCB US composite LEI as an input to a transfer function model of US real GDP, 338 both series being first-differenced and log-transformed. The authors test the null 339 hypothesis that there is no statistical association between changes in the logged LEI 340

t2.2	Autocorrelation	Partial correlation	Lag	AC	PAC	Q-Stat	Prob
t2.3	. ****	. ****	1	0.474	0.474	58.536	0.000
t2.4	. ***	. *	2	0.346	0.157	89.953	0.000
t2.5	. *	* .	3	0.151	-0.082	95.941	0.000
t2.6	. *	. .	4	0.106	0.023	98.922	0.000
t2.7	. .	* .	5	-0.016	-0.089	98.987	0.000
t2.8	6	0.022	0.056	99.111	0.000
t2.9	7	0.006	0.017	99.122	0.000
t2.10	8	-0.008	-0.039	99.141	0.000
t2.11	. *	. *	9	0.126	0.192	103.44	0.000
t2.12	. *	. .	10	0.104	-0.011	106.39	0.000
t2.13	. .	* .	11	0.044	-0.09	106.92	0.000
t2.14	* .	* .	12	-0.059	-0.1	107.88	0.000
t2.15	13	-0.005	0.062	107.88	0.000
t2.16	. .	. *	14	-0.001	0.07	107.88	0.000
t2.17	15	-0.005	-0.038	107.89	0.000
t2.18	. *	. *	16	0.075	0.103	109.43	0.000
t2.19	. .	-i.	17	0.038	-0.033	109.82	0.000
t2.20	18	0.058	0.001	110.76	0.000
t2.21	. *	. *	19	0.096	0.071	113.34	0.000
t2.22	. *	. . 1	20	0.092	-0.013	115.73	0.000
t2.23		. .	21	0.024	0.005	115.89	0.000
t2.24		. .	22	0.053	0.051	116.7	0.000
t2.25		. .	23	0.06	0.013	117.74	0.000
t2.26	. *	. *	24	0.126	0.12	122.29	0.000

t2.1 **Table 3.2** Autocorrelation and partial autocorrelation function estimates of differenced Real GDP, 1947–2011Q1

and changes in logged real GDP in the United States. A positive and statistically
significant coefficient indicates that the leading indicator composite series is
associated with rising real output, and leads to the rejection of the null hypothesis.
Zarnowitz (1992) examined the determinants of Real GDP, 1953–1982, using
VAR models. In this analysis, we test the statistical significance of TCB LEI by
adding the lags of the variable to an AR(1) model. Does the knowledge of the LEI

Table 3.3	An ARIMA RWD	estimate of Real	Gross Domestic Prod	uct, 1947–2011Q1
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Table 3.3 An ARIMA	RWD estimate of R	eal Gross Domest	ic Product, 1947-2	011Q1
Dependent variable: DL	OG(RGDP)			
Method: Least squares				
Date: 02/12/12, Time: 0	7:34			
Sample(adjusted): 2 259)			
Included observations: 2	258 after adjusting en	ndpoints		
Convergence achieved a	after 12 iterations			
Backcast: 1				
Variable	Coefficient	Std. error	t-Statistic	Prob.
С	0.007817	0.000756	10.33377	0.0000
MA(1)	0.289085	0.059828	4.831927	0.0000
R-Squared	0.108390	Mean depend	lent var	0.007825
Adjusted R-squared	0.104907	S.D. depende	nt var	0.009970
S.E. of regression	0.009432	Akaike info c	criterion	-6.481599
Sum squared resid	0.022777	Schwarz crite	erion	-6.454057
Log likelihood	838.1263	F-Statistic		31.12102
Durbin-Watson stat	1.866243	Prob (F-statis	stic)	0.000000

Table 3.4 An ARIMA	estimate of Real Gro	oss Domestic Prod	uct, 1947–2011Q1	
Dependent variable: DL	OG(RGDP)		T	
Method: Least squares				
Date: 01/23/12, Time: 1	4:52			
Sample(adjusted): 3 259)			
Included observations: 2	257 after adjusting er	adpoints		
Convergence achieved a	after 3 iterations			
Variable	Coefficient	Std. error	t-Statistic	Prob.
С	0.007875	0.000926	8.506078	0.0000
AR(1)	0.376487	0.057913	6.500889	0.0000
R-Squared	0.142170	Mean depend	ent var	0.007861
Adjusted R-squared	0.138806	S.D. depende	nt var	0.009972
S.E. of regression	0.009254	Akaike info c	riterion	-6.519720
Sum squared resid	0.021838	Schwarz crite	erion	-6.492100
Log likelihood	839.7840	F-statistic		42.26155
Durbin-Watson stat	2.067711	Prob (F-statis	tic)	0.000000

help forecast future changes in GDP, and can past values of the GDP data predict 347 the future growth of GDP? In a recent study of univariate and time series model 348 post-sample forecasting, Thomakos and Guerard (2001) compared RWD and 349 transfer-function models with NoCH forecasts using rolling one-period-ahead 350 post-sample periods. Guerard (2001) found that the AR(1) and RWD processes 351 are adequate representations of the time series process of real GDP, given the lags 352 of the autocorrelation and PAC functions. Guerard (2001) reported the estimated 353 cross-correlation functions between the G7 respective LEI and real GDP for the 354

5.1 Table 3.5 An AR(1) estimate of Real Gross Domestic Product, 1947–2	2011	Q	1
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t5.2	Dependent variable: R	GDP				
t5.3	Method: Least squares					
t5.4	Date: 01/23/12, Time:	08:40				
t5.5	Sample(adjusted): 200	259				
t5.6	Included observations:	60 after adjusting endp	oints			
t5.7	Convergence achieved	after 5 iterations				
t5.8	Variable	Coefficient	Std. error	t-Statistic	Prob.	
t5.9	С	14,253.05	885.7279	16.09191	0.0000	
t5.10	AR(1)	0.972952	0.009076	107.1982	0.0000	
t5.11	R-Squared	0.994978	Mean depender	nt var	11,944.42	
t5.12	Adjusted R-squared	0.994892	S.D. dependent	var	1137.426	
t5.13	S.E. of regression	81.29588	Akaike info cri	terion	11.66683	
t5.14	4 Sum squared resid 383,323.1 Schwarz criterion 11.73664					
t5.15	Log likelihood	-348.0050	F-Statistic		11,491.46	
t5.16	Durbin-Watson stat	1.033644	Prob (F-statisti	c)	0.000000	

355 1970–2000 period, and found that the resulting transfer function models were 356 statistically significant in forecasting real GDP in the G7 nations.

357 In this chapter, the authors report the estimated autocorrelation and PAC functions of the US real GDP, 1963-March 2002, shown in Table 3.1. EViews is 358 used in the analysis. Let us look at Table 3.6, the estimated autocorrelation PAC 359 functions of real quarterly US GDP, March 1963-March 2002. The estimated 360 autocorrelation function decays gradually, falling from 0.979 for a one period 361 (quarter lag), 0.958 for a two quarter lag, to 0.584 for a 20 quarter lag, and 0.318 362 for a 36 quarter lag. The estimated PAC function is characterized by the "spike" at a 363 one quarter lag. The first estimated partial autocorrelation is 0.979, and the second 364 partial autocorrelation is -0.005. The US real GDP series can be estimated as an 365 RWD series for the 1963–2002 period. The estimated functions substantiate the 366 estimation of the first-order moving average operator of the first-differenced, log-367 368 transformed US real GDP series, denoted RWD, shown in Table 3.7. Guerard (2001) used an autoregressive variation of the RWD model as a forecasting 369 benchmark. The residuals of the RWD model show few deviations from normality. 370 The RWD is a statistically adequately fitted model. We estimate the cross-371 correlation function of the LEI and real GDP for an initial 32 guarter estimation 372 period, following Thomakos and Guerard (2004), and use the 1978-March 2002 373 374 period for initial US post-sample evaluation. Similar estimations are derived for real GDP series in France (FR), Germany (GY), and the UK (see Table 3.8). 375 The LEI are statistically significantly associated with real GDP in the respective 376 countries during the 1978-2002 period, as are shown in the respective GDP 377 regressions in Table 3.8. The lag structures of the models were discussed in Guerard 378 (2001), and we refer the reader to the initial modeling and forecasting analysis. 379 The statistical significance of the transfer functions in Table 3.3 leads one to reject 380

AU8

Table 3.6 Correlogram of USGDP

Date: 05/09/03 Time: 14:28 Sample: 1 158 Included observations: 157 Autocorrelation AC PAC Q-Stat Partial Correlation Prob 0.979 0.979 153.31 0.000 ۱ 1 2 0.958 -0.005 301.09 I 0.000 ۱ 3 0.937 -0.010 443.41 0.000 I 1 0.916 -0.024 580.18 0.000 1 I 4 ł I. I 5 0.894 -0.024 711.33 0.000 ł I ı 0.871 -0.022 836.82 0.000 6 ł ۱ 0.849 -0.015 956.70 0.000 7 ŧ ł 8 0.826 -0.021 1071.0 0.000 0.804 0.003 Ł ۱ ı 9 1179.9 0.000 1 ۱ 10 0.781 -0.011 1283.6 0.000 I t 1 1 11 0.760 0.008 1382.4 0.000 ł ł 12 0.739 0.004 1476.5 0.000 I 1 ı 13 0.719 -0.005 1566.1 0.000 I 1 ۱ 14 0.699 -0.011 1651.3 0.000 I ł ۲ 1 15 0.679 0.002 1732.4 0.000 t 16 0.660 -0.004 1809.4 0.000 ۱ 1 0.640 -0.012 1882.4 0.000 1 I 17 1 ı 18 0.621 -0.003 1951.7 0.000 1 1 ı ı 19 0.602 -0.011 2017.4 0.000 2079.4 0.000 ł ŧ 20 0.584 -0.006 21 0.566 0.004 2138.2 0.000 1 t 1 22 0.548 -0.001 2193.7 0.000 1 ı 1 23 0.531 -0.004 2246.2 0.000 1 I F 1 24 0.514 -0.013 2295.7 0.000 I 25 0.497 0.005 1 ł 2342.4 0.000 1 28 0.480 -0.010 2386.4 0.000 1 27 0.464 -0.007 2427.7 0.000 ı 28 0.448 -0.013 2466.5 0.000 ı I 29 0.431 -0.018 2502.7 0.000 I 30 0.414 -0.016 2536.4 0.000 I 31 0.397 -0.001 2567.7 0.000 32 0.381 -0.020 2596.6 0.000 ł 33 0.365 0.008 t 2623.3 0.000 1 34 0.349 -0.008 2648.0 0.000 35 0.333 0.001 2670.7 0.000 1 ı 36 0.318 -0.013 2691.5 0.000

t6.2

t6.1

Variable	Coefficient	Std. error	t-Statistic	Prob.
С	0.008	0.0001	8.149	0.000
MA(1)	0.218	0.087	2.507	0.013
R-Squared	0.061			
Adjusted R-squared	0.053			
S.E. of regression	0.0086	Akaike info ci	riterion	-6.6575
Sum squared resid	0.0093	Schwarz criter	rion	-6.6129
Log likelihood	428.08	F-statistic		8.1570
Durbin-Watson stat	1.92	Prob(F-statisti	c)	0.0050

t7.1 Table 3.7 Random walk with drift time series model of Real US GDP

t8.1 Table 3.8 Post-sample regression coefficients of the leading economic indicators, 1978–March 2002

			LEI	IEI	IEI	IEI		Adjusted	
t8.2	Country	Const.	(-1)	(-2)	(-3)	(-4)	AR(1)	R-squared	F-Statistic
t8.3 t8.4	USA (t)	0.005 7.200	0.337 4.800	0.060 0.890	0.141 2.130		0.053 0.480	0.283	10.400
t8.5 t8.6	UK	0.005 7.500			0.214 2.610		-0.166 -2.300	0.088	5.600
t8.7 t8.8	Germany	0.004 5.750	0.242 2.610		0.211 2.370	XC	$-0.250 \\ -2.300$	0.102	4.610
t8.9 t8.10	France	0.004 7.960		0.140 1.930	0.133 1.870	-0.064 -0.910	0.038 0.360	0.058	2.470
t8.11 t8.12	Japan	0.005 5.860	0.217 2.900		0		$-0.437 \\ -4.660$	0.174	11.030
t8.13 t8.14	Canada	0.008 4.880		0.306 2.340	0.036 0.270	$-0.263 \\ -2.100$	0.150 0.640	0.240	3.290
t8.15 t8.16	Italy	0.004 4.670		0.132 2.260	-0.089 -1.480	$-0.009 \\ -1.490$	$-0.050 \\ -0.240$	0.059	1.460

the null hypothesis of no statistical association changes in the LEI and changes in 381 real GDP. The statistically significant lags in the cross-correlation functions show 382 how past values of the LEI series are associated with the current values of the 383 respective real GDP. That is, the LEI series lead their respective real GDP series 384 385 and can be used as inputs to transfer function models of real GDP. The multiple regressions of the post-sample period are generally statistically significant at the 1% 386 level, as shown by their respective F-statistics of the regressions. The exception to 387 this result is the French real GDP estimate, see Table 3.8, that is significant at 388 approximately the 5% level. Thus, the estimation of the transfer function is statisti-389 cally significant relative to simply using an AR(1) time series model. 390

US and G7 Post-sample Real GDP Forecasting Analysis

In this section, the author estimates several time series models for the US leading 392 indicators and Real GDP, and corresponding models for the G7 nations. A simple 393 autoregressive variation on the random walk model, an ARIMA (1,1,0), is 394 estimated to serve as a naïve, forecasting model. The ARIMA model is referred 395 to as the RWD Model. The transfer function model uses the LEI series as the input 396 to the Real GDP (output) series. We will evaluate the forecasting performances of 397 the models with respect to their RMSE, defined as the square root of the sum of the 398 individual observation forecast errors squared. The most accurate forecast will have 399 the smallest forecast error squared and hence the smallest RMSE. The RMSE 400 criteria are proportional to the average squared error criteria used in Granger and 401 Newbold (1977). One can estimate models using 32 quarters of data and forecast 402 one-step-ahead. We compare the forecasting accuracy of four models of the US real 403 GDP. The models tested are (1) the transfer function model in which TCB compos- 404 ite index of ILEI is lagged three quarters, denoted TF; (2) a NoCH forecast; (3) the 405 simple RWD model; and (4) a simple transfer function model in which TCB 406 composite index of LEI is lagged one period, denoted TF1. One finds that the 407 three-quarter of lagged LEI transfer function is the most accurate out-of-sample 408 forecasting model for the US real GDP, although there is no statistically significant 409 differences in the rolling one-period-ahead root mean square forecasting errors of 410 the RWD, TF, and TF1 models. 411

The one-period-ahead quarterly RMSE for the 1978–March 2002 period of Real 412 GDP are shown in Table 3.9.

413 AU9

Thus, the US leading indicators lead Real GDP, as one should expect, and the 414 transfer function model produces lower forecast errors than the univariate model, 415 and a naive benchmark, the NoCH model. The reader notes that the transfer 416 function model uses a one-quarter lag that produces forecasts that are not statistically different from the three-quarter lags suggested from the estimated cross- 418 correlation function.

The model forecast errors are not statistically different (the *t*-value of the paired 420 differences of the univariate and TF models is 0.91). An analysis of the rolling one-421 period-ahead RMSE produces somewhat different results for post-sample modeling 422 than the use of one long period of post-sample period. The multiple regression 423 models indicate statistical significance in the US composite index of LEI for the 424 1978–March 2002 period. One does not find that the transfer function model 425 forecast errors are (statistically) significantly lower than univariate ARIMA 426 model (RWD) errors in a rolling one-period-ahead analysis. The authors prefer to 427 measure forecasting performance in the rolling period manner (as we often live in a 428 one-period-ahead forecasting regime).

The RMSE of the G7 nations cast doubt as to the effectiveness of the LEI as a 430 statistically significant input in transfer function models forecasting real GDP. 431 Transfer function model forecasts of real GDP, using TCB do not significantly 432

3 An Introduction to Time Series Modeling and Forecasting

t9.1	Table 3.9 Post-sample accuracy of the US Pacel CDP	Model	RMSE
t9.2	models using The Conference	No-change	0.0117
t9.3	Board LEI in the transfer	RWD	0.0086
t9.4	function model	TF1	0.0080
t9.5		TF	0.0079

t10.1 Table 3.10 Post-sample	Nation	Model	Input source	RMSE
t10.2 using TCB LEIs in the	GR	NoCH		0.0114
t10.3 transfer function model		RWD		0.0109
t10.4		TF	ТСВ	0.0106
t10.5	FR	NoCH		0.0081
t10.6		RWD		0.0065
t10.7		TF	ТСВ	0.0070
t10.8	JP	NoCH		0.0177
t10.9		RWD		0.0152
t10.10		TF	TCB	0.0163
t10.11	UK	NoCH	*	0.0106
t10.12		RWD		0.0090
t10.13		TF	TCB	0.0089

t11.1 Table 3.11 Post-sample	e root Estimation modeling period	s RMSE
t11.2 GDP 1982 2002	$\frac{1}{32}$	5.31
t11.3	36	5.18
t11.4	40	5.19
t11.5	44	4.99
t11.6	48	4.99
t11.7	52	5.03
t11.8	56	5.05
t11.9	60	5.08
t11.10	NoCh	8.09

reduce RMSE relative to the RWD model forecasts during the 1978–March 2002period. Please see Table 3.10.

One may ask why 32 observations were used. Why not use 60 observations of past real GDP to estimate the models? If one sought to minimize the forecasting error from 1982 to June 2002, and one varied the estimation modeling periods, one finds that the 32-quarter estimation is quite reasonable, see Table 3.11. The 40- and 439 44-quarter estimation periods produce the lowest real RMSE, although the 440 differences are not statistically significant.

Summary

441

This chapter examined the predictive information in TCB LEI for the United States, 442 the UK, Japan, and France. We find that TCB LEI and FIBER short-term LEI are 443 statistically significant in modeling the respective real GDP changes during the 444 1970–2000 period. One rejects the null hypothesis of no association between 445 changes in LEI and changes in real GDP in the United States, and the G7 nations. 446 If one uses a rolling 32-quarter estimation period and a one-period-ahead 447 forecasting RMSE calculation, the LEI forecasting errors are not significantly 448 lower than the univariate ARIMA model forecasts. In Chap. 6, we estimate addi-449 tional time series models and introduce the reader to causality testing. 450

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AU2	The acronym "LEI" is used for both "leading economic indicators" and "leading economic indexes"; please check whether any changes should be made.	
AU3	Please check whether the term "auto- gressive" is an acceptable one in the context.	
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Chapter 4 Regression Analysis and Multicollinearity: Two Case Studies

In this chapter, we explore two applications of regression modeling: the question of 4 regression-weighting of GNP forecasts and the issue of estimating models 5 associated with security totals returns. We examine the forecasting of GNP by 6 major econometric firms and the modeling of security returns as a function of well- 7 known investment variables and strategies. We illustrate regression analysis and 8 problems with highly correlated independent variables. We will refer to the corre- 9 lation among independent variables as multicollinearity. 10

The first case study involves combining econometric services' forecasts of GNP. 11 In combining economic forecasts a problem often faced is that the individual 12 forecasts display some degree of dependence. We discuss latent root regression 13 (LRR) for combining collinear GNP forecasts. Guerard and Clemen (1989) results 14 indicate that LRR produces more efficient combining weight estimates (regression 15 parameter estimates) than ordinary least squares estimation (OLS), although out-ofsample forecasting performance is comparable to OLS. Researchers appear to 17 have reached agreement, or consensus, regarding the value of combining forecasts. 18 Performance, measured in terms of a variety of error summary statistics, can be 19 improved by combining multiple forecasts. There is an extensive literature on 20 combining forecasts that can be traced back to Bates and Granger (1969), reached a 21 peak with Winkler and Makridakis (1983), Clemen and Winkler (1986), and Granger (1989), and was documented in a bibliography by Clemen (1989). An important 23 unanswered question, however, regards what combination procedure to use. 24

There are many ways of determining these weights, and the aim was to choose a 25 method which was likely to yield low errors for the combined forecasts. Bates and 26 Granger, denoted as BG in many Granger references, (1969) assumed that 27 the performance of the individual forecasts would be consistent over time in the 28 sense that the variance of errors for the two forecasts could be denoted by σ_1^2 and 29 σ_2^2 for all values of time, *t*. It was further assumed that both forecasts would be 30 unbiased (either naturally or after a correction had been applied). The combined 31 forecasts would be a linear combination of the two sets of forecasts, 32

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bined forecast, σ_c^2 , can then be written:

$$\sigma_c^2 = k^2 \sigma_1^2 + (1-k)^2 \sigma_2^2 + 2\rho k \ \sigma_1 (1-k) \sigma_2, \tag{4.1}$$

where *k* is the proportionate weight given to the first set of forecasts and ρ is the correlation coefficient between the errors in the first set of forecasts and those in the second set. The choice of *k* should be made so that errors of the combined forecasts are small: more specifically, we chose to minimize the overall variance, σ_c^2 . Differentiating with respect to *k*, and equating to zero, we get the minimum of σ_c^2 , occurring when

$$k = \frac{\sigma_2^2 - \rho \sigma_1 \sigma_2}{\sigma_1^2 - \sigma_2^2 - 2\rho \sigma_1 \sigma_2}.$$
 (4.2)

42 In the case where $\rho = 0$, this reduces to

$$k = \sigma_2^2 / \left(\sigma_1^2 + \sigma_2^2 \right).$$
(4.3)

It can be shown that if k is determined by (4.1), the value of σ_c^2 is no greater than the smaller of the two *individual* variances.¹

The optimum value for k is not known at the commencement of combining forecasts. The value given to the weight k would change as evidence was accumulated about the relative performance of the two original forecasts. Thus the combined forecast for time period T, C_T , is more correctly written as

$$C_T = k_T f_{1,T} + (1 - k_T) f_{2,T}, \qquad (4.4)$$

49 where $f_{1,T}$ is the forecast at time *T* from the first set and $f_{2,T}$ is the forecast at time *T* 50 from the second set.

Thought should be given to the possibility that the performance of one of the forecasts might be changing over time (perhaps improving) and that a method based on an estimate of the error variance since the beginning of the forecast might not therefore be appropriate.

55 Granger (1989) defined good forecasting methods (defined by us as those which 56 yield low mean-square forecast error) are likely to possess properties such as:

(a) The average weight k should approach the optimum value, defined by (2), as the number of forecasts increased—provided that the performance of the forecasts

59 is stationary.

¹ The reader will see a variation of (4.1) and (4.2) in Chap. 5 when we discuss optimal security weights in a portfolio. The Bates and Granger optimal forecast weighting is a variation of the optimal Markowitz (1959) two-asset security calculation.

62

- (b) The weights should adapt quickly to new values if there is a lasting change in 60 the success of one of the forecasts. 61
- (c) The weights should vary marginally from the optimum value.

This last point is included since property (a) is not sufficient on its own.² 63 In addition to these properties, there has been an attempt to restrict methods to 64 those which are moderately simple, in order that they can be of use to businessmen. 65

Model building can be tested in combining forecasts. If we had available all the 66 information, the so-called perfect foresight answer, upon which all the forecasts 67 are based, then we would build the complete model. There would be no need for 68 out-of-sample or post-sample forecasting periods. In most cases, only the individual 69 forecasts are available, rather than the information they are based on, and so 70 combining is appropriate. In the BG combinations these data were not used 71 efficiently. For example, if $f_{n,1}$, $g_{n,1}$ are a pair of one-step forecasts of y_{n+1} , made 72 at time *n*, and if the y_t series as stationary, then the unconditional mean 73

$$m_n = \frac{1}{n} \sum_{j=1}^n y_{t-j}$$
(4.5)

is also a forecast of y_{n+1} available at time *n*, although usually a very inefficient one. 74 This new forecast can be included in the combination, giving 75

$$c_{n+1} = \alpha_1 m_n + \alpha_2 f_{n,1} + \alpha_3 g_{n,1}$$
(4.6)

as the combined forecast. The weights α_j can be obtained by regressing $c_{n,1}$ on y_{n+1} 76 as discussed in Granger and Ramanathan (1984). Whether the weights α_j should add 77 to one depends on whether the forecasts are unbiased and the combination is 78 required to be unbiased. Before combining, it is usually a good idea to unbias the 79 component forecasts. Thus, if $w_{w,1}$ is a set of one-step forecasts, run a regression 80

$$y_{n+1} = a + bw_{n,1} + \varepsilon_{n+1}$$
 (4.7)

and check whether a = 0, b = 1, and if ε_n is white noise. If any of these conditions 81 do not hold, an immediately apparently superior forecast can be achieved and these 82 should be used in any combination. 83

In all these extensions of the original combining technique, combinations have 84 been linear, only single-step horizons are considered, and the data available 85 have been assumed to be just the various forecasts and the past data of the series 86 being forecast. On this last point, it is clear that other data can be introduced to 87 produce further forecasts to add to the combinations, or Bayesian techniques could 88

² Granger (1989) additionally pointed out that if the optimum value for *k* is 0.3, one may still obtain poor combined forecast if *k* takes two values only, being 0 on 60% of occasions and 1.0 on the remaining 40%.

be used to help determine the weights. The fact that only linear combinations were
being used was viewed as an unnecessary restriction from the earliest days, but
sensible ways to remove this estimation were unclear.

Procedures suggested by Bates and Granger (1969), with subsequent extensions 92 and applications by Newbold and Granger (1974) and Winkler (1981) among 93 others, model the forecast errors with a multinormal process, the parameters of 94 which determine the combining weights. A number of alternative combining 95 procedures have also been proposed, including simple averages (Makridakis and 96 Winkler 1983), unrestricted regressions (Granger and Ramanathan 1984), 97 98 weighting procedures based on assessments of which forecast might perform best (Bunn 1975; Clemen and Guerard 1989), and various ad hoc procedures (Ashton 99 100 and Ashton 1985). The basic question is whether equally weighted composite forecasting models outperform statistically based forecast models. 101

In developing composite models using the multinormal model or related regres-102 sion approaches one major problem is that the covariance matrix must typically be 103 estimated with relatively small quantities of data. This results in unstable estimation 104 of the covariance matrix and even more unstable estimation of the combining 105 weights (Kang 1986). Furthermore, for economic forecasting the problem is 106 exacerbated by the fact that different forecaster errors are typically highly 107 correlated; correlations above 0.8 are not at all unusual (Clemen and Winkler 108 1986; Figlewski and Urich 1983). 109

We explore the possibility of using LRR (Webster et al. 1974; Gunst et al. 1976) 110 as a procedure for combining dependent forecasts. This approach provides an 111 explicit framework for analysis of collinear data through the mathematics of latent 112 roots and vectors. The data we analyze (GNP forecasts studied in Clemen and 113 Winkler 1986) display pairwise correlations of forecast errors between 0.82114 115 and 0.96. Given these relatively high correlations as well as Kang's demonstration of the instability of the estimated weights in this data set, it seems reasonable to 116 think that LRR might improve on the performance of OLS. 117

118 We assume that at time t - 1 we have access to k forecasts, $f_t = (f_{1t}, \dots, f_{kt})$, 119 for θ_t . We can write θ_t stochastically in terms of the (possibly biased) forecasts f_{it} :

$$\theta_t = a_i + b_i f_{it} + u_{it}, \tag{4.8}$$

120 where each $u_t = (u_{lt}, ..., u_{kt})'$ is an independent realization from a normal process 121 with mean vector (0, ..., 0)' and covariance matrix \sum . At time t - 1, we have 122 available past observations (forecasts and actual values) for time t = 1, ..., t - 1. 123 To represent these data we will adopt the following notation:

$$[\theta, F] = \begin{pmatrix} \theta_1 & 1 & f_{1,1} & \dots & f_{k,1} \\ & \ddots & & & \ddots \\ \theta_{t-1} & 1 & f_{1,t-1} & \dots & f_{k,t-1} \end{pmatrix}.$$
(4.9)

We include the vector of ones because, in general, we will be estimating regression coefficients including a constant term. Multiply each of the different equations (4.9) by a factor γ_i such that $\sum \gamma i = 1$. 126 Then combine equation (4.1) to obtain the following regression representation: 127

$$\theta_{t} = \sum \gamma_{i} a_{i} + \sum \gamma_{i} b_{i} f_{it} + \sum \gamma_{i} \mu_{it}$$

= $\beta_{0} + \beta_{1} f_{1t} + \ldots + \beta_{k} f_{kt} + \varepsilon_{t}$
= $f_{t}^{*} \beta + \varepsilon_{t},$ (4.10)

where

$$\beta = (\beta_0, \dots, \beta_k)' = \left(\sum \gamma_i a_i, \gamma_1 b_1, \dots, \gamma_k b_k\right)'$$
$$f_t^* \beta = (1, f_{1t}, \dots, f_{kt})$$

and

$$\varepsilon_t = \sum \gamma_i \mu_{it}.$$

The distributional assumptions regarding μ_t imply that the regression equation 130 error terms ε_t obey standard OLS assumptions. Therefore, the OLS estimator of β is 131 given by the familiar expression 132

$$B^* = (F'F)^{-1}F'\theta.$$
(4.11)

As usual, β^* is the best linear unbiased estimator of β , and, assuming stationarity 133 of the process through time, the forecast $\theta_t^* = f_t^* \beta^*$ is the best linear unbiased 134 predictor of θ_t .

In the event of multicollinearity in the F matrix, β^* (and hence θ_t^*) can be 136 inefficient. If the process is stationary, one solution to the problem of multicollinear 137 regressors is simply to acquire more data to improve the efficiency of the estima-138 tion, thereby improving prediction performance. However, this is often not possi-139 ble, especially when working with economic data. Thus, there is some motivation to 140 consider biased estimation and prediction if the biased approach might yield a 141 substantial improvement in terms of estimation efficiency. LRR is one such tech-142 nique. The following is a brief description of the procedure, abstracted from 143 Webster et al. (1974) and Gunst et al. (1976). We direct the interested reader to 144 those papers for more details.

LRR seeks to identify near-singularities in the explanatory variables and to 146 determine their predictive value. The procedure uses this information to estimate 147 the regression parameters β by adjusting for non-predictive near-singularities. 148 Define the matrix A to be $n \times (k + 1)$ data matrix containing standardized- 149 dependent and -independent variables. The correlation matrix (A' A) has latent 150 roots λ_i and corresponding latent vectors α_i defined by 151

$$|A'A - \lambda_i I| = 0$$

152 and

$$(A'A - \lambda_i I)\alpha_i = 0.$$

153 Denote the elements of α_i by

$$\alpha'_i = (\alpha_{0i}, \alpha_{1i}, \ldots, \alpha_{ki})$$

154 and

$$\alpha_i^{0'} = (\alpha_{1i}, \ldots, \alpha_{ki}).$$

155 That is, α_i^0 contains all of the elements of α_i except tile first one. Also, define

$$\eta^2 = \Sigma (\theta_i - \theta)^2.$$

156 The OLS estimator β^* can be written as

$$\beta^* = -\eta \Sigma c_i \alpha_i^{\ 0},$$

157 where

$$c_{i} = \alpha_{0i} \lambda_{i}^{-1} \left(\Sigma \alpha_{0}^{2} / \lambda_{j} \right)^{-1}.$$
(4.12)

Values of λ_i and α_{0i} close to zero indicate a non-predictive near-singularity. 159 As α_{0i} becomes close to zero, c_i should also be close to zero. However, since λ_i is 160 also small, c_i may be quite large, and may have a dominant effect in the estimate β^* . 161 Gunst et al. (1976) suggest setting $c_i = 0$ for $|\lambda_i| \le 0.3$ and $|\alpha_{0i}| \le 0.1$, thus 162 obtaining the LRR estimate of the parameter β . Webster et al. (1974) and Gunst 163 et al. (1976) provide detailed geometrical interpretations and discussion of this 164 technique.

165 The First Example: Combining GNP Forecasts

166 Clemen and Winkler (1986) studied the forecasting efficiency of Gross National

167 Product (GN) forecasting services in the mid-1980s, using data from the fourth 168 quarterly of 1970 to the fourth quarter of 1983. Wharton Econometrics (Wharton),

168 quarterly of 1970 to the fourth quarter of 1983. Wharton Econometrics (Wharton), 169 Chase Econometrics (Chase), Data Resources, Inc. (DRI), and the Bureau of

Economic Analysis (BEA) made quarterly forecasts of many economic variables. 170 Clemen and Winkler (1986) used level forecasts of nominal GNP (1970–1983), 171 obtained directly from Wharton and BEA and from the *Statistical Bulletin* 172 published by the Conference Board for Chase and DRI to construct growth rate 173 forecasts (in percentage terms), and calculated the deviations from actual growth as 174 determined from GNP reported in *Business Conditions Digest*. Forecasts with four 175 different horizons (one, two, three, and four quarters) were analyzed. For example, 176 the four-quarter GNP forecast predicts the percentage change for the 3-month 177 AU1 period four quarters in the future (counting the current one). Finally, the data are 178 divided into two periods, one for estimation and one for forecast evaluation. 179 The estimation period runs through 1979 for each horizon, with the remaining 180 data kept in reserve as an independent sample for forecast evaluation. For analysis 181 of the individual forecasts, the reader is referred to Clemen and Winkler (1986) and 182 Clemen (1986). 183

Clemen and Guerard (1989) tested LRR as a combining technique because of the 184 high pairwise correlations among the individual forecasts and the instability of 185 the estimated weights, noted by Kang (1986). However, while these observations 186 suggest multicollinearity, we have no clear indication of the severity of the problem. 187 Belsley et al. (1980) and Belsley (1982, 1984) have discussed diagnostics for explicit 188 AU2 measurement of the severity of multicollinearity. We calculated variance inflation 189 factors, condition indexes, and variance-decomposition proportions for each of the 190 four forecast horizons. These diagnostics are reported in Table 4.1. For condition 191 numbers (defined as the largest of the condition indexes), the value 30 is suggested as 192 a screen; situations with larger values are then examined more closely. All our 193 condition numbers are between 20 and 30; thus, on the basis of this diagnostic alone 194 our data do not appear to display severe multicollinearity. For variance inflation 195 factors (VIFs), Montgomery and Peck (1982) suggest that values from 5 to 10 196 indicate severe multicollinearity. Our VIFs range up to 4.6. Variance-decomposition 197 proportions can also be used to detect multicollinearity, which is indicated by two 198 numbers exceeding 0.5 in any one row of the variance-decomposition table. For our 199 forecasts, the variance-decomposition calculations reveal collinearity between (1) 200 the DRI and BEA forecasts in the one- and two-quarter horizons, (2) the Wharton 201 and BEA forecasts in the three-quarter one, and (3) the Chase and DRI as well as the 202 constant and BEA variables in the four-quarter horizon.³ 203

To some extent, the use of these diagnostics is problematic. For instance, 204 condition indexes are based on eigenvalues (latent roots) of the sample covariance 205 matrix, and it is unclear to what extent models built and estimated on the basis of 206 this diagnostic might be sensitive for relatively small sample sizes. The presence 207

³ This research was supported in part by the National Science Foundation under Grant IST 8600788. We thank George Jaszi of the BEA and Donald Straszheim of Wharton, who graciously provided the forecasts from their respective econometric models. The authors are indebted to Professors S. Sharma and W.L. James for providing access to their LRR procedure as described in Sharma and James (1981).

t1.2			Variance-decomposition proportions						
t1.3	Horizon	Condition indexes	Constant	Wharton	Chase	DRI	BEA		
t1.4	1	9.78	0.68	0.00	0.03	0.02	0.07		
t1.5		15.80	0.04	0.01	0.00	0.56	0.63		
t1.6		17.65	0.01	0.03	0.73	0.30	0.30		
t1.7		20.93	0.27	0.96	0.24	0.11	0.00		
t1.8		VIF		3.38	3.86	3.25	3.24		
t1.9	2	11.06	0.55	0.25	0.14	0.00	0.01		
t1.10		12.58	0.17	0.60	0.13	0.01	0.13		
t1.11		14.06	0.16	0.11	0.62	0.01	0.23		
t1.12		27.41	0.11	0.04	0.11	0.98	0.63		
t1.13		VIF		1.85	2.25	4.60	3.23		
t1.14	3	10.94	0.71	0.00	0.26	0.01	0.00		
t1.15		13.69	0.23	0.42	0.44	0.01	0.01		
t1.16		18.98	0.06	0.50	0.27	0.09	0.53		
t1.17		22.24	0.00	0.08	0.03	0.88	0.46		
t1.18		VIF		2.54	2.40	3.93	3.27		
t1.19	4	7.36	0.05	0.84	0.01	0.00	0.00		
t1.20		11.14	0.29	0.06	0.29	0.09	0.01		
t1.21		16.39	0.01	0.03	0.62	0.84	0.00		
t1.22		22.86	0.65	0.06	0.07	0.07	0.98		
t1.23		VIF		1.52	2.31	2.54	2.22		

t1.1 Table 4.1 Multicollinearity diagnostics for GNP forecasts

of a condition index greater than 30 may be a reliable indicator of multicollinearity; 208 however, values slightly less than 30 do not necessarily mean that effects due to 209 multicollinearity will be unnoticeable. With regard to the variance-decomposition 210 proportions, the Guerard and Clemen (1989) results indicated that the one-quarter 211 DRI and BEA forecasts appear to be associated with an ill-conditioned covariance 212 matrix. That is, the correlation coefficient between the one-quarter DRI and BEA 213 (0.82, reported in Clemen and Winkler 1986) is the least of the pairwise correlations 214 for this horizon. Likewise, the correlation between Wharton and BEA errors in the 215 two-quarter analysis (0.94) is the second-lowest of the reported pairwise 216 correlations. Given these observations, it seems reasonable to conclude that 217 multicollinearity, perhaps at a relatively low level, was present in the Guerard 218 and Clemen (1989) data. 219

Application of LRR, using the Gunst et al. (1976) criteria for vector deletion, produced the results shown in Table 4.2. Details regarding the latent roots and vectors and the vector deletion patterns for each analysis are available from the authors. The coefficient estimates for the Chase and DRI forecasts are highly significant in the one-quarter horizon. In the two-quarter horizon, coefficient estimates for DRI and BEA are significant, as is the DRI coefficient estimate in the three-quarter horizon.

Table 4.2 LRR and OLS regression results

Horizon		Constant	Wharton	Chase	DRI	BEA	R^2
1	LRR	1.30	-0.23 (-0.58)	0.96 (2.83) ^a	0.37 (4.93)a	-0.11 (-1.78)	0.40
	OLS	2.18	-0.53 (-1.28)	0.65 (1.66)	0.33 (0.92)	0.48 (1.43)	0.46
2	LRR	1.71	0.08 (0.24)	-0.25 (-0.69)	$(2.52)^{a}$	0.63 (2.31) ^a	0.24
	OLS	1.48	0.06 (0.20)	-0.28 (-0.76)	0.59 (0.87)	0.52 (1.10)	0.24
3	LRR	4.17	0.16 (0.39)	-0.62 (-1.60)	$(2.56)^{a}$	0.76 (1.56)	0.18
	OLS	4.17	0.21 (0.46)	-0.59 (-1.53)	0.20 (0.34)	0.82 (1.47)	0.18
4	LRR	8.69	-0.09 (-0.40)	-0.60 (-1.69)	0.96 (2.03)	-0.08 (-0.36)	0.12
	OLS	10.92	-0.06 (-0.28)	-0.47 (-1.10)	1.10 (2.39) ^a	-0.63 (-0.96)	0.17

values in parentileses are *i*-statist

^aSignificance at the 0.05 level

 Table 4.3 Performance of combining methods for the post-estimation evaluation period shown
 t3.1

Horizon	Evaluation period	Equal weights	OLS	LRR	t3.2
1	80.1-82.2	2.47	2.89	2.76	t3.3
2	80.1-82.3	3.60	4.19	4.40	t3.4
3	80.1-82.4	4.35	4.58	4.49	t3.5
4	80.1-83.1	4.45	3.67	3.71	t3.6

Performance is mean absolute relative error, where absolute relative error is defined as l(actualforecast)/actuall

For comparison, OLS results are also included in Table 4.2. Generally speaking, 227 LRR and OLS produced coefficient estimates that are comparable in terms of signs 228 and relative sizes. (While this comparison is a matter of degree, two exceptions are 229 BEA in the one- and four-quarter horizons). On the other hand, LRR generally 230 yielded more efficient estimates of the parameters than OLS, as measured by the 231 *t*-statistics. 232

The true test of a forecasting procedure is how well it performs outside of the 233 fitting data. Table 4.3 presents the results obtained by using the estimated models to 234 predict actual nominal GNP for the evaluation periods shown. Guerard and Clemen 235 (1989) included the arithmetic average (equal weights) as one of the combining 236 procedures for use as a benchmark. The performance measure we used, mean 237 absolute relative error, is mean absolute percentage error (MAPE) divided by 238 100. MAPE is a widely used forecast performance measure that allows performance 239 comparisons among different forecast situations (see Armstrong 1985). The results 240

t2 1

in Table 4.3 show that OLS and LLR performed comparably. Given the similar
estimates of the combining weights in the two analyses, this result is not surprising.
The equal weights combination outperformed the regression model in all but the
four-quarter horizon.

The Guerard and Clemen (1989) empirical results show that LRR produced more 245 efficient parameter estimates than OLS. However, the similar out-of-sample perfor-246 mance of the two methods leads us to be somewhat ambivalent. In theory, LRR's 247 more efficient estimation of parameters should result in more efficient predictors and 248 hence better out-of-sample prediction performance. In light of the data's high 249 correlations, Kang's results, and Clemen's and Winkler's (1986) results from 250 combining these GNP forecasts using a Bayesian model, Guerard and Clemen 251 252 (1989) concluded that the comparable performance of LRR and OLS is troubling. 253 Compared to OLS, Clemen's and Winkler's Bayesian model resulted in forecasting performance improvements of about 16% in terms of mean squared error. One 254 possible interpretation might be that Clemen's and Winkler's model, being mathe-255 256 matically similar to ridge regression (Lindley and Smith 1972; Hocking 1976), tended to counteract the dependence among the forecasts. Of course, other 257 258 techniques are available for use with collinear data, notably principal components regression (Gunst et al. 1976) and LRR. The Guerard and Clemen (1989) motivation 259 for trying LRR was that it differs fundamentally from ridge regression (and the 260 related Clemen/Winkler model) in the way multicollinearity is handled. Where ridge 261 regression depends on the estimation of a biasing parameter, principal components 262 regression and LRR are estimated by the elimination of non-predictive near-263 singularities as described above. However, the Guerard and Clemen (1989) GNP 264 forecasts appeared to be collinear enough to cause some difficulty in the OLS 265 analysis, but not severe enough for LRR to dominate OLS. 266

267 The Second Example: Modeling the Returns of the US Equities

Our second example will address the estimations of the determinants of the US equity 268 security monthly returns. In 1990, Harry Markowitz became the Head of the Global 269 Portfolio Research Department (GPRD) at Daiwa Securities Trust. His department 270 used fundamental data to create models for Japanese and the US securities and the 271 researchers tested single variable and regression-weighted composite model 272 strategies for Japan and the USA over 1974–1990. The GPRD analysis builds upon 273 Guerard and Takano (1991) and Guerard (1990) framework. We refer the reader to 274 275 those studies and the work of Savita Subramanian at Bank of America Merrill Lynch for testing these variables, and many other strategies in the US equity market. The 276 quantitative work of Subramanian is some of the best "sell side" research, in the 277 opinion of the author.⁴ In this section, we review and revisit the GPRD regression 278

⁴ Savita Subramanian (2011), "US Quantitative Primer," Bank of America Merrill Lynch, May.

analysis.⁵ Guerard and Takano used book value, cash flow, and sales, relative to price, 279 AU3 in their analysis. The major papers on combination of value ratios to predict stock 280 returns that include at least CP and/or SP include Chan et al. (1991), Bloch et al. 281 (1993), Lakonishok et al. (1994), and Haugen and Baker (2010). In fact, the Bloch 282 AU4 et al. (1993) was a more technical version of Guerard and Takano (1991). 283

The composite models could be created by combining variables using OLS, 284 outlier-adjusted or robust regression (ROB), or weighted latent root regression 285 (WLRR) modeling, in which outliers and the high correlations among the variables 286 are used in the estimation procedure. The reader is referred to Bloch et al. (1993) for 287 a discussion of ROB and WLRR techniques.⁶ The Markowitz group found that the 288 AU5 use of the more advanced statistical techniques produced higher relative out-of- 289 sample portfolio geometric returns and Sharpe ratios. Statistical modeling is not just 290 fun, but it is also consistent with maximizing portfolio returns. The quarterly 291 estimated models outperformed the semiannual estimated models, although the 292 underlying data was semiannual in Japan. The dependent variable in the composite 293 model is total security quarterly returns and the independent variables are the EPR, 294 BPR, CPR, and SPR variables. The ultimate test of OLS, ROB, and WLRR 295 analyses can be found in the Bloch et al. (1993) simulations which reported higher 296 Geometric Means, Sharpe Ratios, and F-Statistics using WLRR than OLS in 297 estimating models of the determinants of monthly security returns. The Bloch 298 et al. research (1993) has been reestimated, updated, and enhanced in Guerard 299 (2006), Stone and Guerard (2010), and Guerard et al. (2012). 300 AU6

Let us discuss two enhancements in the Guerard et al. (2012) study: the addition of 301 price momentum and earnings per share (eps) forecasts, revisions, and breadth 302 variables. Earnings forecasting enhances returns relative to using only reported 303 financial data and valuation ratios. In 1975, a database of eps forecasts was created 304

⁵ There are many approaches to security valuation and the creation of expected returns. The first approaches to security analysis and stock selection involved the use of valuation techniques using reported earnings and other financial data. Graham and Dodd (1934) recommended that stocks be purchased on the basis of the price-earnings (P/E) ratio and Basu (1977) reported evidence supporting the low P/E model. James (Jim) Miller, Chief Investment Officer, CIO, of Continental Bank commissioned the project with Drexel, Burnham, Lambert, in 1989. Miller and Guerard (1991) presented a stock selection model at The Berkeley Program in Finance that used earnings, book value, cash flow, sales, relative variables, and earnings per share forecast revisions. Miller and Guerard experimented with a price momentum variable, the Columbine Alpha, described in Brush (2001). Jack Brush's Columbine Alpha "pushed out" the eight-factor EP, BP, CP, SP, and relative variables' Efficient Frontier. Guerard delivered paper sat Columbine Equity Research conferences in 1989 and 1994. See Guerard (1990).

⁶ Guerard (2006) reestimated the GPRD model using PACAP data at The Wharton School from Wharton Research Data Services (WRDS). The WRDS/PACAP data is as close to the GPRD data as was possible in academia. The average cross-sectional quarterly WLRR model *F*-statistic in the GPRD analysis was 16 during the 1974–1990 period whereas the corresponding *F*-statistic reported in the Guerard (2006) was 11 for the post-publication, 1993–2001 period. Both sets of models were highly statistically significant and could be effectively used as stock selection models.

305 by Lynch, Jones, and Ryan, a New York brokerage firm, by collecting and publishing the consensus statistics of 1-year-ahead and 2-year-ahead eps forecasts [Brown 306 (1999)]. The database evolved to become known as the Institutional Brokerage 307 Estimation Service (I/B/E/S) database. There is an extensive literature regarding 308 the effectiveness of analysts' earnings forecasts, earnings revisions, earnings forecast 309 variability, and breadth of earnings forecast revisions, summarized in Bruce and 310 AU7 Epstein (1994), Brown (1999), and Ramnath et al. (2008). The vast majority of the 311 AU8 earnings forecasting literature in the Bruce and Brown references find that the use of 312 earnings forecasts does not increase stockholder wealth, as specifically tested in Elton 313 314 et al. (1981) in their consensus forecasted growth variable, FGR. Reported earnings follow a random walk with drift process, and analysts are rarely more accurate than a 315 316 no-change model in forecasting eps [Cragg and Malkiel (1968)]. Analysts become AU9 more accurate as time passes during the year, and quarterly data are reported. Analyst 317 revisions are statistically correlated with stockholder returns during the year 318 [Hawkins et al. (1984) and Arnott (1985)]. Wheeler (1994) developed and tested a AU10 319 320 strategy in which analyst forecast revision breadth, defined as the number of upward forecast revisions subtracted by the number of downward forecast revisions, divided 321 322 by the total number of estimates, was the criteria for stock selection. Wheeler found AU11 statistically significant excess returns from the breadth strategy. A composite earn-323 ings variable, CTEF, is calculated using equally weighted revisions, RV; forecasted 324 earnings yields, FEP; and breadth, BR, of FY1 and FY2 forecasts, a variable put forth 325 in Guerard (1997) and further tested in Guerard et al. (1997). Adding I/B/E/S 326 variables in the form of CTEF added to the eight value ratios in Guerard and Takano 327 (1991) produced more than 2.5% of additional annualized return [Guerard et al. 328 (1997)]. The finding of significant predictive performance value for I/B/E/S variables AU12 329 indicates that analyst forecast information has value beyond purely statistical extrap-330 331 olation of past value and growth measures. Guerard (2006) reported the growing importance of earnings forecasts, revisions, and breadth in Japan and the USA, 332 particularly with respect to smaller capitalized securities. 333 Momentum investing was studied by academics at about the same time that 334 AU13 earnings forecasting studies were being published. Levy (1967), Arnott (1979), and 335 AU14

Brush and Boles (1983) found statistically significant power in relative strength. 336 337 The Brush and Boles analysis was particularly valuable because it found that the short-term (3-month) financial predictability of a naïve monthly price momentum 338 model, taking the price at time t - 1 divided by the price 12 months ago, t - 12, 339 was as statistically significant at identifying underpriced securities as using the 340 alpha of the market model adjusted for the security beta. Brush and Boles found that 341 beta adjustments slightly enhanced the predictive power in the 6–12-month periods. 342 343 Brush (2001) is an excellent 20-year summary of the price momentum literature. Fama and French (1992, 1995) used a price momentum variable using the price 344 2 months ago divided by the price 12 months ago, thus avoiding the well-known 345 return or residual reversal effect. The Brush et al. (2004) and Fama studies find 346 significant stock price anomalies, even with Korajcyk and Sadka using transactions 347 costs. The vast majority find that the use of 3-, 6-, and 12-month price momentum 348

AU15

AU16

variables, often defined as intermediate-term variables, is statistically significantly 349 associated with excess returns. 350

Guerard et al. (2012) added a Brush-based price momentum: taking the price at 351 time t - 1 divided by the price 12 months ago, t - 12, denoted PM, and the 352 consensus analysts' earnings forecasts and analysts' revisions composite variable, 353 CTEF, to the stock selection model, one can estimate an expanded stock selection 354 model to use as an input to an optimization analysis. The stock selection model 355 estimated in this chapter, denoted as the United States Expected Returns, USER, is 356

$$TR_{t+1} = a_0 + a_1 EP_t + a_2 BP_t + a_3 CP_t + a_4 SP_t + a_5 REP_t + a_6 RBP_t + a_7 RCP_t + a_8 RSP_t + a_9 CTEF_t + a_{10} PM_t + e_t,$$
(4.13)

where:

	557
EP = [earnings per share]/[price per share] = earnings-price ratio;	358
BP = [book value per share]/[price per share] = book-price ratio;	359
CP = [cash flow per share]/[price per share] = cash flow-price ratio;	360
SP = [net sales per share]/[price per share] = sales-price ratio;	361
REP = [current EP ratio]/[average EP ratio over the past 5 years];	362
RBP = [current BP ratio]/[average BP ratio over the past 5 years];	363
RCP = [current CP ratio]/[average CP ratio over the past 5 years];	364
RSP = [current SP ratio]/[average SP ratio over the past 5 years];	365
CTEF = consensus earnings-per-share I/B/E/S forecast, revisions, and breadth;	366
PM = Price Momentum; and	367
e = randomly distributed error term.	368

The USER model is estimated using WLRR analysis in (4.13) to identify variables 369 statistically significant at the 10% level; uses the normalized coefficients as weights; 370 and averages the variable weights over the past 12 months. The 12-month smoothing 371 is consistent with the four-quarter smoothing in Guerard and Takano (1991) and 372 AU17 Bloch et al. (1993). 373

While EP and BP variables are significant in explaining returns, the majority of 374 the forecast performance is attributable to other model variables, namely, the 375 relative earnings-to-price, relative cash-to-price, relative sales-to-price, price 376 momentum variable, and earnings forecast variable. The consensus earnings 377 forecasting variable, CTEF, and the price momentum variable, PM, dominate the 378 composite model, as is suggested by the fact that the variables account for 45% of 379 the model average weights. 380

Earnings forecasts, revisions, and directions of revisions are key variables in stock 381 selection modeling. The asset selection of the CTEF variable is highly significant, see 382 Guerard (2012). The average our-quarter smoothed regression coefficients are: 383 AU18 Time-average value of estimated coefficients: 384

a_1	a_2	<i>a</i> ₃	a_4	a_5	<i>a</i> ₆	<i>a</i> ₇	a_8	<i>a</i> 9	<i>a</i> ₁₀	385
0.044	0.038	0.020	0.038	0.089	0.086	0.187	0.122	0.219	0.224	386

t4.1 Table 4.4 OLS NREG0801 the REG procedure model: MODEL1-dependent variable: RET0801

t4.2	Number of observations read				3,656			
t4.3	Number of observed	vation	is used		3,482			
t4.4	Number of obser	rvation	s with missing v	alues	174			
t4.5	Analysis of varia	ance						
t4.6	Source		DF	Sum of squar	es	Mean square	F value	$\Pr > F$
t4.7	Model		10	256.20661		25.62066	28.53	< 0.0001
t4.8	Error		3,471	3,117.52880		0.89816		
t4.9	Corrected total		3,481	3,373.73542				
t4.10	Root MSE		0.94772	R-square		0.0759		
t4.11	Dependent mean	ı	0.01606	Adj <i>R</i> -sq		0.0733		
t4.12	Coeff Var		5,899.57118					
t4.13	Parameter estimation	ates						
t4.14	Variable	DF	Parameter e	estimate	Stand	ard error	t value	$\Pr > t $
t4.15	Intercept	1	0.01391		0.016	06	0.87	0.3867
t4.16	EP0801	1	0.18965		0.063	21	3.00	0.0027
t4.17	BP0801	1	-0.01773		0.038	34	-0.46	0.6437
t4.18	CP0801	1	-0.15718		0.071	92	-2.19	0.0289
t4.19	SP0801	1	0.01553		0.040	74	0.38	0.7031
t4.20	REP0801	1	0.01093		0.015	73	0.69	0.4873
t4.21	RBP0801	1	0.01767		0.018	07	0.98	0.3283
t4.22	RCP0801	1	0.02961		0.015	79	1.87	0.0609
t4.23	RSP0801	1	0.14622		0.020	64	7.08	< 0.0001
t4.24	CTEF0801	1	0.11279		0.029	95	3.77	0.0002
t4.25	PM0801	1	-0.16049		0.020	55	-7.81	< 0.0001

In terms of information coefficients, ICs, the use of the WLRR procedure produces the higher IC for the models during the 1998–2007 time period, 0.043, versus the equally weighted IC of 0.040, a result consistent with the previously noted studies.

Let us examine the WLRR SAS output for estimating (4.13) using OLS, ROB using the Beaton–Tukey approximation, and the WLRR techniques for the month of January 2008.

The EP, RCP, RSP, and CTEF variables have the (correct) positive coefficients 394 395 and are statistically significant in the OLS regression, having t-values that exceed 1.645, the critical 10% level; see Table 4.4. The regression F-statistic of 28.53 396 indicates that the overall regression is highly statistically significant for the 3,482 397 firm sample in January 2008. The adjusted R-squared statistic of 0.073 is quite high 398 for cross-sectional regressions (across securities, at one point in time). The 399 400 F-Statistic of 28.53 is statistically significant at the 1% level. The estimated OLS regression is plagued by outliers, as one sees in Fig. 4.1. The studentized residuals, 401 RStudent, discussed in Chap. 2 and shown in Fig. 4.1, indicate the presence of 402 outliers. A scaled residual known as the Cook distance measure, CookD, or Cook's 403 D, also is shown in Fig. 4.1 and confirms the RStudent result. 404



Most of the USER variables are associated with OLS outliers, see Fig. 4.2. The 405 BP, CP, SP, RSP, and PM variables are particularly associated with outliers in 406 the January 2008 regression, Fig. 4.3.

The application of the Beaton–Tukey (BT) outlier-adjustment procedure, used in 408 Bloch et al. (1993), increases the *F*-Statistics from its OLS value of 28.53 to 34.22. 409 Please see Table 4.5. The BT procedure produces positive and statistically significant coefficients on the EP, RSP, and EF (CTEF) variables. The BT procedure 411 reduces the studentized residuals and Cook's D calculated values. Thus, the effect 412 of outliers has been substantially reduced by the Beaton–Tukey Robust Regression 413 application. 414

The application of the principal components regression analysis, WIPC, in the 415 SAS proc IML procedure approximates of Bloch et al. WLRR. The WIPC 416

407 AU19



Fig. 4.2 OLS residuals by independent variables

regression analysis shows that the weighted EP, CP, RSP, and CTEF variables are 417 highly statistically significantly associated with security returns in January 2008. 418 WRDS WIPC 0801 419

VARN	PC9S	TPC9 42
WEP0801	0.044	4.618 42
WBP0801	-0.023	-3.112 42
WCP0801	0.035	4.506 42
WSP0801	-0.020	-2.672 424
WREP0801	0.011	0.992 42
WRBP0801	0.008	0.489 42
WRCP0801	0.018	1.352 42
WRSP0801	0.127	6.615 42
WEF0801	0.138	5.462 42
WPM0801	-0.190	-9.768 43



Fig. 4.3 Robust regression diagnostics-dependent variable: WTR0801



Fig. 4.3 (continued)

The *F*-Statistic of ROB exceeds the OLS *F*-Statistic approximately 90% of the 431 months. The ultimate test of OLS, ROB, and WLRR analyses can be found in the 432 Bloch et al. simulations which report higher Geometric Means, Sharpe Ratios, and 433 *F*-Statistics using WLRR than OLS in estimating models of the determinants of 434 monthly security returns. Moreover, regression weighting of variables 435 outperformed equally weighting the variable in security returns models. We have 436 briefly surveyed the academic literature on anomalies and found substantial evi- 437 dence that valuation, earnings expectations, and price momentum variables are 438 significantly associated with security returns. Further evidence on the anomalies is 439 found in Levy (1999).⁷ We will create portfolios with the USER Model in Chap. 6 440 AU20 AU21

Summary and Conclusions

442

We have used two case studies to illustrate the effectiveness of regression 443 modeling. Regression analysis offered marginal improvement in the case of com- 444 bining GNP forecasts, but offered substantial improvement in identifying financial 445

- · Cash Flow-to-Price is the 12-month trailing cash flow-per-share divided by the current price.
- Earnings-to-Price is the 12-month trailing earnings-per-share divided by the current price.
- Return on Assets is the 12-month trailing total income divided by the most recently reported total assets.
- · Residual Risk is the trailing variance of residual stock return unexplained by market return.
- 12-month Return is the total return for the stock over the trailing 12 months.
- Return on Equity is the 12-month trailing eps divided by the most recently reported book equity.
- Volatility is the 24-month trailing volatility of total stock return.
- Book-to-Price is the most recently reported book value of equity divided by the current market price.
- Profit Margin is 12-month trailing earnings before interest divided by 12-month trailing sales.
- 3-month Return is the total return for the stock over the trailing 3 months.
- Sales-to-Price is 12-month trailing sales-per-share divided by the market price.

The four measures of cheapness in the USER model: cash-to-price, earnings-to-price, book-toprice, and sales-to-price, all have significant positive payoffs. Haugen and Baker (2010) find statistically significant results for the four fundamental factors as did the previously studies we reviewed. The Haugen and Baker (2010) analysis and results are consistent with the Bloch et al. (1993) model.

⁷ Haugen and Baker (2010) extended their 1996 study in a recent volume to honor Harry Markowitz. Haugen and Baker estimate their model using weighted least squares. In a given month they estimated the payoffs to a variety of firm and stock characteristics using a weighted least squares multiple regression in each month in the period 1963 through 2007. Haugen and Baker found the most significant factors were; Residual Return is last month's residual stock return unexplained by the market.
t5.2	Number of observations read		3,475					
t5.3	Number of observ	ation	s used	3,475				
t5.4	Analysis of varia	nce						
t5.5	Source		DF	Sum of squ	ares	Mean square	F value	$\Pr > F$
t5.6	Model		10	151.05	5712	15.10571	34.22	< 0.0001
t5.7	Error		3,464	1,529.1	1683	0.44143		
t5.8	Corrected total		3,474	1,680.17	7395			
t5.9	Root MSE		0.66440	R-square		0.0899		
t5.10	Dependent mean		0.00118	Adj R-sq		0.0873		
t5.11	Coeff Var 56,310					C		
t5.12	Parameter estimat	tes						
t5.13	Variable	DF	Parameter e	estimate	Stand	dard error	t value	$\Pr > t $
t5.14	Intercept	1	0.00627		0.01	128	0.56	0.5781
t5.15	WEP0801	1	0.15940		0.047	797	3.32	0.0009
t5.16	WBP0801	1	-0.02611		0.027	782	-0.94	0.3480
t5.17	WCP0801	1	-0.10215		0.056	519	-1.82	0.0691
t5.18	WSP0801	1	0.01029		0.030	011	0.34	0.7327
t5.19	WREP0801	1	0.01144		0.01	141	1.00	0.3164
t5.20	WRBP0801	1	0.00664		0.016	540	0.41	0.6855
t5.21	WRCP0801	1	0.01746		0.013	305	1.34	0.1811
t5.22	WRSP0801	1	0.12725		0.019	919	6.63	< 0.0001
t5.23	WEF0801	1	0.13858		0.025	527	5.48	< 0.0001
t5.24	WPM0801	1	-0.16475		0.016	590	-9.75	< 0.0001

t5.1 **Table 4.5** ROB NREG0801 the REG procedure model: MODEL1-dependent variable: WTR0801

variables associated with security returns. Regression models addressing outliersand multicollinearity problems outperformed equally weighted strategies in stockselection modeling.

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Chapter 5 Transfer Function Modeling and Granger Causality Testing

2

1

In this chapter we fit univariate and bivariate time series models in the tradition of 4 Box and Jenkins (1976) and Granger and Newbold (1977) and apply traditional 5 Granger causality testing following the Ashley et al. (1980) methodology. Second, 6 we estimate Vector Autoregressive Models (VAR) and Chen and Lee (1990) Vector 7 ARMA (VARMA) causality test. We test two series for causality: (1) stock prices 8 and mergers and (2) the money supply and stock prices. 9

Testing for Causality: The Ashley et al. (1980) Test

There is a large and growing literature on causality testing in economics. Clive 11 Granger, one of the great minds in time series, reminds us that The phrase "X causes 12 Y' must be handled with considerable delicacy, as the concept of causation is a very 13 subtle and difficult one (Ashley et al. (1980)). We will refer to Ashley et al. (1980) 14 as AGS (1980). Granger held that a universally acceptable definition of causation 15 may well not be possible, but a reasonable definition might be the following: Let Ω_n 16 represent all the information available in the universe at time *n*. Suppose that at time 17 *n* optimum forecasts are made of X_{n+1} using all of the information in Ω_n and also 18 using all of this information apart from the past and present values Y_{n-i} , $j \ge 0$, of 19 the series Y_t . If the first forecast, using all the information, is superior to the second, 20 then the series Y_t has some special information about X_t , not available elsewhere, 21 and Y_t is said to cause X_t . Before applying this definition, one must establish the 22 criteria to decide if one forecast is superior to another. The usual procedure is to 23 compare the relative mean-square errors of post-sample forecasts, as we discussed 24 in Chap. 1. 25

To make the suggested definition suitable for practical use a number of 26 simplifications have to be made. Linear forecasts only will be considered, together 27 with the usual least-squares loss function, and the information set Ω_n has to be 28

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AU1

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replaced by the past and present values of some set of time series, R_n : { X_{n-j} , Y_{n-j} , Z_{n-j} , ..., $j \ge 0$ }. Any causation now found will only be relative to R_n ; spurious results can occur if some vital series is not in this set.

The simplest case is when R_n consists of just values from the series X_t and Y_t , 32 where now the definition reduces to the following: let MSE(X) be the population 33 mean-square of the one-step forecast error of X_{m+1} using the optimum linear 34 forecast based on X_{n-i} , $j \ge 0$, and let MSE (X, Y) be the population mean-square 35 of the one-step forecast error of X_{n+1} using the optimum linear forecast based on 36 $X_{n-j}, Y_{n-j} \ge 0$. Then Y causes X if MSE (X, Y) < MSE (X). The testing involving 37 the definition of causation (stated in terms of variances rather than mean-square 38 errors) was introduced into the economic literature by Granger (1969) and it has 39 40 been applied by Sims (1972) and Ashley et al. (1980), which we will refer to as AGS (1980). 41

42 AGS (1980) proposed several step approach to the analysis of causality between 43 a pair of time series X_t and Y_t :

- 44 (i) Each series is prewhitened by building single-series ARIMA models using the
 45 Box–Jenkins procedure.
- 46 (ii) Form the cross-correlogram between these two residual series,

$$\rho_k = \operatorname{corr}(\operatorname{res} x_t, \operatorname{res} y_{t-k}).$$

(iii) For positive and negative values of k: If any ρ_k for k > 0 are significantly 47 different from zero, there is an indication that Y_t may be causing X_t , since the 48 correlogram indicates that past Y_t may be useful in forecasting X_t . Similarly, if 49 any ρ_k is significantly nonzero for $k < 0, X_t$ appears to be causing Y_t . If both 50 occur, two-way causality, or feedback, between the series is indicated. AGS 51 (1980) note that the sampling distribution of the ρ_k depends on the exact 52 relationship between the series. On the null hypothesis of no relationship, it 53 is well known that the ρ_k are asymptotically distributed as independent normal 54 with means zero and variances 1/n, where n is the number of observations 55 employed, but the experience shows that the test suggested by this result 56 must be used with extreme caution in finite samples.¹ In practice, we also 57 use a priori judgement about the forms of plausible relations between eco-58 nomic time series. Thus for example, a value of ρ_1 well inside the interval 59 $\left[-2/\sqrt{n}, +2/\sqrt{n}\right]$ might be tentatively treated as significant, while a substan-60 tially larger value of ρ_7 might be ignored if ρ_5 , ρ_6 , ρ_8 , and ρ_9 are all negligible. 61

This step is analogous to the univariate Box–Jenkins identification step, where a tentative specification is obtained by judgmental analysis of a correlogram. The key word is "tentative"; the indicated direction of causation is only tentative at this stage and may be modified or rejected on the basis of subsequent modeling and forecasting results.

¹One must apparently be even more careful with the Box–Pierce test on sums of squared ρ_k .

- (iv) For every indicated causation, a bivariate model relating the residuals is 67 identified, estimated, and diagnostically checked. If only one-way causation 68 is present, the appropriate model is unidirectional and can be identified directly 69 from the shape of the cross-correlogram, see Granger and Newbold (1977). 70
- (v) From the fitted model for residuals, after dropping insignificant terms, the 71 corresponding model for the original series is derived, by combining the 72 univariate models with the bivariate model for the residuals. It is then checked 73 for common factors, estimated, and diagnostic checks applied.²
- (vi) Finally, the bivariate model for the original series is used to generate a set of 75 one-step forecasts for a post-sample period. The corresponding errors are then 76 compared to the post-sample one-step forecast errors produced by the univari-77 ate model developed in step (i) to see if the bivariate model actually does 78 forecast better.³ The use of sequential one-step forecasts follows directly from 79 the definition above and avoids the problem of error buildup that would 80 otherwise occur as the forecast horizon is lengthened.

Because of specification and sampling error (and perhaps some structural 82 change) the two forecast error series thus produced are likely to be cross-correlated 83 and autocorrelated and to have nonzero means. In light of these problems, no direct 84 test for the significance of improvements in mean-squared forecasting error appears 85 to be available. Consequently, we have developed the following indirect procedure. 86

For some out-of-sample observation, t, let e_{1r} and e_{2r} be the forecast errors made 87 by the univariate and bivariate models, respectively, of some time series. Elementary algebra then yields the following relation among sample statistics for the entire out-of-sample period: 90

$$MSE(e_1) - MSE(e_2) = [s^2(e_1) - s^2(e_2)] + [m(e_1)^2 - m(e_1)^2], \quad (5.1)$$

where MSE denotes sample mean-squared error, s^2 denotes sample variance, and m_{91} denotes sample mean. Letting 92

$$\Delta_t = e_{1t} - e_{2t}$$
 and $\sum_2 = e_{1t} + e_{2t}$, (5.2)

² OLS estimation suffices to produce unbiased estimates, since all the bivariate models considered are reduced forms. It also allows one to consider variants of one equation without disturbing the forecasting results from the other, and it is computationally simpler. On the other hand, where substantial contemporaneous correlation occurs between the residuals, seemingly unrelated regression GLS estimation can be expected to yield noticeably better parameter estimates and post-sample forecasts. All estimation in this study is OLS; a re-estimation of our final bivariate model using GLS might strengthen our conclusions somewhat.

³ Alternatively, one might fit both models to the sample period, produce forecasts of the first postsample observation, reestimate both models with that observation added to the sample, forecast the second post-sample observation, and so on until the end of the post-sample period. This would, of course, be more expensive than the approach in the text.

equation (5.1) can be rewritten as follows, even if e_{1t} and e_{2t} are correlated:

$$MSE(e_1) - MSE(e_2) = \left[\widehat{cov}(\Delta, \sum)\right] + [m(e_1)^2 - m(e_2)^2],$$
 (5.3)

where \widehat{cov} denotes the sample covariance over the out-of-sample period.

Let us assume that both error means are positive; the modifications necessary in 95 the other cases should become clear. Consider the analogue of (5.3) relating 96 population parameters instead of sample statistics, and let cov denote the popula-97 tion covariance and μ denote the population mean. From (5.3), it is then clear that 98 we can conclude that the bivariate model outperforms the univariate model if we 99 can reject the joint null hypothesis cov $(\Delta, \Sigma) = 0$ and $\mu(\Delta) = 0$ in favor of the 100 alternative hypothesis that both quantities are nonnegative and at least one is 101 102 positive.

103 Now consider the regression equation

$$\Delta_t = \beta_1 + \beta_2 \left[\sum_t - m \left(\sum_t \right) \right] + \mu_t, \tag{5.4}$$

where μ_t is an error term with mean zero that can be treated as independent of \sum_t . 104 From the algebra of regression, the test outlined in the preceding paragraph is 105 equivalent to testing the null hypothesis $\beta_1 = \beta_2 = 0$ against the alternative that 106 both are nonnegative and at least one is positive. If either of the two least squares 107 estimates, $\hat{\beta}_1$ and $\hat{\beta}_2$, is significantly negative, the bivariate model clearly cannot be 108 judged a significant improvement. If one estimate is negative but not significant, a 109 one-tailed t test on the other estimated coefficient can be used. If both estimates are 110 positive, an F test of the null hypothesis that both population values are zero can be 111 employed. But this test is, in essence, four-tailed; it does not take into account the 112 signs of the estimated coefficients. If the estimates were independent, it is clear that 113 114 the probability of obtaining an F-statistic greater than or equal to F_0 , say, and having both estimates positive is equal to one-fourth the significance level 115 associated with F_0 . Consideration of the possible shapes of iso-probability curves 116 $(\hat{\beta}_1, \beta_2)$ under the null hypothesis that both population values are zero for 117 establishes that the true significance level is never more than half the probability 118 obtained from tables of the F distribution. If both estimates are positive, then one 119 can perform an F test and report a significance level equal to half that obtained from 120 the tables. 121

The approach just described differs from others that have been employed to analyze causality in its stress on models relating the original variables and on postsample forecasting performance. We now discuss these two differences. Models directly relating the original variables provide a sounder, as well as a 125 more natural basis for conclusions about causality. As has been argued in detail by 126 Granger and Newbold (1977), however, prewhitening and analysis of the cross- 127 correlogram of the prewhitened series are useful steps in the identification of 128 models relating the original series, since the cross-correlogram of the latter is likely 129 to be impossible to interpret sensibly. Because the correlations between the 130 prewhitened series (the ρ_k) have unknown sampling distributions, this analysis 131 involves subjective judgements, as does the identification step in univariate 132 Box–Jenkins analysis. AGS (1980) state that in neither case is an obviously better 133 approach available, and in both cases the tentative conclusions reached are 134 subjected to further tests.

It is somewhat less clear how out-of-sample data are optimally employed in an 136 analysis of causality. This question is closely related to fundamental problems of 137 model evaluation and validation and is complicated by sampling error and possible 138 specification error and time-varying coefficients. The riskiness of basing 139 conclusions about causality entirely on within-sample performance is reasonably 140 clear. Since the basic definition of causality is a statement about forecasting ability, 141 it follows that tests focusing directly on forecasting are most clearly appropriate. 142 Indeed, it can be argued that goodness-of-fit tests (as opposed to tests of forecasting 143 ability) are contrary in spirit to the basic definition.⁴ Moreover, within-sample 144 forecast errors have doubtful statistical properties in the present context when the 145 Box–Jenkins methodology is employed. While the power of that methodology has 146 been demonstrated in numerous applications and rationalizes our use of it here, it 147 must be noted that the identification (model specification) procedures in steps 148 (i)-(iv) above involve consideration and evaluation of a wide variety of model 149 formulation. A good deal of sample information is thus employed in specification 150 choice, and there is a sense in which most of the sample's real degrees of freedom 151 are used up in this process. It thus seems both safer and more natural to place 152 considerable weight on out-of-sample forecasting performance. 153

The approach outlined above uses the post-sample data only in the final step, as a 154 test track over which the univariate and bivariate models are run in order to 155 compare their forecasting abilities. This approach is of course vulnerable to unde-156 tected specification error or structural change. Partly as a consequence of this, the 157 likely characteristics of post-sample forecast errors render testing for performance 158 improvement somewhat delicate, as we noted above. Finally, the appropriate 159 division of the total data set into sample and post-sample periods in the AGS 160

⁴ If one finds that one model (using a wider information set, say) fits better than another, one is really saying "If I had known that at the beginning of the sample period, I could have used that information to construct better forecasts *during* the sample period." But this is not strictly operational and thus seems somewhat contrary in spirit to the basic definition of causality that we employ.

(1980) approach is unclear, and this is a nontrivial problem. We do not want to seem
overly dogmatic on this issue. Our basic point is simply that model specification
(perhaps especially within the Box–Jenkins framework) may well be infected by
sampling error and polluted by data mining, so that it is unwise to perform tests for
causality on the same data set used to select the models to be tested.

AGS applied their methodology to aggregate advertising and consumption 166 during the 1956-1975 period. The bivariate aggregate consumption model, 167 using aggregate advertising as its input, reduced the out-of-sample forecasting 168 error by only 5.1 % relative to the univariate aggregate consumption model, 169 indicating that aggregate advertising does not cause aggregate consumption. The 170 bivariate aggregate advertising model, using aggregate consumption as its input, 171 172 reduced the out-of-sample forecasting error by 26 % relative to the univariate aggregate advertising model, indicating that aggregate consumption causes aggre-173 gate advertising. 174

175 Quarterly Mergers, 1992–2011: Automatic Time Series 176 Modeling and an Application of the Ashley et al. (1980) Test

Let us explore further the AGS (1980) approach using a case study of aggregate 177 mergers using Mergerstat quarterly data from 1992 to 2011. There is a well-178 established history of mergers and stock prices.⁵ Guerard (1985) used the AGS 179 (1980) bivariate transfer function causality testing methodology and reported that 180 stock prices led mergers over the Nelson quarterly data from 1895 to 1954. Guerard 181 reported that the bivariate merger model, with stock prices as its input, reduced the 182 out-of-sample forecasting errors by 35.7 % less than the univariate time series 183 merger model. Thus, quarterly stock prices led mergers over the 1895–1954 period. 184 We use the AGS (1980) approach to model mergers as a function of leading 185 economic indicators (LEI) and stock prices (using the S&P 500). Most economic 186

⁵ The merger history of the United States was studied by Nelson (1959), who reported that mergers were highly correlated with stock prices and industrial production from 1895 to 1954. Nelson (1966) later found that stock prices lead mergers by over 5 months (5.25) over the 1919–1961 period. Melicher et al. (1983) and Guerard (1985) used ARIMA and transfer function modeling to find that stock prices lead mergers. Guerard and McDonald (1995) reported that the annual merger series from 1895 to 1979 was a near-random walk and that outlier-estimated time series models did not statistically outperform the naïve random walk with drift model. Golbe and White (1993) fit a sine wave to a "spliced" US annual merger history and found that a sine wave, representing a 40-year merger model, described the behavior of mergers.

historians recite the major merger movements and their "waves" since 1895.⁶ 187 AU2 A time series of the US quarterly data is obtained from the FactSet Mergerstat 188 database for 1992–2011Q2. The data is read into Oxmetrics. We run an analysis of 189 the quarterly data in which the change in the logarithmic transformation (dlog) of 190 mergers is a function of the dlog components of the LEI published by The 191

The height of the merger movement was reached in 1901 when 785 plants combined to form America's first billion-dollar firm, the United States Steel Corporation. The series of mergers creating the US Steel allowed it to control 65 % of the domestic blast furnace and finished steel output. This growth in concentration was typical of the first merger movement. The early mergers saw 78 of 92 large consolidations gain control of 50 % of their total industry output, and 26 secure 80 % or more.

The first major merger movement occurred during a period of rapid economic growth. The economic rationale for the large merger movement was the development of the modern corporation, with its limited liability, and the modern capital markets, which facilitated the consolidations through the absorption of the large security issues necessary to purchase firms. Nelson found that the mergers were highly correlated to the period's stock prices and industry production. However, mergers were more sensitive to stock prices. The expansion of security issues allowed financiers the financial power necessary to induce independent firms to enter large consolidations. The rationale for the first merger movement was not one of trying to preserve profits despite slackening demand and greater competitive pressures. Nor was the merger movement the result of the development of the national railroad system, which reduced geographic isolation and transportation costs. The first merger movement ended in 1904 with a depression, the onset of which coincided the Northern Securities case. Here it was held, for the first time, that antitrust laws could be used to attack mergers leading to market dominance.

A second major merger movement stirred the country from 1916 to the depression of 1929. This merger movement was only briefly interrupted by the First World War and the recession of 1921 and 1922. The approximately 12,000 mergers of the period coincided with the stock market boom of the 1920s. Although mergers greatly affected the electric and gas utility industry, market structure was not as severely concentrated by the second movement as it was by the first merger movement. Stigler (1950) concluded that mergers during this period created oligopolies, such as Bethlehem Steel and Continental Can. Mergers, primarily vertical and conglomerate in nature as opposed to the essentially horizontal mergers of the first movement, did affect competition adversely. The conglomerate product-line extensions of the 1920s were enhanced by the high-cross elasticities of demand for the merging companies' products Lintner (1971). Antitrust laws,

⁶The US merger history was characterized by George Stigler (1950) to have occurred in three waves. The first major merger movement began in 1879, with the creation of the Standard Oil Trust, and ended with the depression of 1904. During the merger movement, giant corporations were formed by the combination of numerous smaller firms. The smaller companies represented nearly all the manufacturing or refining capacity of their industries. The forty largest firms in the oil-refining industry, comprising over ninety percent of the country's refining capacity and oil pipelines for its transportation, combined to form Standard Oil. In the two decades following the rise of Standard Oil, similar horizontal mergers created single dominant firms in several industries. These dominant firms included the Cottonseed Oil Trust (1884), the Linseed Oil Trust (1885), the National Lead Trust (1887), the Distillers and Cattle Feeders (1887), and the Sugar Refineries Company (1887). The trust form of organization was outlawed by court decisions. But merger activities continued to create "near" monopolies as the single corporation or holding company organization became dominant. The Diamond Match Company (1889), the American Tobacco Company (1890), the United States Rubber Company (1892), the General Electric Company (1892), and the United States Leather Company (1893) were created by the development of the modern corporation or holding company.

Conference Board. An AR(1) process adequately models the quarterly mergers 192 series, using 32 observations for the estimation period, see Table 5.1, as the partial 193 autocorrelation (PAC) function dies after lag 1. A time series regression of mergers 194 as a function of the components of the LEI reveals that only stock prices and the 195 money supply are statistically significant at the 15 % level; moreover, the money 196 supply variable has an incorrectly negative coefficient, see (5.5). An application of 197 the Automatic Modeling Selection procedure, see (5.6), leads to only the negative 198 money supply. Guerard reported a four-quarter lag in the relationship between 199 mergers and stock prices from 1895 to 1954. We expect lags in the LEI to lead 200 mergers. We use one- and two-quarter lags in the LEI data (see Table 5.2 for the 201 cross-correlation estimate) and report in (5.8) that the one-period lagged stock 202 203 price series is statistically correlated with mergers. In (5.8), (5.9), and (5.10), we report that the current and one-period lagged stock price data leads mergers. The 204 F-statistic of (5.10) dominates the F-statistics of (5.8) and (5.9) in which we run 205 regressions of mergers as a function of the LEI data. There is a statistically 206 207 significant two-quarter lag with LEI and mergers; however, the effect is less statistically pronounced than the stock price data. An application of the Doornik 208 and Hendry (2009a, b) Automatic Modeling Selection procedure, see (5.7), leads to 209 a one-period lag in stock prices and four outliers. A further application of the 210 Doornik and Hendry (2009a, b) Automatic Modeling Selection cointegration pro-211 cedure, see SYS (10), leads to a one-period lag in stock prices and four outliers. 212

though not seriously enforced, prevented mergers from creating a single dominant firm. Merger activity diminished with the depression of 1929 and continued to decline until the 1940s.

The third merger movement began in 1940; mergers reached a significant proportion of firms in 1946 and 1947. The merger action from 1940 to 1947, although involving 7.5 % of all manufacturing and mining corporations and controlling 5 % of the total assets of the firms in those industries, was quite small compared to the merger activities of the 1920s. The mergers of the 1940s included only one merger between companies with assets exceeding 50 million dollars and none between firms with assets surpassing 100 million dollars. The corresponding figures for the mergers of the 1920s were 14 and eight, respectively. Eleven firms acquired larger firms during the mergers of the 1920s than the largest firm acquired during the 1940s merger. The mergers of the 1940s affected competition far less than did the two previous merger movements, with the exception of the food and textile industries. The acquisitions by the large firms during the 1940s rarely amounted to more than seven percent of the acquiring firms' 1939 assets or to as much as a quarter of ~ the acquiring firm's growth rate from 1940 to 1947. Approximately 5 billion dollars of assets were held by acquired or merged firms over the 1940–1947 period. Smaller firms were generally acquired by larger firms. Companies with assets exceeding 100 million dollars acquired, on average, firms with assets of less than two million dollars. The larger firms tended to engage in a greater number of acquisitions than smaller firms. The acquisitions by the larger, acquiring firms tended to involve more firms than did those acquired by smaller, acquiring firms. Mergers added relatively less to the existing size of the larger acquiring firms in the early period of the third merger movement. The relatively smaller asset growth of the larger acquiring firms is in accordance with the third merger movement's generally small effects on competition and concentration. One factor contributing to the maintenance of competition was the initiative for the mergers coming from the owners of the smaller firms. Financiers and investment bankers did not play a prominent part in the early third merger movement, but certainly have in the 1992–2011 period.

AU3

 Table 5.1
 Quarterly mergers, 1992–2011, autocorrelation function estimates

Sample 1 32		
Autocorrelation	Partial Correlation	AC PAC Q-Stat Prob
*** .	***	1 -0.430 -0.430 6.4786 0.011
. **.	. * .	2 0.289 0.129 9.5172 0.009
.** .	.* .	3 -0.297 -0.167 12.836 0.005
. **.	. * .	4 0.323 0.163 16.883 0.002
*** .	.* .	5 -0.335 -0.147 21.400 0.001
. **.	. .	6 0.220 -0.027 23.434 0.001
.** .	. .	7 -0.193 -0.013 25.051 0.001
. .	.** .	8 -0.047 -0.309 25.153 0.001
.* .	.* .	9 -0.111 -0.124 25.734 0.002
. .	.** .	10 -0.028 -0.228 25.772 0.004
. * .	. .	11 0.067 0.016 26.002 0.006
.* .	.** .	12 -0.185 -0.224 27.874 0.006
. * .	.* .	13 0.121 -0.146 28.709 0.007
. .	. * .	14 0.022 0.127 28.737 0.011
. * .	. .	15 0.102 -0.057 29.399 0.014
. .	. * .	16 -0.008 0.112 29.403 0.021

Table	5.2	Quarterly	mergers,	1992–2011,	cross-correlation	function
estimat	es					

Sample 1 32

Included observations: 32			
Correlations are asymptotically	consistent	approx	imations

DDMERGERS,DLEI(-i)	DDMERGERS,DLEI(+i)	i	lag	lead
. * .	. * .	C	0 -0.0949	-0.0949
. * .		1	-0.1243	0.1088
. * .	. ***.	2	0.1017	0.2784
.*** .	.** .	З	3 -0.3371	-0.1761
. * .	. * .	4	-0.0897	0.1190
	. ** .	5	5 -0.0390	0.1976
. * .	. * .	6	6 0.0523	0.1242
. **		7	7 -0.1949	0.0298
. ** .	. * .	8	0.2065	-0.1144

If one applies the Ashley et al. (1980) transfer function causality test to the 213 mergers and stock price series, one finds a *t*-value of 0.57 on the stock price series. 214 That is, a transfer function merger model using one-period lagged stock prices as an 215 input reduces the root mean square root relative to a random-walk with drift model, 216 but the forecast error reduction is not statistically significant, a result reported by 217

t1.1

105

t1.2

t2.1

t2.2

218 Guerard and McDonald (1995). Ashley (1998, 2003) and Thomakos and Guerard (2004) have reexamined the issue of post-sample periods for model validation and 219 relative forecasting efficiency. The purpose of this case study is to present an 220 updated and new analysis of the merger movements in the United States and the 221 relationship between mergers, stock prices, and LEI. We find additional statistical 222 correlation and regression analysis to support the historical statistical evidence that 223 stock prices lead mergers. Stock prices are a component of the LEI; however, stock 224 prices more directly lead mergers than the LEI. Stock prices do not lead mergers in 225 an Ashley, Granger, and Schmalensee causality test for the 1992–2011 period.⁷ 226

Ox Professional version 6.00 EQ(5) Modelling dDMergers by Ordinary Least Squares (OLS) Coefficient Std.Error t-value t-prob Part.R^2 0.0616215 0.02423 2.54 0.0134 0.0905 Constant 0.2470 dHrWeek 2.20214 1.885 1.17 0.0206 dWkInCL -0.406564 0.2838 -1.43 0.1568 0.0306 -1.41 dMfgOrders -1.00722 0.7157 0.1641 0.0296 dSuppDev 0.317889 0.2910 1.09 0.2787 0.0180 dMfgNonD 0.0253327 0.2199 0.115 0.9086 0.0002 BldPerm 0.293603 0.2489 1.18 0.2425 0.0210 dSP500 0.331035 0.2130 1.55 0.1250 0.0358 dM2 -2.53324 1.605 -1.58 0.1194 0.0369 dConExp 0.00541588 0.1708 0.0317 0.9748 0.0000 0.107663 RSS 0.753438773 sigma $0.243771 \quad F(10,65) =$ R^2 2.095 [0.037]* 0.127429 log-likelihood Adj.R^2 67.4866

The use of the Autometrics algorithm in Oxmetrics for automatic time series regressions is reported in Equation 6.

Autometrics:	dimens:	ions of initial GUM	
no. of observations	76	no. of parameters	11
no. free regressors (k1)	11	no. free components	(k2) 0
no. of equations	1	no. diagnostic tests	5
Summary	of Auto	metrics search	
initial search space	2^11	final search space	2^3
no. estimated models	93	no. terminal models	2
test form	LR-F	target size Defa	ault:0.05
outlier detection	no	presearch reduction	lags
backtesting	GUM0	tie-breaker	SC
diagnostics p-value	0.01	search effort	standard
time	0.12	Autometrics version	1.5e

⁷ Neither stock prices nor LEI passed the AGS (1980) causality test for mergers.

EQ(6) Modelling dDMergers by OLS

Constant dM2	Coefficient 0.0595716 -4.34725	Std.Error 0.01523 1.198	t-value 3.91 -3.63	t-prob 0.0002 0.0005	Part.R^2 0.1713 0.1511
sigma R^2 Adj.R^2 no. of observa mean(dDMergers	0.1069 0.1511 0.1396 s) 0.02678	05 RSS 43 F(1,74) 72 log-li) 76 no. of 42 se(dDMe) = 13 kelihood parameter ergers)	0.84 .18 [0.0 63 	457254 D01]** 3.0958 2 L15257
AR 1-2 t ARCH 1-3	test: F(2 test: F(1	,72) = ,74) = 0.	3.1772 [0 .094512 [0	.0476]* .7594]	

ARCH 1-1 test. The use of the lagged LEI components in the merger analysis is shown in GUM (3), and lagged stock prices are statistically significant.

	dom(5) Hoderri	ing abherge	T2 DY OH2		
	Coefficient	Std.Error	t-value	t-prob	Part.R^2
Constant	0.0293535	0.02199	1.33	0.1886	0.0373
dHrWeek	0.718022	1.935	0.371	0.7123	0.0030
dHrWeek 1	-4.76930	2.260	-2.11	0.0403	0.0883
dHrWeek 2	1.46406	1.945	0.753	0.4554	0.0122
dWkInCL	-0.268383	0.2958	-0.907	0.3690	0.0176
dWkInCL 1	0.154163	0.2948	0.523	0.6036	0.0059
dWkInCL ²	-0.0874009	0.2729	-0.320	0.7502	0.0022
dMfgOrders	-0.888739	0.7525	-1.18	0.2437	0.0294
dMfgOrders_1	0.595087	0.7798	0.763	0.4493	0.0125
dMfgOrders_2	0.397199	0.7510	0.529	0.5994	0.0060
dSuppDev	0.149083	0.2632	0.566	0.5739	0.0069
dSuppDev_1	-0.291959	0.2718	-1.07	0.2883	0.0245
dSuppDev 2	0.289764	0.2669	1.09	0.2832	0.0250
dMfgNonD	0.0375464	0.2700	0.139	0.8900	0.0004
dMfgNonD 1	-0.186103	0.2740	-0.679	0.5004	0.0099
dMfgNonD_2	-0.206999	0.2516	-0.823	0.4149	0.0145
BldPerm	-0.162543	0.2562	-0.634	0.5289	0.0087
BldPerm_1	0.231607	0.2557	0.906	0.3698	0.0175
BldPerm_2	0.166691	0.2366	0.705	0.4846	0.0107
dSP500	0.181444	0.1974	0.919	0.3627	0.0180
dSP500_1	0.374018	0.2129	1.76	0.0856	0.0629
dSP500_2	0.261796	0.2092	1.25	0.2171	0.0329
dM2	-2.36158	1.649	-1.43	0.1588	0.0427
dM2_1	-1.56727	1.631	-0.961	0.3417	0.0197
dM2_2	1.89004	1.452	1.30	0.1994	0.0355
dConExp	0.0499092	0.1528	0.327	0.7454	0.0023
dConExp_1	0.0725079	0.1710	0.424	0.6735	0.0039
dConExp_2	-0.00138546	0.1626	-0.00852	0.9932	0.0000
sigma	0.09363	25 RSS		0.4032	284062
R^2	0.5317	62 F(27,40	5) = 1	.935 [0.	024]*
Adj.R^2	0.2569	27 log-lil	kelihood	87	.8492
no. of observ	vations	74 no. of	parameter	s	28
mean(dDMerger	s) 0.02095	68 se(dDMe	ergers)	0.	10862

Chow test:	AR 1-2 test: F(2,44) = 5.5118 [0.0073]** ARCH 1-1 test: F(1,72) = 10.026 [0.0023]** Normality test: Chi^2(2) = 2.2175 [0.3300] Hetero test: F(54,19) = 1.4692 [0.1790] F(21,25) = 0.71075 [0.7849] for break after 55
no. no. no.	Autometrics: dimensions of initial GUM of observations 74 no. of parameters 28 free regressors (k1) 28 no. free components (k2) 0 of equations 1 no. diagnostic tests 5
init no. test outl back diag time	Summary of Autometrics searchial search space2^28 final search space2^8estimated models193 no. terminal models4formLR-F target sizeDefault:0.05ier detectionnopresearch reductionlagstestingGUM0tie-breakerSCnostics p-value0.01search effortstandard0.25Autometrics version1.5e
	UM(4) Modelling dDMergers by OLS
Constan dSP500 dSP500_ dSP500_	Coefficient Std.Error t-value t-prob Part.R^2 t 0.00555250 0.01152 0.482 0.6315 0.0033 0.291821 0.1458 2.00 0.0493 0.0541 1 0.515576 0.1481 3.48 0.0009 0.1475 2 0.204682 0.1467 1.40 0.1673 0.0271
sigm R^2 Adj. no. mean	a 0.0951595 RSS 0.633873118 0.264034 F(3,70) = 8.371 [0.000]** R^2 0.232493 log-likelihood 71.1175 of observations 74 no. of parameters 4 (dDMergers) 0.0209568 se(dDMergers) 0.10862
Chow test:	AR 1-2 test: ARCH 1-1 test: Normality test: Hetero test: F(2,68) = 9.0433 [0.0003]** F(1,72) = 2.3886 [0.1266] 10.374 [0.0056]** F(6,67) = 0.52308 [0.7888] F(21,49) = 0.66163 [0.8483] for break after 55

The use of the lagged LEI components in the merger analysis is shown in equation 7, EQ(7), and current and lagged stock prices are statistically significant. EQ(7) Modelling dDMergers by OLS

EQ(/) Modelling (inwerde	ers by Ors		
Co	efficient Sto	d.Erro	r t-value	t-prob	Part.R^2
dSP500	0.320817	0.1440	2.23	0.0290	0.0645
dSP500_1	0.569148	0.1442	2 3.95	0.0002	0.1778
siama	0 0954224	BGG		0 655	590714
lc	g-likelihood	1000	69.871	0.000	550714
no. of observatic	ns 74	no. o:	f paramete	rs	2
mean(dDMergers)	0.0209568	se (dDì	Mergers)	0	.10862
AR 1-2 test	F(2,70)	=	9.5500 [(.0002]**	
ARCH 1-1 t	est: F(1,72) =	1.9007	[0.1723]	
Normality to	est: Chi^2(2) =	10.625 [().0049]**	
Hetero tes	t: F(4,69) =	0.72801	[0.5759]	
Hetero-X t	est: F(5,68) =	1.1718	[0.3321]	
RESET23 te	st: F(2,70) =	0.058718	[0.9430]	

GUM(6) Modelling dDMergers by OLS Coefficient Std.Error t-value t-prob Part.R^2 2.11 0.0384 dSP500 0.302460 0.1434 0.0590 dSP500 1 0.524426 0.1462 3.59 0.0006 0.1534 dSP500 2 0.214017 0.1446 1.48 0.1433 0.0299 0.0946435 RSS 0.635975134 sigma log-likelihood 70.995 no. of observations 74 no. of parameters 3 0.0209568 se(dDMergers) 0.10862 mean(dDMergers) AR 1-2 test: = 9.0747 [0.0003]** F(2,69) F(1,72) = 1.8115 [0.1826]ARCH 1-1 test: Normality test: Hetero test: F(6,67) F(21,50) = 0.63549 [0.8713] for break after 55 Chow test: EQ(8) Modelling dDMergers by OLS Coefficient Std.Error t-value t-prob Part.R^2 dSP500 1 0.603289 0.1080 5.59 0.0000 0.3115 4.05 0.0001 I:12 0.296530 0.07331 0.1917 4.86 I:16 0.357167 0.07352 0.0000 0.2548 I:18 0.288096 0.07331 3.93 0.0002 0.1829 -2.45 I:65 -0.179780 0.07331 0.0167 0.0802 0.0733045 RSS 0.370775349 sigma 90.9588 o. of parameters log-likelihood ions 74 no. 74 no. of paramet 0.0209568 se(dDMergers) no. of observations 5 mean(dDMergers) 0.10862 AR 1-2 test: F(2,67) = 2.5108 [0.0888] AR I-2 test: ARCH 1-1 test: F(1,72)Normality test: Chi^2(2) ARCH 1-1 test. Normality test: = 0.072879 [0.7880] = 0.21892 [0.8963]= 0.59968 [0.5519] F(2,67) Hetero-X test: F(2,67) = 0.59968 [0.5519] RESET23 test: F(2,67) = 2.9589 [0.0587] EQ(9) Modelling dDMergers by OLS Coefficient Std.Error t-value t-prob Part.R^2 dDMergers_1 -0.307811 0.1105 -2.78 0.0069 0.1010 -0.0183499 0.01466 -1.25 0.2150 Constant 0.0222 dlei 1.41159 1.122 1.26 0.2128 0.0224 1.64150 1.36 0.1779 dLEI] 1.206 0.0261 dLEI 2 3.29982 1.159 2.85 0.0058 0.1052 sigma 0.0963794 RSS 0.640940151 0.255829 5.93 [0.000]** R^2 F(4, 69) =Adj.R^2 70.7073 0.212689 log-likelihood 74 no. of observations no. of parameters 5

0.0209568 se(dDMergers)

0.10862

mean(dDMergers)

* *

* * * *

* * * *

EQ(10) Modelling dDMergers by OLS

dDMergers_1 dLEI_2	Coefficient -0.266408 4.16836	Std.Error 0.1109 0.9233	t-value -2.40 4.51	t-prob Part.R^2 0.0189 0.0742 0.0000 0.2206
sigma log-likelihood	0.0980261 67.8789	RSS	0.	.691856946
mean(dDMergers)	0.0209568	se(dDMerge	rs)	0.10862
AR 1-2 te ARCH 1-1 Normality Hetero te Hetero-X RESET23 t	st: F(2, test: F(1, test: Chi' st: F(4, test: F(5, est: F(2,	$\begin{array}{rcl} 70) & = & 2\\ 72) & = & 0\\ 2(2) & = & 1\\ 69) & = & 0\\ 68) & = & 0\\ 70) & = & 0 \end{array}$	2.1666 [0. .19580 [0. .1.783 [0. .37461 [0. .32981 [0. .13933 [0.	1222] 6595] 0028]** 8260] 8933] 8702]
SYS	(10) Estimat	ing the sys	tem by OLS	
URF equation : dSP500_1 dSP500_2	for: dDMerger Coeffici 0.684	s ent Std.Er 853 0.1	ror t-va	lue t-prob .59 0.0000
dSF500_2 dDMergers_1 I:12 I:16	-0.403 0.265	148 0.09 718 0.07 818 0.07	2293 3 9623 -4 7600 3 7591 4	.19 0.0001 .50 0.0009 .73 0.0000
I:21 I:27 I:41	-0.0583 0.00245 -0.0283	222 0.07 011 0.07 959 0.07	7659 -0. 758 0.0 7627 -0.	762 0.4492 316 0.9749 372 0.7109
I:66 Constant	0.0455 U 0.00528	124 0.07 934 0.009	0. 0625 0.	580 0.5638 550 0.5846
sigma = 0.075:	1446 RSS =	0.350096260)8	
URF equation :	tor: dSP500 Coefficie	nt Std.Err	or t-valu	ue t-prob
dSP500_1 dSP500_2 dDMergers_1 I.12	0.197 0.0479 -0.0327 0.0723	326 0.1 722 0.1 802 0.07 661 0.06	.002 1 .057 0. 7869 -0.	.97 0.0535 454 0.6516 417 0.6784 16 0.2487
I:12 I:16 I:21 I:27	0.0295	421 0.06 6644 0.06 216 0.06	5208 0. 5263 2 5344 3	476 0.6358 .87 0.0056 .12 0.0027
I:41 I:66 Constant	-0.217 -0.261 U 0.0123	843 0.06 739 0.06 240 0.007	5237 -3 5413 -4 7871 1	.49 0.0009 .08 0.0001 .57 0.1225
sigma = 0.0614508 F	RSS = 0.23412	44214		
log-likelihood Omega 1.28000 R^2(LR) no. of observations	201.251 -T 1728e-005 lo 0.809249 R^ 72 no	/2log Omega g Y'Y/T 2(LM) . of parame	405. -9.60 ters	.578149 0927303 .553802 20
F-test on regressors F-tests on retained r dSP500_1 15 dDMergers_1 9. I:16 12 I:27 5.	except unres regressors, F 6.4890 [0.000 84542 [0.000 2.5221 [0.000 88011 [0.005 5830 [0.005	tricted: F((2,61) =]** dSP5]**]**]**	18,122) = 00_2 I:12 I:21 I:41 tant U	8.74087 [0.0000] 6.16797 [0.004] 6.09321 [0.004] 6.51040 [0.003] 6.80811 [0.003] 1.21699 [0.303]

Causality Testing: An Alternative Approach by Chen and Lee 229

The most complicated task in transfer function modeling is the identification of the 230 transfer function form for each input series, particularly if the transfer function 231 model includes multiple-input variables. Let us use the methodology of Liu (1999) 232 and Chen and Lee (1990) to employ the linear transfer function (LTF) method. The 233 LTF identification method can be used in the same manner no matter if the transfer 234 function model has single-input or multiple-input variables. This method is more 235 practical and easier to use than the cross correlation function (CCF) method 236 discussed in Box and Jenkins (1976).

As in multiple regression models, a single-equation transfer function model 238 may contain more than one input variable. Assuming that the input and output 239 series are both stationary, the general form of a single-input transfer function 240 model is 241

$$Y_t = C + \frac{\omega(B)}{\delta(B)} X_t + N_t, \quad N_t = \frac{\theta(B)}{\phi(B)} a_t, \tag{5.5}$$

where $\omega(B) = (\omega_0 + \omega_1 B + \dots + \omega_{h-1} B^{h-1}) B^b$,

$$\delta(B) = 1 - \delta_1 B - \dots - \phi_r B^r,$$

$$\phi(B) = 1 - \phi_1 B - \dots - \phi_p B^p,$$

$$\theta(B) = 1 - \theta_1 B - \dots - \theta_q B^q.$$

and

The operators $\phi(B)$ and $\theta(B)$ can be in simple or multiplicative form. In the 244 above model, N_t is referred to as the disturbance or noise of the model, and a_t is a 245 sequence of random shocks following i.i.d. In model (5.5), the order *b* in the $\omega(B)$ 246 polynomial is referred to as the *delay* of the transfer function. Box and Jenkins 247 (1976) defined $\omega(B)$ as 248

$$\omega(B) = (\omega_0 - \omega_1 B - \dots - \omega_{h-1} B^{h-1}) B^b.$$
(5.6)

By using a positive sign in front of all ω_j coefficients, Chen and Lee (199) state 249 that the direction of changes in Y_t will correspond to the direction of changes in X_t 250 *consistently* depending on the sign of ω_j . 251

Similar to the stationary condition for $\phi(B)$, it is important to restrict all roots of 252 the $\delta(B)$; it is polynomial to lie outside the unit circle. Under such an assumption, 253 the transfer function $\omega(B)/\delta(B)$ can always be expressed in linear form as 254

243

5 Transfer Function Modeling and Granger Causality Testing

$$V(B) = v_0 + v_1 B + v_2 B^2 + \cdots.$$
 (5.7)

The LTF *V*(*B*) has a finite number of terms if $\delta(B) = 1$ (since *V*(*B*) = $\omega(B)$) and an infinite number of terms if $\delta(B) \neq 1$. The values v_0, v_1, v_2, \ldots are referred to as transfer function weights (or impulse response weights) for the input series X_t . Using *V*(*B*), the transfer function in (5.7) can be expressed in linear form as

$$Y_t = C + V(B) X_t + N_t. (5.8)$$

Single-equation transfer function modeling also assumes a unidirectional rela-259 tionship between the input and the output series, i.e., X_t may affect the present and 260 future value of Y_t , but Y_t does not influence X_t . The same notion holds true if there 261 are multiple-input series in the model. It is important to verify that only a 262 unidirectional influence is present among the variables in a single-equation 263 transfer function analysis. If a bidirectional or feedback relationship exists 264 among the variables, inconsistent parameter estimates may occur. It is easy to 265 extend the single-input model to multiple-input models. Assuming that we have m 266 input variables in the system, the multiple-input transfer function model can be 267 written as 268

$$Y_t = C + \frac{\omega_1(B)}{\delta_1(B)} X_{1t} + \frac{\omega_2(B)}{\delta_2(B)} X_{2t} = \dots + \frac{\omega_m(B)}{\delta_m(B)} X_{mt} + \frac{\theta(B)}{\phi(B)} a_t,$$
(5.9)

where the rational transfer function $\omega_i(B)/\delta_i(B)$ for each input variable has the general form as defined in (5.9).

The identification method to be discussed in this section is applicable for both single-input and multiple-input transfer function models for notational convenience; however, the single-input model presented in (5.9) will be used here. The transfer function model identification procedure can be generally divided into three steps:

276 1. Estimation of the transfer function weights, v_i 's

277 2. Determination of the model for the disturbance term N_t

278 3. Determination of the form of the rational polynomial $\omega(B)/\delta(B)$ that best 279 approximates V(B)

The CCF is primarily used as a tool for diagnostic checking.

The rational transfer function $\omega(B)/\delta(B)$ can be approximated by an LTF V(B)with a finite number of terms, say K + 1. Using such an approximation, model (5.10) can be expressed as

$$Y_t = C + (v_0 + v_1 B + v_2 B^2 + \dots + v_K B^K) X_t + N_t.$$
(5.10)

Using the above model, the transfer function weights $v_0, v_1, v_2, \ldots, v_K$ can be 284 easily obtained by the ordinary least squares method. 285

The use of the autoregressive disturbance models in the LTF method shall 286 improve the efficiency of the transfer function eight estimates, which in turn 287 shall improve the accuracy of the estimated disturbance \hat{N}_i . The values of $\hat{\phi}_1$ and 288 $\hat{\Phi}_1$ may also provide an indication of whether regular or seasonal differencing of the 289 input and output series is necessary. After the transfer function weights are 290 estimated, the disturbance series can be computed using these weights where 291

$$\hat{N}_t = Y_t - \hat{C} - \hat{V}(B)X_t.$$
(5.11)

After the transfer function weights are estimated, the form of the rational transfer 292 function $\omega(B)/\delta(B)$ can also be determined. Recall that 293

$$V(B) = \frac{\omega(B)}{\delta(B)} = \frac{(\omega_0 + \omega_1 B + \dots + \omega_{h-1} B^h) B^h}{1 - \delta_1 B - \dots - \delta_r B^r}.$$
 (5.12)

If $\delta(B) = 1$ (i.e., r = 0), then $V(B) = \omega(B)$ and V(B) has a cutoff pattern. On the 294 other hand, if $\delta(B) \neq 1$ (i.e., $r \geq 1$), then V(B) is an infinite series theoretically and 295 therefore has a die-out pattern. Since $\hat{V}(B)$ is an estimate of V(B), we may conclude 296 that $\delta(B) = 1$ and $\omega(B)$ comprise only the significant terms in $\hat{V}(B)$ if $\hat{V}(B)$ has a 297 cutoff pattern. On the other hand when $\hat{V}(B)$ has a die-out pattern, it implies that the 298 $\delta(B)$ polynomial is not 1. In such a case, the corner table method proposed in Liu 299 and Hanssens (1982) can be used to determine the values b, h, and r in the rational 300 $\overline{AU4}$ polynomial $\omega(B)/\delta(B)$. 301

For a set of transfer function weights v_i 's, the *corner table method* can be used to 302 identify the orders in the corresponding rational transfer function $\omega(B)/\delta(B)$. The 303 method uses a table which consists of $\Delta(f, g)$ as the entry of the f-th row and g-th 304 column, $f = 0, 1, 2, \dots, g = 1, 2, 3, \dots$, and $\Delta(f, g)$ is the determinant of a $g \times g$ 305 matrix defined as 306 AU5

$$D(f,g) = \begin{bmatrix} u_f & u_{f-1} & \dots & u_{f-g+1} \\ u_{f+1} & u_f & \dots & u_{f-g+2} \\ \vdots & \vdots & \dots & \vdots \\ u_{f+g-1} & u_{f+g-2} & \dots & u_f \end{bmatrix}$$

where $u_i = v_j / v_{\text{max}}$, $u_j = 0$ if j < 0, and v_{max} is the maximum value of $|v_j|$, j = 1, 2, ..., K. 307 It can be shown that the transfer function weights v_i 's have a representation 308 $\omega(B)/\delta(B)$ with order b, h, and r if the associated table has the following pattern: 309



where a "0" denotes a zero value, an "x" denotes a nonzero value, and an "*" denotes an indefinite value (may or may not be zero). In the above table, the entries in the first *b* rows and the lower right-hand corner starting at row h + b + 1 (labeled as h + b) and column r + 1 are all zeros. Therefore this table can be used to determine the values of *b*, *h*, and *r*. We shall refer to the above table as the corner table for the associated transfer function weights.

In practice the weights v_i are estimated, and the estimates \hat{v}_i are subject to random 317 errors. Consequently, one usually finds some small values in the corner table (for 318 the zeros indicated above). However, the upper section and lower right-hand corner 319 will show a sudden drop in values. Note that in the construction of the corner table, 320 we have $\Delta(f, 1) = \hat{u}_f$ for the entries in the first column (i.e., when g = 1). Since \hat{u}_f is 321 the transfer function weight \hat{u}_f normalized by \hat{v}_{max} , the significance level of the 322 values in the first column is the same as the corresponding transfer function eights 323 estimates. For the entries in the rest of the table, one compares the absolute values 324 of the entries with 1.0 to determine if the entries should be regarded as zeros. After a 325 transfer function model is identified, the next step is to estimate its parameters. 326 Representing the transfer function model as 327

$$Y_t = C + \frac{\omega(B)}{\delta(B)} X_t + \frac{\theta(B)}{\phi(B)} a_t, \qquad (5.13)$$

the task is to estimate the vectors of parameters $\omega = [\omega_0, \omega_1, \dots, \omega_{s-1}]'$, and 328 $\delta = [\delta_1, \delta_2, \dots, \delta_r]', \phi = [\phi_1, \phi_2, \dots, \phi_p]'$, and $\theta = [\theta_1, \theta_2, \dots, \theta_q]'$. If there are 329 several explanatory variables we will have sever ω and δ vectors. The exact ML 330 AU6 method can be used to estimate the parameters in the transfer function model. 331

After a transfer function model has been identified and estimated, it is necessary 332 to verify if the model adequately fits the data. In the same way that the sample ACF 333 is used in the diagnostic checking of ARIMA models, the sample CCF can be used 334 in diagnostic checking of transfer function models. The sample ACF and CCF can 335 be conveniently combined into sample cross correlation matrices (CCM), which 336 can be used to simplify the diagnostic checking procedure. The autocorrelation of a 337 time series represents the correlation between the values within a series. 338

It is useful to note that the cross correlation at lag k is a generalization of 339 autocorrelation at lag k since $\rho_{YX}(k) = \rho_Y(k)$ cross correlation measures not only 340 the strength of an association but also its direction. To see the full picture of the 341 relationship between the series Y_t and X_t , it is important to examine the cross 342 correlations, $\rho_{YK}(k)$, for both positive and negative lags. The sequence of cross 343 correlations $\rho_{YK}(k)$, $k = 0, \pm 1, \pm 2, \pm 3, \ldots$ is referred to as the *CCF* for the 344 bivariate series Y_t and X_t . 345

The estimate of the cross covariance at lag k, $\gamma_{YX}^{(k)}$ in (5.28) is provided by 346

$$C_{YK}(k) = \frac{1}{n} \sum_{t=k+1}^{n} (Y_t - \bar{Y})(X_{t-k} - \bar{X}), \quad k = 0, \ 1, \ 2, \ \dots$$

$$C_{YK}(k) = \frac{1}{n} \sum_{t=1}^{n+k} (Y_{t-k} - \bar{Y})(X_t - \bar{X}), \quad k = 0, -1, -2, \ \dots$$

(5.14)

and \overline{Y} and \overline{X} are the sample means of Y_t and X_t series. Note that $C_{YY}(0)$ and $C_{XX}(0)$ are 347 the estimates of σ_Y^2 and σ_X^2 , respectively. 348

While it is workable to use CCF in diagnostic checking if only two series are 349 considered, it is necessary to put the relevant CCFs into a matrix form to facilitate visual 350 inspection when more than two series are involved in a study. This matrix form CCF is 351 referred to as CCM. Assuming that $Z_t = [Y_t, X_t]'$, the CCM for the vector series Z_t are 352

 $\begin{matrix} \log & 0 & 1 & 2 & 3 \\ 1 & \rho_{YX}(0) & 1 & \rho_{YX}(1) & \rho_{YX}(1) \\ \rho_{YX}(0) & 1 & \rho_{XY}(1) & \rho_{XX}(1) & \rho_{XY}(2) & \rho_{XX}(2) \\ 0 & \rho_{XY}(2) & \rho_{XX}(2) & \rho_{XX}(2) \\ 0 & \rho_{XY}(3) & \rho_{XX}(3) \\ 0 & \rho_{XY}(3) & \rho_{XY}(3) \\ 0 & \rho_{XY}(3) & \rho_{XY}(3)$

Thus the CCM contains the ACF for each series and both directions of CCFs. 353 When the vector series Z_t contains m time series, i.e., $Z_t = [Z_{1t}, Z_{2t}, ..., Z_{mt}]'$, the 354 lag *k* CCM of the vector series Z_t is defined as 355

$$\rho(k) = \begin{bmatrix}
\rho_{11}(k) & \rho_{12}(k) & \cdots & \rho_{1m}(k) \\
\rho_{21}(k) & P_{22}(k) & \cdots & P_{2m}(k) \\
\vdots & \vdots & \cdots & \vdots \\
\rho_{m1}(k) & \rho_{m2}(k) & \cdots & \rho_{mm}(k)
\end{bmatrix}, \quad k = 0, 1, 2, 3, \dots, \quad (5.15)$$

356 where

$$\rho_{ij}(k) = \gamma_{ij}(k) / [\gamma_{ii}(0)\gamma_{jj}(0)]^{1/2}$$

357 and

$$\gamma_{ij}(k) = E[(Z_{it} - \mu_i)(Z_j(t - k) - \mu_j)], \quad \mu_i = E(Z_{it}).$$

Since the cross covariance $\gamma_{ij}(k)$ can be estimated by

$$C_{ij}(k) = \frac{1}{n} \sum_{t=k+1}^{n} (Z_{it} - \bar{Z}_i) (Z_{j(t-k)} - \bar{Z}_j), \qquad (5.16)$$

359 the estimate of the cross correlation at lag k can be written as

$$\hat{\rho}_{ij}(k) = C_{ij}(k) / [C_{ii}(0)C_{jj}(0)]^{1/2}.$$
(5.17)

The (i, j)th element of the displayed lag *k* matrix reflects the correlation between 361 Z_{it} and $Z_{j(t-k)}$. In this manner, the elements of the CCM and the autoregression 362 matrices have similar interpretations.

The CCM provides an effective means to display the autocorrelations and cross 363 correlations jointly. The autocorrelations are represented along the matrix diagonal 364 while the cross correlations are represented by the off-diagonal elements. 365 Interpreting the sample CCM may be difficult due to the number of entries in the 366 367 matrices. Following Tiao and Box (1981), an effective summary of the correlation structure is provided by using the indicator symbols (+, -) to replace the numerical 368 values of the elements in $\hat{\rho}(k)$ matrices, where a "+" sign is employed to indicate a 369 value greater than $1.96/\sqrt{n}$, a "-" sign for a value less than $-1.96/\sqrt{n}$, and a "." for 370 values in between. This device is motivated from the consideration that if the series 371 were white noise, i.e., $Z_{it} = Z_{jt} = a_t$, then for large *n*, the $\rho_{ij}(k)$ would be normally 372 distributed with mean 0 and variance n^{-1} . 373

As in ARIMA modeling, diagnostic checking of transfer function modeling is to 374 confirm (1) model validity and parsimony; (2) no lack of fit in the model; and (3) 375 376 model assumptions are satisfied. Important model assumptions include that (a) a_t follows a white noise process and (b) a_t is independent of X_t and its lags. If the 377 assumption (b) is not satisfied, it means that a_t can be predicted by X_t and its lags, 378 and therefore there is lack of fit in the model. With this in mind, satisfaction of 379 assumption (b) also implies no lack of fit in the model. The methods and tools for 380 checking model validity and keeping model parsimony are the same as those for 381 382 ARIMA modeling and one should examine the time plot of residuals.

To verify assumption (a), the sample ACF of the residual series \hat{a}_t may be examined. If \hat{a}_t is indeed a white noise process, all the sample autocorrelations of the residual series should be insignificant. To verify assumption (b), the CCF between the residuals and prewhitened input series should be examined. If a_t and X_t are independent, none of the sample cross correlations should be significant.

To simplify the diagnostic checking procedure, we may combine the above two steps into one step by suing sample CCM of the residuals and prewhitened input

415

series. Assuming the independence of the residuals and the prewhitened input 390 series, the CCMs between these two series would have insignificant values for the 391 entire matrix over all lags as shown below: 392



The diagonal elements again represent the sample autocorrelations of the \hat{a}_t 's and 393 the prewhitened input series while the off-diagonal elements represent the cross 394 correlations of these series. The dots represent insignificant correlations. If any of 395 these correlations were significant, a "+" or "–" would appear in the relevant 396 matrix element. Prewhitening the input series is required to correctly test for the 397 independence of two series. Suppose that the residual series a_t is white noise but the 398 X_t series is autocorrelated. The resulting CCF would have a pattern very similar to 399 the ACF of the X_t series. Thus an independence test using CCF can be conducted 400 only when each series is serially uncorrelated. It is for this reason that the 401 autocorrelations in the input series be removed by an ARIMA filter before the 402 cross correlation test is made.

Causality Analysis of Quarterly Mergers, 1992–2011:404An Application of the Chen and Lee Test405

Let us consider an economic system with two variables denoted as Y_t , mergers, 406 andCausality Analysis of Quarterly Mergers, 1992–2011... X_t , LEI or stock prices. 407 Denoting the optimal and unbiased forecast of Y_{n+1} using the information set Ω by 408 \hat{Y}_{n+1} , the conditional variance of the forecast error (which is $Y_{n+1} - \hat{Y}_{n+1}$) can be 409 written as $Var(Y_{n+1}|\Omega)$. If the information set Ω is Y, X, or $\{Y \text{ and } X\}$ (i.e., including 410 all data in each variable up to and including t = n), $Var(Y_{n+1}|\Omega)$ is the one-step-411 ahead forecast variance of Y_{n+1} based on Y, X, or $\{Y \text{ and } X\}$, respectively. Below are 412 the definitions of these four possible relationships in Chen and Lee (1990): 413

1. Independency $(Y \land X)$. Y and X are *independent* if and only if 414

$$Var(Y_{n+1}|Y) = Var(Y_{n+1}|Y,X) = Var(Y_{n+1}|Y,X,X_{n+1})$$
(5.18)

and

$$\operatorname{Var}(X_{n+1}|X) = \operatorname{Var}(X_{n+1}|Y,X) = \operatorname{Var}(X_{n+1}|Y,X,Y_{n+1}).$$
(5.19)

When two time series are independent, the one-step-ahead forecast variance of 416 Y_{n+1} based on *Y* will not be reduced by including additional information on *X*, or 417 including both *X* and concurrent information X_{n+1} . Similarly, the same relation-418 ship must also hold true for the one-step-ahead forecast variance of X_{n+1} . 419

5 Transfer Function Modeling and Granger Causality Testing

420 Therefore when two time series are truly *independent*, no external information

421 (including up to the forecast origin and concurrent) can improve the one-step-422 ahead forecast variance of Y_{n+1} or X_{n+1} .

423 2. Contemporaneous $(Y \leftrightarrow X)$: Y and X are *contemporaneously related* if and 424 only if

$$Var(Y_{n+1}|Y) = Var(Y_{n+1}|Y,X)$$
 (5.20)

$$Var(Y_{n+1}|Y, X) > Var(Y_{n+1}|Y, X, N_{n+1})$$
(5.21)

425 and

$$\operatorname{Var}(X_{n+1}|X) = \operatorname{Var}(X_{n+1}|Y,X)$$
(5.22)

$$Var(X_{n+1}|Y, X) > Var(X_{n+1}|Y, X, Y_{n+1}).$$
(5.23)

When two time series are *contemporaneously* related, the one-step-ahead forecast variance of Y_{n+1} based on Y will not be reduced by including additional information on X. However, when concurrent information X_{n+1} for the variable X is used, the one-step-ahead forecast variance of Y_{n+1} will be reduced. Similarly, the same relationship must also hold true for the one-step-ahead forecast variance of X_{n+1} .

432 3. Unidirectional ($Y \leftarrow X$): There is a *unidirectional relationship* from X to Y if and 433 only if

$$Var(Y_{n+1}|Y) > Var(Y_{n+1}|Y,X)$$
 (5.24)

434 and

$$\operatorname{Var}(X_{n+1}|X) > \operatorname{Var}(X_{n+1}|Y,X).$$
 (5.25)

When *Y* is *unidirectionally* influenced by *X* (i.e., *X* causes *Y*), the one-step-ahead forecast variance of Y_{n+1} based on *Y* will be reduced by including additional information on *X*. However, the one-step-ahead forecast variance of X_{n+1} based on *X* will not be reduced by including additional information on *Y*.

439 4. Feedback ($Y \Leftrightarrow X$): There is a *feedback relationship* between Y and X if and only 440 if

$$Var(Y_{n+1}|Y) > Var(Y_{n+1}|Y,X)$$
 (5.26)

441 and

$$\operatorname{Var}(X_{n+1}|X) > \operatorname{Var}(X_{n+1}|Y,X).$$
 (5.27)

442 When *Y* and *X* have a *feedback* relationship, the one-step-ahead forecast variance 443 of Y_{n+1} based on *Y* will be reduced by including additional information *X*, and 444 similarly, the one-step-ahead forecast variance of X_{n+1} based on *X* will also be 445 reduced by including additional information on *Y*.

119

449

In causality testing, our goal is to determine which dynamic relationship exists 446 between the variables Y and X. Chen and Lee (1990) need the reader to systemati- 447 cally test the following five statistical hypotheses: 448

$$\begin{array}{l} H_1: Y \wedge X; \\ H_2: Y \leftrightarrow X; \\ H_3: Y \not\models X; \\ H_4: Y \not\models X; \\ H_5: Y \Leftrightarrow X. \end{array}$$
(5.28)

The hypotheses H₃ and H₄ are stated in a negative manner.

A number of time series models can be employed for causality testing (see, e.g., 450 Sims 1972; and AGS 1980). Because VARMA models have been shown to be 451 effective in forecasting, this class of models can also be used for causality testing 452 (Chen and Lee 1990). A bivariate VARMA (p, q) model can be generally expressed 453 as 454

$$\left(I - \phi_1 B - \dots - \phi_p B^p\right) \begin{bmatrix} Y_t \\ X_t \end{bmatrix} = C + \left(I - \theta_1 B - \dots = \theta_q B^q\right) \begin{bmatrix} a_{lt} \\ a_{2t} \end{bmatrix}, \quad (5.29)$$

where ϕ_i 's and θ_j 's are 2 × 2 matrices, C is a 2 × 1 constant vector, and $a_t = [a_{1t}, a_{2t}]'$ 455 is a sequence of random shock vectors identically and independently distributed as a 456 normal distribution with zero mean and covariance matrix \sum with $\sum = \begin{bmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{21} & \sigma_{22} \end{bmatrix}$. 457 458

For convenience, the model in (5.29) can be rewritten as

$$\begin{bmatrix} \phi_{11}(B) & \phi_{12}(B) \\ \phi_{21}(B) & \phi_{22}(B) \end{bmatrix} \begin{bmatrix} Y_t \\ X_t \end{bmatrix} = C + \begin{bmatrix} \theta_{11}(B)\theta_{12}(B) \\ \theta_{21}(B)\theta_{22}(B) \end{bmatrix} \begin{bmatrix} a_{1t} \\ a_{2t} \end{bmatrix},$$
(5.30)

where $\phi_{ij}(B) = \phi_{ij0} - \phi_{ij1}B - \phi_{ij2}B^2 - \cdots$, and $\theta_{ij}(B) = \theta_{ij0} - \theta_{ij1}B - 459$ $\theta_{ij2}B^2 - \cdots$. It is important to note that $\phi_{ij0} = \theta_{ij0} = 1$ if i = j, and $\phi_{ij0} = \theta_{ij0}$ 460 = 0 if $i \neq j$.

Assuming that the form of the model in (5.30) is known, sufficient conditions for 462 testing the hypotheses H₁, H₂, H₃, H₄, and H₅ using $\phi_{ii}(B)$ and $\theta_{ii}(B)$ of (5.30) are 463 listed below: 464

Hypothesis Sufficient conditions (constraints)

$\mathrm{H}_1:Y\wedge X$	$\phi_{12}(B) = \phi_{21}(B) = 0,$	$\theta_{12}(B)=\theta_{21}(B)=0,$	$\sigma_{12}=\sigma_{21}=0.$
$\mathrm{H}_2:Y\leftrightarrow X$	$\phi_{12}(B) = \phi_{21}(B) = 0,$	$\theta_{12}(B) = \theta_{21}(B) = 0.$	
$H_3: Y \not\models X$	$\phi_{12}(B) = \theta_{12}(B) = 0.$		
$H_4: Y \not\Rightarrow X$	$\phi_{12}(B) = \theta_{21}(B) = 0.$		
$H_5: Y \Leftrightarrow X$	No constraints.		(53.1)

The conditions in (5.32) become necessary and sufficient conditions if the model 465 in (5.31) is a pure vector AR or a pure vector MA model. In the above hypotheses, 466 H_3 implies that the past X does not help to predict future Y, and H_4 implies that the 467

468 past *Y* does not help to predict *X*. In both situations, we assume σ_{12} to be nonzero. 469 However, if σ_{12} equals to zero, the hypotheses H₃, H₄, and H₅ can be tested under a 470 more stringent condition. Therefore the following three additional hypotheses 471 should also be considered:

HypothesisSufficient conditions (Constraints)
$$H_3^*: Y < \not\models X$$
 $\phi_{12}(B) = \theta_{12}(B) = 0, \sigma_{12} = 0.$ $H_4^*: Y \not\Rightarrow > X$ $\phi_{21}(B) = \theta_{21}(B) = 0,$ $H_5^*: Y < \Leftrightarrow > X$ $\phi_{12} = 0.$

In the above hypotheses, H_3^* implies that both past and concurrent *X* do not help to predict *Y*, and H_4^* implies that both past and concurrent *Y* do not help to predict *X*. For H_5^* , it implies a "true" feedback relationship since *Y* and *X* are not contemporaneously related.

Chen and Lee (1990) proposed a decision tree approach which consists of testing 476 sequence of pair-wise hypotheses that are defined by each of the above а 477 relationships. This inference procedure is based on the principle that a maintained 478 hypothesis should not be rejected unless there is sufficient evidence against it. Two 479 480 procedures for identifying dynamic relationships are considered here: (1) the backward procedure and (2) the forward procedure. The backward procedure 481 takes the position that a hypothesis should not be rejected in favor of a more 482 restrictive one unless sufficient evidence indicates otherwise. Consequently, the 483 statistical procedure starts from the most general hypothesis, H_5 , and then examines 484 the relative validity of competing hypotheses in an increasing order of parameter 485 486 restrictions. On the other hand, the forward procedure asserts that a simpler model is preferred unless the evidence strongly suggests otherwise. Hence, the forward 487 procedure starts its test from the most restrictive hypothesis, H_1 , and moves toward 488 less restrictive hypotheses. In both procedures, each step of the test examines one or 489 two pairs of nested hypotheses. Chen and Lee (1990) state that the forward 490 491 procedure works better (i.e., the test procedure has higher discriminating power) 492 if the variables considered are likely to be independent or have a more restrictive relationship. On the other hand, the backward procedure works better if the 493 variables considered are likely to have more complex relationships. 494

The first step of backward procedure, B1, is to examine two pairs of hypotheses: 496 (a) H_3 versus H_5 and (b) H_4 versus H_5 . This step, distinguishing the feedback 497 relationship from unidirectional relationship, gives rise to four possible outcomes, 498 E_1 to E_4 , as follows:

499 E_1 : H_3 is not rejected in the pair-wise test (a) and H_4 is rejected in the pair-wise 500 test (b).

501 E_2 : H_3 is rejected in test (a) and H_4 is not rejected in test (b).

502 E_3 : H_3 is not rejected in test (a) and H_4 is not rejected in (b).

503 E_4 : H_3 is rejected in test (a) and H_4 is rejected in text (b).

The outcome of E_1 implies that the past information of *Y* may help to predict 504 current *X*, but the past *X* does not help to predict current *Y*. Hence, this outcome 505 leads to the next pair-wise test (g), H_3^* versus H_3 , where we try to detect the 506 contemporaneous effect in the unidirectional relationship. If H_3^* is rejected in test 507 (g), the conclusion, $Y \Rightarrow X$, is reached; otherwise the conclusion, $Y \Rightarrow > X$, would 508 be made. Similarly, the occurrence of events E_2 and E_4 , respectively, suggests a 509 possible unidirectional relationship from *X* to *Y* and a possible feedback relation-510 ship between *Y* and *X*. Therefore, the outcome of E_2 leads to the pair-wise test (h), 511 which helps us to choose between H_4^* and H_4 . Under the outcome of E_4 , it requires 512 the test (i) which discriminates between the strong feedback hypothesis (H_5^*) and the 513 weak feedback hypothesis (H_5). The rejection of H_4^* in test (h) implies $Y \Leftrightarrow X$. 514 Otherwise, the conclusion, $Y < \Leftarrow X$, would be reached. In test (i), the rejection of 515 H_5^* implies $Y \Leftrightarrow X$. If H_5^* is not rejected, we can conclude $Y < \Leftrightarrow > X$.

When one of the events, E_1 , E_2 , and E_4 , occurs in sequence B1, the backward 517 procedure stops at the end of test (g), test (h), and test (i) respectively. If neither H₃ 518 nor H₄ is rejected (i.e., E_3 is realized), the backward procedure will move to 519 sequence B2 where two pairs of hypotheses will be examined: (c) H₂ versus H₃ 520 and (d) H₂ versus H₄. Again, four possible results may come out of this sequence. 521 They are summarized as follows: 522

H_2 is rejected in pair-wise test (c) but is not rejected in test (d). 52	23
H_2 is not rejected in test (c) but is rejected in test (d). 52	24
H_2 is rejected in either test (c) or (d), 52	25
H_2 is rejected in both test (c) and text (d). 52	26
H_2 is not rejected in test (c) but is rejected in test (d).52 H_2 is rejected in either test (c) or (d).52 H_2 is rejected in both test (c) and text (d).52	24 25 26

Since test (c) examines the possibility of $Y \Rightarrow X$ and test (d) examines that of 527 $Y \Leftarrow X$, outcome E_5 implies that the relationship $Y \Rightarrow X$ is more probable than 528 $Y \Leftarrow X$. Therefore, the result of event E_5 leads to test (g). A similar argument 529 suggests that the occurrence of E_6 leads to test (h). A definitive conclusion will be 530 reached at the end of tests (g) and (h). The rejection of H_2 in both test (c) and test (d) 531 indicates the equal possibility of $Y \Leftarrow X$ and $Y \Rightarrow X$. Hence, the result of E_8 calls 532 for test (f): H_2 versus H_5 . If H_2 is rejected at test (f), then the possibility of the 533 feedback relationship is established and the backward procedure moves to test (i). 534 When H_2 is not rejected at test (f) or when event E_7 is realized, the backward 535 procedure then proceeds to test (e), which discriminates between the independency 536 and the contemporaneous relationship. If H_1 is rejected in test (e), the conclusion of 537 $Y \leftrightarrow X$ is reached. Otherwise, $Y \land X$ will be the case. 538

The forward procedure, as illustrated in the previous section, begins by testing 539 the validity of the independency hypothesis at sequence F1. The hypothesis indices, 540 H₁ to H₅, the outcome indices, E₁ to E₈, and the pair-wise test indices, (a) to (h), are 541 consistent. The sequence F1 considers two pairs of hypotheses testing, test (e) and 542 test (j). If h₁ is not rejected in either test, the conclusion of $Y \wedge X$ is reached and the 543 forward procedure stops. Otherwise, the procedure will move forward to sequence 544

545 F2, which examines the relative likelihood of the contemporaneous relationship versus the unidirectional relationship. Notice that sequence F2 is identical to 546 sequence B2, where one of the four possible outcomes, E_5 , E_6 , E_7 , and E_8 , will 547 emerge. Using the same argument on sequence B2, the outcomes of E5 and E6 lead 548 to tests (g) and (h), respectively. A conclusion from one of the four possible 549 unidirectional relationships can be reached as a result and the forward procedure 550 stops. The outcome of E_7 implies $Y \leftrightarrow X$ and stops the forward procedure. How-551 ever, the outcome of E_8 , which rules out the case of a contemporaneous relation-552 ship, leads the forward procedure to sequence F3, which corresponds to sequence 553 B1 in the backward procedure. Tests (a) and (b) may generate one of the four 554 possible outcomes, E1, E2, E3, and E4. Similar to sequence B1 in the backward 555 procedure, the outcomes of E1 and E2 lead to tests (g) and (h), respectively. One of 556 the four unidirectional relationships will be detected as a result and the procedure 557 stops. The outcome of E_4 implies a possible feedback relationship, and a further 558 study, test (i), is needed to identify its nature. When H₅^{*} is rejected in test (i), we 559 conclude $Y \Leftrightarrow X$; otherwise, we conclude $Y \ll X$. The outcome E₃ implies that 560 Y may help to predict X and X may help to predict Y, but the nature of this dynamic 561 relationship is not clear. Therefore, test (f) is needed. When H₂ is not rejected in test 562 (f), the conclusion $Y \leftrightarrow X$ is reached and the procedure stops. If H₂ is rejected in test 563 (f), the procedure moves to test (i) to determine the nature of the feedback 564 relationship. Consequently, either $Y \Leftrightarrow X$ or $Y < \Leftrightarrow > X$ is shown to exist. 565

In practice, the model(s) for the time series under study is unknown. However, the order of the VARMA model for the series can be determined using the model identification procedure discussed. The test procedures are rather robust with respect to the selected model as long as the order of the model is generally correct. Corresponding to each hypothesis, the parameters of the constrained model can be estimated using the maximum likelihood estimation method. The likelihood ratio statistic is then calculated for each pair of hypotheses:

$$LR(H_i vs. H_j) + l(H_i) - l(H_j),$$
 (5.33)

s73 where $l(H_i) = -2^*$ (log of the maximum likelihood value under H_i). The above s74 likelihood ratio statistic follows a χ^2 -distribution with ν degrees of freedom where ν s75 in each test is the difference between the number of estimated parameters under the s76 null (the more restrictive one) and the alternative (the less restrictive one) s77 hypotheses. A chi-square table can then be used to determine the significance of s78 the test statistic for the tested hypotheses.

In each procedure, an *a* significance level will be used in conducting all pairwise tests. Note that this *a* level is not the Type I error probability for the overall performance of the procedures. It serves only as a cutoff point in a sequential decision procedure. The smaller the *a*, the higher is the probability that the more restrictive hypothesis will not be rejected. Hence, taking a smaller *a* is equivalent to favoring the more restrictive hypotheses (i.e., simpler relationships), and taking a 584 larger *a* is equivalent to favoring the more complicated relationships. 585

The above three statistical methods investigate different aspects of a multivariate 586 time series structure. The Sims test detects the dynamic relationship from the 587 reduced autoregressive form, and the VARMA test examines the reduced form of 588 a VARMA structure. The implementation of the Sims test is the easiest of the three 589 and requires the least subjective judgement. While the literature provides a few 590 observations on the relative performance of these three tests, Granger and Newbold 591 (1974) pointed out that the Sims test has a tendency to generate spurious 592 correlations. The Chen and Lee (1990) test begins with a traditional transfer 593 function model estimate shown in Tables 5.3–5.5.

We identify two outliers in the initial merger transfer function model using LEI 595 as the input. The estimation of the Innovational Outlier (IO, a one-time event in the 596 time series) and Level Shift (LS, a permanent change in the time series) outliers 597 reduces the residual standard deviations by about 20 %.⁸ 598

LEI and stock prices are statistically associated with mergers in the Chen and 599 Lee (1990) SCA analysis. 600

One sees the one and two quarter lags in the LEI in the merger transfer function 601 model equation estimate, shown in Table 5.4

	SUMMARY	FOR UNIV	ARIATE T	IME SER	IES MODE	L TFI	M1	
	VARIAB	LE TYP	E OF VARIA	ORIGINA ABLE (L DI DR CENTER	FFERENCING RED		
	DDI	MERGER	RANDOM	ORI	GINAL	NONE		
		DLEI	RANDOM	ORI	GINAL	NONE		
PARAMETER LABEL 1 2 3	VARIABLE NAME DLEI DLEI DDMERGER	NUM./ DENOM. NUM. NUM. D-AR	FACTOR 1 1	ORDER 1 2 1	CONS- TRAINT NONE NONE NONE	VALUE 2.0222 1.8669 - 2787	STD ERROR 1.0804 1.0900 1131	T VALUE 1.87 1.71 -2 46
$\mathbf{\hat{v}}$	EFFECTIV R-SQUARE RESIDUAL (-2)*LOG AIC SIC	E NUMBEF	R OF OBSE RD ERROR. NOOD FUNC	T RVATION TION	NONE 	7 0.29 962069E-0 1134658E+0 126658E+0 .117496E+0	3 4 1 3 3 3	-2.40

t3.2

t3.1

⁸ The SCA outlier estimation using stock prices as the input series is:

One sees the one and two quarter lags in the LEI with estimated outliers in Table $5.5\,$

t4.1 Table 5.4 Summary for univariate time series model-TFM1

	VARIAD	un IIt	VARIA	ABLE	OR CENTER	RED		
	DD:	MERGER	RANDOM	ORI	GINAL	NONE		
		DLEI 	RANDOM	OR]	GINAL	NONE		
PARAMETER LABEL	VARIABLE NAME	NUM./ DENOM.	FACTOR	ORDER	CONS- TRAINT	VALUE	STD ERROR	VAL
1	DLEI	NUM.	1	1	NONE	1.8650	1.0165	1.
2	DLEI	NUM.	1	2	NONE	1.9462	1.0362	1.
3 A	DDMERGER	MA D-AR	1	1	NONE	6603	1284	-3.
	SUMMARY FO	DR UNIVA	RIATE TIN E OF (VARIA	ME SERI ORIGINA	ES MODEL L DI DR CENTEF	UTSMODEI UTSMODEI FFERENCING	3	
		NS	RANDOM	ORI	GINAL	NONE		
PARAMETER LABEL	VARIABLE NAME	NUM./ DENOM.	FACTOR	ORDER	CONS- TRAINT	VALUE	STD ERROR	VAI
	NS	MA	1	1	NONE	6568	.1896	-3.
1	NS	D-AR	1	1	NONE	8621	.1283	-6.
1 2								
1 2	TOTAL NU EFFECTIV RESIDUAL	MBER OF E NUMBER STANDAR	OBSERVAT R OF OBSE RD ERROR.	IONS . RVATIO	NS (74 73).932517E-01		
1 2	TOTAL NU EFFECTIV RESIDUAL	MBER OF E NUMBER STANDAR	OBSERVAI R OF OBSE RD ERROR.		NS (74 73).932517E-01	(0	onti

Table 5.4 (continued)

SUMMARY FOR UNIVARIATE TIME SERIES MODEL -- TFM1 _____ ORIGINAL VARIABLE TYPE OF DIFFERENCING VARIABLE OR CENTERED DDMERGER RANDOM ORIGINAL NONE DLEI RANDOM ORIGINAL NONE _____ _____ _____ PARAMETER VARIABLE NUM./ FACTOR ORDER VALUE STD CONS-Т ERROR VALUE DENOM. TRAINT LABEL NAME DLEI NUM. 1 1 NONE 1.8650 1.0165 1.83 1 2 DLEI NUM. 1 2 NONE 1.9462 1.0362 1.88 .1902 -3.47 .1284 -6.73 3 DDMERGER 1 -.6603 MA 1 NONE DDMERGER D-AR 1 1 NONE -.8640 4 EFFECTIVE NUMBER OF OBSERVATIONS . . R-SQUARE 0.337 RESIDUAL STANDARD ERROR. 0.932355E-01 (-2)*LOG LIKELIHOOD FUNCTION . . . -0.139238E+03 SIC. TO TO -0.0074 0.0929 -0.6789 AUTOCORRELATIONS
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t4.3

t4.2

t5.1

	VARIABL	E TYP	PE OF VAR	ORIGIN. IABLE	AL D OR CENTE	IFFERENCING ERED		
	DDM	ERGER	RANDOM	OR	IGINAL	NONE		
	נס	LEI	RANDOM	ORI	IGINAL	NONE		
PARAMETER LABEL	VARIABLE NAME	NUM./ DENOM.	FACTOR	ORDER	CONS- TRAINT	VALUE	STD ERROR	T VALU
1	DLEI	NUM.	1	1	NONE	3.3055	.8470	3.9
2	DLEI	NUM.	1	2	NONE	1.1306	.8511	1.3
3	DDMERGER	MA	1	1	NONE	.3947	.2720	1.4
4	DDMERGER	D-AR	T	Т	NONE	0032	. 3027	0
	SUMMAI	RY OF C	UTLIER 1	DETECTIO	ON AND AI	OJUSTMENT		
		rime	ESTIMA	TE T-V	/ALUE	TYPE		
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		J4 	-0.03		4.01			
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TOTAL N EFFECTI RESIDUA: RESIDUA:	UMBER OF OB: VE NUMBER OI L STANDARD I L STANDARD I SUM	SERVATI F OBSER ERROR (ERROR (MMARY F VARIABI DDMI DSF	ONS VATIONS WITHOUT WITH OUT OOR UNIV/ COR UNIV/ COR UNIV/ VARIAB ERGER R 2500 R	OUTLIEF TLIER AI OF ORIC LE OR C ANDOM	ADJUST DJUSTMEN ME SERIES BINAL D ENTERED ORIGINA ORIGINA	MENT). 0.1 MENT). 0.1 SMODEL TFM IFFERENCING L NONE L NONE	103580E+(784829E-(11	76 73 00 01
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t5.2

Let us move to a final Chen and Lee (1990) merger model estimation. The final form of the mergers and LEI analysis with the CCCF and CCM analysis is shown in Table 5.6.
	VARIABL	E TYP	E OF (VARIA	ORIGINA BLE (L DI DR CENTE	FFERENCING		
	DDMERGER RANDOM ORIGINAL		GINAL	NONE				
	D	LEI	RANDOM	ORI	GINAL	NONE		
PARAMETER LABEL	VARIABLE NAME	NUM./ DENOM.	FACTOR	ORDER	CONS- TRAINT	VALUE	STD ERROR	T VALUE
1 2	DLEI DLEI	NUM. NUM.	1 1	1 2	NONE NONE	3.3055 1.1306	.8470	3.90 1.33
3	DDMERGER DDMERGER	MA D-AR	1 1	1	NONE NONE	0052	.2720	1.45 02
SUMMARY OF OUTLIER DETECTION AND ADJUSTMENT								
		TIME	ESTIMATH	E T-V	ALUE	TYPE	\mathbf{O}	
		12 16	0.115 0.398	3	8.68 5.29	TC IO		
		18	0.183	2	2.97	IO		
		29 36	-0.028	-4	1.56	LS		
		42	-0.167	-2	2.70	IO		
		67 73	-0.151	-2	2.43	IO		
MAXIMUM NUMBER OF OUTLIERS IS REACHED ** THE OUTLIER(S) AFTER TIME PERIOD 71 OCCURS WITHIN THE LAST FIVE OBSERVATIONS OF THE SERIES. THE IDENTIFIED TYPE ANS THE ESTIMATE OF THE OUTLIER(S) MAY NOT BE RELIABLE								
TOTAL NUMBER OF OBSERVATIONS. 76 EFFECTIVE NUMBER OF OBSERVATIONS. 73 RESIDUAL STANDARD ERROR (WITHOUT OUTLIER ADJUSTMENT). 0.103580E+00 RESIDUAL STANDARD ERROR (WITH OUTLIER ADJUSTMENT). 0.610908E-01								
	SERIES	NAME		MEAN	S	TD. ERROR		
	12	DDME DLEI	RGER	0.0)268)075	0.1145 0.0112		
NOTE: THE APPROX. STD. ERROR FOR THE ESTIMATED CORRELATIONS BELOW IS (1/NOBE**.5) = 0.11471								
SAMPLE CORRELATION MATRIX OF THE SERIES								
1.00 0.26 1.00								
SUMMARIES OF CROSS CORRELATION MATRICES USING +,-,., WHERE + DENOTES A VALUE GREATER THAN 2/SQRT(NOBE) - DENOTES A VALUE LESS THAN -2/SQRT(NOBE) . DENOTES A NON-SIGNIFICANT VALUE BASED ON THE ABOVE CRITERION								

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

1 2 1 .+.+..... ++.... 1 . 2 ++....-2 . CROSS CORRELATION MATRICES IN TERMS OF +, -, . LAGS 1 THROUGH 6 . + + + • • + . . + . + LAGS 7 THROUGH 12 LAGS 13 THROUGH 18 LAGS 19 THROUGH 24 . . STEPAR VARIABLES ARE ddmerger, dLEI . @ ARFITS ARE 1 to 6. rccm 1 to 6 TIME PERIOD ANALYZED 1 TO EFFECTIVE NUMBER OF OBSERVATIONS (NOBE). . . 76 76 SERIES NAME MEAN STD. ERROR DDMERGER 0.0268 0.1145 1 2 DLEI 0.0075 0.0112 NOTE: THE APPROX. STD. ERROR FOR THE ESTIMATED CORRELATIONS BELOW IS $(1/NOBE^{**}.5) = 0.11471$ SAMPLE CORRELATION MATRIX OF THE SERIES 1.00 0.26 1.00

SUMMARIES OF CROSS CORRELATION MATRICES USING +,-,., WHERE + DENOTES A VALUE GREATER THAN 2/SQRT(NOBE) - DENOTES A VALUE LESS THAN -2/SQRT(NOBE) . DENOTES A NON-SIGNIFICANT VALUE BASED ON THE ABOVE CRITERION

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

1 2 1 .+.+.+.... ++.... 1 . 2 ++....-. 2 . CROSS CORRELATION MATRICES IN TERMS OF LAGS 1 THROUGH 6 . + + . . + + LAGS 7 THROUGH 12 • LAGS 13 THROUGH 18 LAGS 19 THROUGH 24 DETERMINANT OF S(0) = 0.146494E-05NOTE: S(0) IS THE SAMPLE COVARIANCE MATRIX OF W(MAXLAG+1),...,W(NOBE) AUTOREGRESSIVE FITTING ON LAG(S) 1 SUMMARIES OF CROSS CORRELATION MATRICES USING +,-,., WHERE + DENOTES A VALUE GREATER THAN 2/SQRT(NOBE) - DENOTES A VALUE LESS THAN -2/SQRT(NOBE) . DENOTES A NON-SIGNIFICANT VALUE BASED ON THE ABOVE CRITERION

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

	1	2	
1 .+ 1	.+ 	++	
2 2			<u>k</u>
CROSS CORRELA	TION MATRICES	IN TERMS OF +	
-	LAGS 1 THROUG	Н 6	
+ +		+	
:	LAGS 7 THROUG	H 12	
· · · · +			
	XX)	
	LAGS 13 THROUG	H 18	
		• • • •	• •
	LAGS 19 THROUG	н 24	
		· · · · · ·	
AUTOREGRES	SIVE FITTING O	N LAG(S) 1	2
SUMMARIES OF CROSS CO + DENOTES A	JKKELATION MAT A VALUE GREATE	RICES USING 4 R THAN 2/SORI	-,-,., WHERE C(NOBE)
- DENOTES	A VALUE LESS	THAN -2/SQRT	(NOBE)
. DENOTES A NON-SIGN	IFICANT VALUE	BASED ON THE	ABOVE CRITERION

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Table 5.6 (continued)

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

1 2
1+ 1
² / ₂
CROSS CORRELATION MATRICES IN TERMS OF +,-,.
LAGS 1 THROUGH 6
LAGS 7 THROUGH 12
+
· · · · · · · · · · · · · · · · · · ·
LAGS 13 THROUGH 18
LAGS 19 THROUGH 24
AUTOREGRESSIVE FITTING ON LAG(S) I 2 3
SUMMARIES OF CROSS CORRELATION MATRICES USING $+, -, .$, WHERE
- DENOTES A VALUE GREATER THAN 2/SQRT(NOBE)
. DENOTES A NON-SIGNIFICANT VALUE BASED ON THE ABOVE CRITERION

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

1 2
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
2 2
CROSS CORRELATION MATRICES IN TERMS OF +, -, .
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
LAGS 7 THROUGH 12
LAGS 13 THROUGH 18
LAGS 19 THROUGH 24
AUTOREGRESSIVE FITTING ON LAG(S) 1 2 3 4
SUMMARIES OF CROSS CORRELATION MATRICES USING +,-,., WHERE + DENOTES A VALUE GREATER THAN 2/SQRT(NOBE) - DENOTES A VALUE LESS THAN -2/SQRT(NOBE)
. DENOTES A NON-SIGNIFICANT VALUE BASED ON THE ABOVE CRITERION

133

Table 5.6 (continued)

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

1 2
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
2
CROSS CORRELATION MATRICES IN TERMS OF +,-,.
LAGS 7 THROUGH 12
LAGS 13 THROUGH 18
LAGS 19 THROUGH 24
AUTOREGRESSIVE FITTING ON LAG(S) 1 2 3 4 5
SUMMARIES OF CROSS CORRELATION MATRICES USING +,-,., WHERE + DENOTES A VALUE GREATER THAN 2/SQRT(NOBE)
- DENOTES A VALUE LESS THAN -2/SQRT(NOBE) . DENOTES A NON-SIGNIFICANT VALUE BASED ON THE ABOVE CRITERION

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

1 2
1 1
² / ₂
CROSS CORRELATION MATRICES IN TERMS OF +,-,.
LAGS 1 THROUGH 6
LAGS 7 THROUGH 12
<u>-</u>
· · · · · · · · · · · · · · · · · · ·
LAGS 13 THROUGH 18
LAGS 19 THROUGH 24
AUTOREGRESSIVE FITTING ON LAG(S) 1 2 3 4 5 6
SUMMARIES OF CROSS CORRELATION MATRICES USING +,-,., WHERE + DENOTES A VALUE GREATER THAN 2/SQRT(NOBE)
- DENOTES A VALUE LESS THAN -2/SQRT(NOBE) . DENOTES A NON-SIGNIFICANT VALUE BASED ON THE ABOVE CRITERIOI

BEHAVIOR OF VALUES IN (I,J)TH POSITION OF CROSS CORRELATION MATRIX OVER ALL OUTPUTTED LAGS WHEN SERIES J LAGS SERIES I

			1		2		
	1 . 1 .		 				
	2.	•••••					
CROSS	CORREI	LATION	MATRICE	S IN TERM	IS OF +,-,		
		LAGS	1 THRO	UGH 6			
 			· · · ·	· · · ·			
		LAGS	7 THRC	UGH 12	\mathbf{O}		
 		•	· · · ·	· · · ·	• :	· · · ·	
		LAGS	13 THRC	UGH 18			
· · · ·		•			· · · ·	· · ·	
		LAGS	19 THRC	UGH 24			
 	Ċ	(C	- · · ·	••• •••	· · · ·	•••	
C	9					(conti	nued)

======= STEPWISE AUTOREGRESSION SUMMARY ========					
I RESIDUAL I EIGENVAL.I CHI-SQ I I SIGNIFICANCE LAG I VARIANCESI OF SIGMA I TEST I AIC I OF PARTIAL AR COEFF.					
1 I .105E-01 I .981E-04 I 23.68 I -13.684 I - + I .101E-03 I .105E-01 I I I . +					
2 I .896E-02 I .974E-04 I 10.42 I -13.741 I . + I .998E-04 I .897E-02 I I I					
3 I .870E-02 I .915E-04 I 5.78 I -13.728 I . I .944E-04 I .870E-02 I I I .					
4 I .737E-02 I .904E-04 I 10.74 I -13.800 I + . I .941E-04 I .737E-02 I I I I .					
5 I .735E-02 I .901E-04 I .29 I -13.700 I I .939E-04 I .736E-02 I I I					
6 I .726E-02 I .896E-04 I 1.05 I -13.613 I I .931E-04 I .726E-02 I I I					
NOTE: CHI-SQUARED CRITICAL VALUES WITH 4 DEGREES OF FREEDOM ARE 5 PERCENT: 9.5 1 PERCENT: 13.3 NOTE: THE PARTIAL AUTOREGRESSION COEFFICIENT MATRIX FOR LAG L IS THE ESTIMATED PHI(L) FROM THE FIT WHERE THE MAXIMUM LAG USED IS L (I.E. THE LAST COEFFICIENT MATRIX). THE ELEMENTS ARE STANDARDIZED BY DIVIDING EACH BY ITS STANDARD ERROR. MTSMODEL ARMA11. SERIES ARE ddmerger, dLEI. 0 MODEL IS (1-PHI*B)SERIES=C+(1-TH1*B)NOISE. SUMMARY FOR MULTIVARIATE ARMA MODEL ARMA11 VARIABLE DIFFERENCING					
VARIABLE DIFFERENCING DDMERGER					
DLEI PARAMETER FACTOR ORDER CONSTRAINT					

1	С	CONSTANT	0	CC
2	PHI	REG AR	1	CPHI
3	TH1	REG MA	1	CTH1

CAUSALTEST MODEL ARMA11. OUTPUT PRINT(CORR). alpha .01

SUMMARY OF THE TIME SERIES SERIES MEAN STD DEV DIFFERENCE ORDER(S) NAME 0.0268 DDMERGER 0.1145 1 0.0075 2 DLEI 0.0112 _____ ERROR COVARIANCE MATRIX 1 2 1 .011543 .000136 2 .000306 ITERATIONS TERMINATED DUE TO: CHANGE IN (-2*LOG LIKELIHOOD)/NOBE .LE. 0.100E-03 TOTAL NUMBER OF ITERATIONS IS 10 MODEL SUMMARY WITH MAXIMUM LIKELIHOOD PARAMETER ESTIMATES ---- CONSTANT VECTOR (STD ERROR) ----0.045 (0.024) 0.004 (0.002) ----- PHI MATRICES -----ESTIMATES OF PHI(1) MATRIX AND SIGNIFICANCE -.280 10.149 • + .004 .472 . + STANDARD ERRORS .243 3.027 .017 .230 THETA MATRICES -----ESTIMATES OF THETA(1) MATRIX AND SIGNIFICANCE -.050 8.230 -.011 .073 · + STANDARD ERRORS 3.218 .263 .018 .246 _____ ERROR COVARIANCE MATRIX 1 2 .008643 .000143 .000100 1 2

==== SUMM	ARY OF FINAL PARAMETER ESTIMATES &	AND THEIR STANDARD E	IRRORS
==== PARAMETER NUMBER	PARAMETER DESCRIPTION	FINAL ESTIMATE	ESTIMATED STD. ERROR
1 2 3 4 5 6 7 8 9 10	CONSTANT (1) CONSTANT (2) AUTOREGRESSIVE (1, 1, 1) AUTOREGRESSIVE (1, 1, 2) AUTOREGRESSIVE (1, 2, 1) AUTOREGRESSIVE (1, 2, 1) MOVING AVERAGE (1, 1, 1) MOVING AVERAGE (1, 1, 2) MOVING AVERAGE (1, 2, 1) MOVING AVERAGE (1, 2, 2) CORRELATION MATRIX OF THI	-0.045279 0.003729 -0.280315 10.149337 0.003976 0.471517 -0.049937 8.230138 -0.010919 0.073078 	0.023810 0.001855 0.243195 3.027162 0.016524 0.229912 0.262984 3.217553 0.018313 0.245583
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6 7 8 9 00 1.00) 10
10	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$) 1.00 3 1.00
ALL EI -2*(LOG T	THE RESIDUAL COVARIANCE MATRIX IS JEMENTS IN THE MATRIX PARAMETERS A LIKELIHOOD AT FINAL ESTIMATES UNI HE RESIDUAL COVARIANCE MATRIX IS 3 DURING IN THE MATRIX ESTIMATES	S SET TO FULL MATRIX RE ALLOWED TO BE ES DER H5) IS -0.8983 SET TO DIAGONAL MATH	K TIMATED 30741E+03 RIX
-2* (LOG THE -2* (LOG	LIKELIHOOD AT FINAL ESTIMATES UNI THE RESIDUAL COVARIANCE MATRIX IS (2,1)TH ELEMENTS IN THE MATRIX PA LIKELIHOOD AT FINAL ESTIMATES UNI	DER H5*) IS -0.896 S SET TO FULL MATRIX RAMETERS ARE SET TO DER H4) IS -0.896	55939E+03 ZERO 59059E+03
THE -2* (LOG	(2,1) TH ELEMENTS IN THE MATRIX PA LIKELIHOOD AT FINAL ESTIMATES UNI	RAMETERS ARE SET TO DER H4*) IS -0.8953	ZERO 37550E+03
THE -2* (LOG T THE -2* (LOG	<pre>(1,2)TH ELEMENTS IN THE MATRIX PA LIKELIHOOD AT FINAL ESTIMATES UNI HE RESIDUAL COVARIANCE MATRIX IS S (1,2)TH ELEMENTS IN THE MATRIX PA LIKELIHOOD AT FINAL ESTIMATES UNI</pre>	RAMETERS ARE SET TO DER H3) IS -0.878(SET TO DIAGONAL MATH RAMETERS ARE SET TO DER H3*) IS -0.8771	ZERO 54498E+03 RIX ZERO L4380E+03
THE THE -2*(LOG	THE RESIDUAL COVARIANCE MATRIX IS (2,1)TH ELEMENTS IN THE MATRIX PA (1,2)TH ELEMENTS IN THE MATRIX PA LIKELIHOOD AT FINAL ESTIMATES UNIT	S SET TO FULL MATRIX RAMETERS ARE SET TO RAMETERS ARE SET TO DER H2) IS -0.8775	X ZERO ZERO 54552E+03
T THE THE -2*(LOG	HE RESIDUAL COVARIANCE MATRIX IS ((2,1)TH ELEMENTS IN THE MATRIX PA (1,2)TH ELEMENTS IN THE MATRIX PA LIKELIHOOD AT FINAL ESTIMATES UNI	SET TO DIAGONAL MATH RAMETERS ARE SET TO RAMETERS ARE SET TO DER H1) IS -0.8763	RIX ZERO ZERO 34247E+03
RESULT	BASED ON THE BACKWARD PROCEDURE DDMERGER <<= DLEI (Y IS STR BASED ON THE FORWARD PROCEDURE	(Y:DDMERGER, X: DI ONGLY CAUSED BY X) (Y:DDMERGER, X: DI	LEI) LEI)
	DDMERGER <<= DLEI (Y IS STR	ONGLY CAUSED BY X)	

t6.2

Table 5.7 The money supply and stock prices, 1967–2011

PARAMETER	VARIABLE	NUM./	FACTOR	ORDER	CONS-	VALUE	STD	Т
LABEL	NAME	DENOM.			TRAINT		ERROR	VALUE
1	MSIM1P	NUM.	1	1	NONE	5574	.2845	-1.96
2	MSIM1P	NUM.	1	2	NONE	.0890	.2643	.34
3	MSIM1P	NUM.	1	3	NONE	.1484	.2641	.56
4	MSIM1P	NUM.	1	4	NONE	1.0079	.2837	3.55
5	SP500	D-AR	1	1	NONE	.2728	.0414	6.58
	EFFECTIV	E NUMBER	OF OBSE	RVATION	s	540		
	R-SQUARE					0.081		
	RESIDUAL	STANDAF	D ERROR.			0.357160E-01		
sfer func	tion res	iduals	are w	hite	noise	(random),	as il	lustrate

The transfer function residuals are white noise (random), as illustrated by the autocorrelation function of the residuals (ACF RES).

(continued)

The Chen and Lee (1990) test finds that LEI strongly cause mergers during the 1992–2011 period. Moreover, the Chen and Lee (1990) test finds that stock prices cause mergers during the 1992–2011 period.⁹

Money Supply and Stock Prices, 1967–2011

We examine the causal relationship between the money supply (M1P) and stock prices, as measured by the S&P 500 during the 1967.01–2011.04 period. Thomakos and Guerard (2004) and Ashley (2004) found that the money supply passed the AGS (1980) causality test and the Ashley post-sample criteria test (2004). We obtain M1P and S&P 500 monthly data from the St. Louis Federal Reserve economic database (FRED).¹⁰ Both series have a difference in the logarithmic process; i.e., the series are dlog-transformed. We use SCA and the Chen and Lee (1990) test for the money supply and stock returns series. There is a four-month lag in the (positive) effect of the money supply on stock prices (and returns), see Table 5.7.

139

t7.1

AU7

⁹ Had one modeled stock prices and mergers for the 1979–2011 period, one finds only a contemporaneous relationship and no strong causality findings.

¹⁰ We use M1P, a variation on M1, rather than M3, that was used in the earlier studies because M3 was discontinued in the FRED database.

ACF RES

NAME OF THE SERIESRESMEAN OF THE (DIFFERENCED) SERIES0.0011STANDARD DEVIATION OF THE SERIES0.0355T-VALUE OF MEAN (AGAINST ZERO)0.6960

AUTOCORRELATIONS

 1-12
 -.01 -.00
 .04
 .01
 .08 -.07 -.04
 .05 -.01 -.02
 .06 -.02

 ST.E.
 .04
 .04
 .04
 .04
 .04
 .04
 .04
 .04
 .04

 Q
 .0
 .0
 .8
 .9
 4.6
 7.4
 8.1
 9.7
 10.0
 11.9
 12.1

-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0

	Ι
1 -0.01	+ I +
2 0.00	+ I +
3 0.04	+ IX+
4 0.01	+ I +
5 0.08	+ IXX
6 -0.07	XXI +
7 -0.04	+XI +
8 0.05	+ IX+
9 -0.01	+ I +
10 -0.02	+XI +
11 0.06	+ IX+
12 -0.02	+ I +
13 0.01	+ I +
14 -0.04	+XI +
15 -0.04	+XI +
16 0.07	+ IXX
17 -0.05	+XI +
18 0.03	+ IX+
19 0.00	+ I +
20 -0.06	+XI +
21 -0.08	XXI +
22 -0.01	+ I +
23 -0.03	+XI +
24 -0.03	+XI +

t7.2

	VARIABI	LE TYPE	OF ORIGI	NAL DI	FFERENCI	NG		
		VARIA	BLE OR O	ENTERE	C			
	SP	500 RAN	IDOM OI	RIGINAL	NONE			
	MSI	M1P RAN	IDOM OF	RIGINAL	NONE			
PARAMETER	VARIABLE	NUM./	FACTOR	ORDER	CONS-	VALUE	STD	Т
LABEL	NAME	DENOM.			TRAINT		ERROR	VALUE
1	MSIM1P	NUM.	1	1	NONE	.0180	.2289	.08
2	MSIM1P	NUM.	1	2	NONE	.0548	.2140	.26
3	MSIM1P	NUM.	1	3	NONE	.0884	.2137	.41
4	MSIM1P	NUM.	1	4	NONE	.6230	.2282	2.73
5	SP500	MA	1	1	NONE	2144	.0429	-5.00
	CUDALA	DVODOU		DOTION				

SUMMARY OF OUTLIER DETECTION AND ADJUSTMENT

TIME ESTIMATE T-VALUE TYPE

				-
4	10	-0.120	-4.33	AO
8	32	-0.074	-3.21	тс
Ç) 0	-0.097	-4.15	тс
ç	96	0.107	4.62	тс
1	08	0.087	3.06	Ю
1	58	-0.105	-3.67	ю
1	76	-0.090	-3.23	AO
1	88	0.104	4.50	тс
2	49	-0.100	-4.35	тс
2	83	-0.086	-3.03	ю
2	89	0.111	3.88	ю
3	64	0.082	3.54	тс
3	79	-0.087	-3.04	ю
3	82	0.080	3.46	тс
4	10 ·	0.090	-3.15	10
4	16 -	0.123	-4.43	AO
4	26 -	0.110	-3.95	AO
5	01 ·	0.219	-7.70	ΙΟ
5	07	0.093	4.04	тс
5	35 -	0.123	-4.33	IO
TOTAL NUMBER OF OBSERVAT	IONS		545	-

RESIDUAL STANDARD ERROR (WITHOUT OUTLIER ADJUSTMENT). . 0.358532E-01

RESIDUAL STANDARD ERROR (WITH OUTLIER ADJUSTMENT) ... 0.284839E-01

t8.2

We find significant outliers in the money supply and stock returns series estimates, see Table 5.8.

The estimation of outliers reduces the residual standard error by approximately 20 %.

However, the Chen and Lee (1990) test does not report that the money supply causes stock prices,

RESULT BASED ON THE BACKWARD PROCEDURE (Y:SP500, X:MSIM1P) SP500 =>> MSIM1P (Y STRONGLY CAUSES X)

RESULT BASED ON THE FORWARD PROCEDURE (Y:SP500, X:MSIM1P) SP500 ^ MSIM1P (Y IS INDEPENDENT OF X)

but rather that stock prices (returns) cause the money supply and that stock prices are independent of the money supply.

In this chapter, we fit univariate and bivariate time series models in the tradition of Box and Jenkins (1976) and Granger and Newbold (1977) and apply traditional Granger causality testing following the Ashley et al. (1980) methodology and the Vector Autoregressive Models (VAR) and Chen and Lee (1990) VARMA causality test. We test two series for causality: (1) stock prices and mergers and (2) the money supply and stock prices. We find mixed results on Granger causality testing models.

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Chapter 6 A Case Study of Portfolio Construction Using the USER Data and the Barra **Aegis System**

In this chapter, we estimate a set of monthly regression models to create monthly 5 expected returns and demonstrate the effectiveness of the Barra Aegis system. The 6 Aegis system creates and tests investment management strategies, producing 7 portfolios and attributing portfolio returns according to the Barra multifactor risk 8 model. We find support with the Barra Aegis for the composite modeling, the 9 United States Expected Returns (USER), developed and estimated in Chap. 4, 10 using fundamental, expectations, and momentum-based data for the US equities 11 during the December 1979–December 2009 period. To measure risk, one can vary 12 the period of volatility calculation, such as using 5 years of monthly data in 13 calculating the covariance matrix, as was done in Bloch et al. (1993), or 1 year of 14 daily returns to calculate a covariance matrix, as was done in Guerard et al. (1993), 15 AU1 or 2-5 years of data to calculate factor returns as in the Barra system, discussed in 16 Menchero et al. (2010). The Capital Asset Pricing Model, the CAPM, holds that the 17 return to a security is a function of the security beta: 18

$$R_{jt} = R_{\rm F} + \beta_j [E(R_{\rm Mt}) - R_F] + e_{jt}, \qquad (6.1)$$

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where R_{jt} is expected security return at time *t*; *E* (R_{Mt}), expected return on the market at time *t*; R_F , risk-free rate; β_j , security beta, a random regression coefficient; and e_{it} , randomly distributed error term.¹

Let us estimate beta coefficients to be used in the CAPM to determine the rate of 22 return on equity. One can fit a regression line of monthly holding period returns 23 (HPRs) against the excess returns of an index such as the value-weighted Center for 24 Research in Security Prices (CRSP) index, which is an index of all publicly traded 25 stocks. Most stock betas are estimated using 5 years of monthly data, some sixty 26 observations, although one can use almost any number of observations.² One 27 generally needs at least thirty observations for normality of residuals to occur. 28 One can use the Standard & Poor's 500 Index, or the Dow Jones Industrial Index 29 30 (DJIA), or many other stock indexes.

Empirical tests of the CAPM often resulted in unsatisfactory results. That is, the 31 average estimated market risk premium was too small, relative to the theoretical 32 market risk premium and the average estimated risk-free rate exceeded the known 33 34 risk-free rate. Thus low-beta stocks appeared to earn more than was expected and high-beta stocks appeared to earn less than was expected (Black et al. (1972)). The 35 36 equity world appeared more risk-neutral than one would have expected during the 1931–1965 period. There could be many issues with estimating betas using ordinary 37 least squares. Roll (1969, 1977) and Sharpe (1971) identified and tested several 38 issues with beta estimations. Bill Sharpe estimated characteristic lines, the line of 39

40 stock or mutual fund return versus the market return, using ordinary least squares

41 (OLS) and the mean absolute deviation (MAD) for the 30 stocks of the Dow Jones

42 Industrial Average stocks versus the Standard and Poor's 425 Index (S&P 425) for

the 1965–1970 period and 30 randomly selected mutual funds over the 1964–1970

period versus the S&P 425. Sharpe found little difference in the OLS and MAD
betas, and concluded that the MAD estimation gains may be "relatively modest."

¹ The CAPM beta, its measure of systematic risk, from the Capital Market Line equilibrium condition, in an alternative formulation:

Ē

$$\beta_j = \frac{\text{Cov}(R_j, R_M)}{\text{Var}(R_M)}$$
(6.2)

$$E(R_j) = R_F + \left[\frac{E(R_M) - R_F}{\sigma_M^2}\right] \operatorname{Cov}(R_j, R_M)$$
$$= R_F + \left[E(R_M) - R_F\right] \frac{\operatorname{Cov}(R_j, R_M)}{\operatorname{Var}(R_M)}$$

$$E(R_j) = R_{\rm F} + [E(R_{\rm M}) - R_{\rm F}]\beta_j.$$
 (6.3)

Equation (6.3) defines the Security Market Line, (SML), which describes the linear relationship between the security's return and its systematic risk, as measured by beta.

² Standard &Poor's, *The Stock Market Encyclopedia*, uses 5 years on monthly data to estimate beta coefficients.

AU1,2

The difficulty of measuring beta and its corresponding SML gave rise to extra- 46 market measures of risk, found in the work of King (1966), Farrell (1973), 47 Rosenberg (1973, 1976, 1979), Stone (1974, 2002), Ross (1976), Ross and Roll 48 (1980), Blin and Bender (1995), and Blin et al. (1998) and culminated in the 49 AU4 creation of the MSCI Barra and Sungard APT portfolio creation and management 50 systems. We highlight the Barra Aegis system in this analysis. The Barra risk model 51 was developed in the series of studies by Rosenberg and completely discussed in 52 Rudd and Clasing (1982) and Grinhold and Kahn (2000). The extra-market risk 53 measures are a seemingly endless source of discussion, debate, and often frustration 54 among investment managers. Farrell (1974, 1997) estimated a four-"factor" extra- 55 AU5 market model. Farrell took an initial universe of 100 stocks in 1974 (due to 56 AU6 computer limitations), and ran market models for each stock to estimate betas and 57 residuals from the market model: 58

$$R_{j_{t}} = a_{j} + b_{j}R_{M_{t}} + e_{j}$$

$$e_{j_{t}} = R_{j_{t}} - \hat{a}_{j} - \hat{b}_{j}R_{M_{T}}.$$
(6.4)
(6.5)

The residuals of (6.5) should be independent variables, if one factor (the market) 59 is sufficient for modeling security returns. That is, after removing the market impact 60 by estimating a beta, Farrell hypothesized that the residual of IBM should be 61 independent of Dow, Merck, or Dominion Resources. The residuals should be 62 independent, of course, with the market, in theory. The expected returns should 63 be priced by only the beta. Farrell (1974) examined the correlations among the 64 security residuals of (6.9) and found that the residuals of IBM and Merck were 65 highly correlated, but the residuals of IBM and D (then Virginia Electric & Power) 66 were not correlated. Farrell used a statistical technique known as Cluster Analysis 67 to create clusters, or groups, of securities, having highly correlated market model 68 residuals. Farrell found four clusters of securities based on his extra-market covari- 69 ance. The clusters contained securities with highly correlated residuals that were 70 uncorrelated with residuals of securities in the other clusters. Farrell referred to his 71 clusters as "Growth Stocks" (electronics, office equipment, drug, hospital supply 72 firms, and firms with above-average earnings growth), "Cyclical Stocks" (Metals, 73 machinery, building supplies, general industrial firms, and other companies with 74 above-average exposure to the business cycle), "Stable Stocks" (banks, utilities, 75 retailers, and firms with below-average exposure to the business cycle), and 76 "Energy Stocks" (coal, crude oil, and domestic and international oil firms). 77

Bernell Stone (1974) developed a two-factor index model which modeled equity 78 AUT returns as a function of an equity index and long-term debt returns. Both equity and 79 debt returns had significant betas. In recent years, Stone and Guerard (2010a, b) 80 have developed a portfolio algorithm to generate portfolios that have similar stock 81 betas (systematic risk), market capitalizations, dividend yield, and sales growth 82 cross sections, such that one can access the excess returns of the analysts' forecasts, 83 forecast revisions, and breadth model, as one moves from low (least preferred) to 84 high (most preferred) securities with regard to his or her portfolio construction 85

variable (i.e., CTEF or a composite model of value and analysts' forecasting 86 factors). In the Stone and Guerard (2010a) work, the ranking on forecasted return 87 and grouping into fractile portfolios produce a set of portfolios ordered on the basis 88 of predicted return score. This return cross section will almost certainly have a wide 89 range of forecasted return values. However, each portfolio in the cross section will 90 almost never have the same average values as that of the control variables. To 91 produce a cross-sectional match on any of the control variables, we must reassign 92 stocks. For instance, if we were trying to make each portfolio in the cross section 93 that has the same average beta value, we could move a stock with an above-average 94 95 beta value into a portfolio whose average beta value is below the population average. At the same time, we could shift a stock with a below-average beta value into 96 97 the above-average portfolio from the below-average portfolio. The reassignment problem can be formulated as a mathematical assignment program (MAP). Using 98 the MAP produces a cross-sectional match on beta or any other risk control 99 variable. All (fractile) portfolios should have explanatory controls equal to their 100 population average value. 101

In 1976, Ross published his "Arbitrage Theory of Capital Asset Pricing," which held that security returns were a function of several (4–5) economic factors. Ross and Roll (1980) empirically substantiated the need for 4–5 factors to describe the return generating process. In 1986, Chen, Ross, and Roll (CRR) developed an estimated multifactor security return model based on

$$R = a + b_{\rm MP} \,\mathrm{MP} + b_{\rm DEI} \,\mathrm{DEI} + b_{\rm UI} \,\mathrm{UI} + b_{\rm UPR} \,\mathrm{UPR} + b_{\rm UTS} \,\mathrm{UTS} \,te_t, \tag{6.6}$$

where MP is monthly growth rate of industrial production; DEI, change in expected
inflation; UI, unexpected inflation; UPR, risk premium; and UTS, term structure of
interest rates.

CRR defined unexpected inflation as the monthly (first) differences of the 110 Consumer Price Index (CIP) less the expected inflation rate. The risk premia variable 111 is the "Baa and under" bond return at time and less the long-term government bond 112 return. The term structure variable is the long-term government bond return less the 113 Treasury bill rates, known at time t - 1, and applied to time t. When CRR applied 114 115 their five-factor model in conjunction with the value-weighted index betas, during the 1958–1984 period, the index betas are not statistically significant whereas the 116 economic variables are statistically significant. The Stone, Farrell, and CRR multi-117 factor model used 4-5 factors to describe equity security risk. The models used 118

119 different statistical approaches and economic models to control for risk.

120 The BARRA Model: The Primary Institutional Risk Model

121 As discussed previously, the most frequent approach for the prediction of risk is to 122 use historical price behavior in the estimation of beta. Beta was defined as the 123 sensitivity of the expected excess rate of return on the stock to the expected excess AU8

AU9

rate of return on the market portfolio. Unfortunately, the word *expected* has been 124 used, and no good records of aggregate expectations exist. Thus, a major assump- 125 tion has to be made to enable average (realized) rates of return to be used in place of 126 expected rates of return, which, in turn, permits us to use the slope of regression line 127 (estimated from realized data) to form the basis for a prediction of beta. 128

If this assumption, which essentially states that the future is going to be similar to 129 the "average past," is made, then the estimation of historical beta proceeds as 130 follows. Choose a suitable number of periods for which the excess returns of the 131 security and market portfolio proxy are known. There is a subtle trade-off here. 132 When more data points are used, the accuracy of the estimation procedure is 133 improved, provided the relationship being estimated does not change. Usually the 134 relationship does change; therefore, a small number of most recent data points is 135 preferred so that dated information will not obscure the current relationship. It is 136 usually accepted that a happy medium is achieved by using 60 monthly returns.³ 137 The security series is then regressed against the market portfolio series. This 138 provides an estimate of beta (which is equivalent to the slope of the characteristic 139 line) and the residual variance. 140

Menchero et al. (2010) use the CAPM framework and decompose the return of 141 any asset into a systematic component, correlated with the market, and a residual 142 uncorrelated with the market. The CAPM predicts that the residual return is zero. 143 The predicted value of the residual does not preclude correlations among residual 144 returns, because there may be multiple sources of equity return co-movement, even 145 if there is a single source of expected return. It can be shown that if the regression 146 equation is properly specified and certain other conditions are fulfilled, then the beta 147 obtained is an optimal estimate (actually, minimum-variance, unbiased) of the true 148 AU10 historical beta averaged over past periods. However, this does not imply that the 149 historical beta is a good predictor of future beta. For instance, one defect is that 150 random events impacting the firm in the past may have coincided with market 151 movements purely by chance, causing the estimated value to differ from the true 152 value. Thus, the beta obtained by this method is an estimate of the true historical 153 beta obscured by measurement error. Rudd and Clasing (1982) discussed beta 154 prediction with respect to the use of historic price information. Three possible 155 prediction methods for beta were suggested. These are the following: 156

- 1. *Naïve*: $\hat{\beta}_j = 1.0$ for all securities (i.e., every security has the average beta). 157
- 2. *Historical*: $\hat{\beta}_i = H\hat{\beta}_i$, the historical beta obtained as the coefficient forms an $_{158}$ ordinary least squares regression. 159

³We have glossed over a number of econometric subtleties in these few sentences. Those readers who wish to learn more about these estimation difficulties are directed toward the following articles and the references contained there: Merton Miller and Myron Scholes, "Rates of Return in Relation to Risk: A Reexamination of Recent Findings," in Studies in The Theory of Capital Markets, ed. Michael Jensen (New York: Praeger Publishers, 1972), pp. 47-48.

160 3. *Bayesian-adjusted beta*: $\hat{\beta}_j = 1.0 + BA(H\hat{\beta}_j - 1)$, where the historical betas are adjusted toward the mean value of 1.0.

¹⁶² In each case, the prediction of residual risk is obtained by subtracting the ¹⁶³ systematic variance $(\hat{\beta}_j^2 V_M)$ from the total variance of the security. The residual ¹⁶⁴ variance is obtained directly from the regression.

However, relying simply upon historical price data is unduly restricting in that there are excellent sources of information which may help in improving the prediction of risk. For instance, most analysts would agree that fundamental information is useful in understanding a company's prospects. The *fundamental predictions of risk*, which were pioneered principally by Professor Barr Rosenberg and Vinay Marathe of the University of California at Berkeley, became the fountation of the Barra system.

The historical beta estimate will be an unbiased predictor of the future value of 172 beta, provided that the expected change between the true value of beta averaged 173 over the past periods and its value in the future is zero. If this expected change is 174 not zero, then the historical beta estimate will be misleading (biased). Thus, if 175 historical betas are used as a prediction of beta, there is an implicit assumption that 176 the future will be similar to the past. Is this assumption reasonable? The answer is, 177 probably not. The investment environment changes so rapidly that it would appear 178 imprudent to use averages of historical (5-year) price data as predictions of the 179 future. 180

Barr Rosenberg and Walt McKibben (1973) estimated the determinants of security betas and standard deviations. This estimation formed the basis of the Rosenberg extra-market component study (1974), in which security-specific risk eculd be modeled as a function of financial descriptors, or known financial characteristics of the firm. Rosenberg and McKibben found that the financial characteristics that were statistically associated with beta during the 1954–1970 period were:

- 188 1. Latest annual proportional change in earnings per share;
- 189 2. Liquidity, as measured by the quick ratio;
- 190 3. Leverage, as measured by the senior debt-to-total assets ratio;
- 191 4. Growth, as measured by the 5-year growth in earnings per share;
- 192 5. Book-to-Price ratio;
- 193 6. Historic beta;
- 194 7. Logarithm of stock price;
- 195 8. Standard deviation of earnings per share growth;
- 196 9. Gross plant per dollar of total assets;
- 197 10. Share turnover.

Rosenberg and McKibben used 32 variables and a 578-firm sample to estimate the determinants of betas and standard deviations. For betas, Rosenberg and McKibben found that the positive and statistically significant determinants of beta were the standard deviation of eps growth, share turnover, the price-to-book AU11

multiple, and the historic beta.⁴ Rosenberg et al. (1975), Rosenberg and Marathe 202 (1979), Rudd and Rosenberg (1979, 1980), and Rudd and Clasing (1982) expanded 203 upon the initial Rosenberg MFM framework. 204

204 AU12

In 1975, Barr Rosenberg and his associates introduced the BARRA US Equity 205 Model, often denoted USE1. We spend a great deal of time on the BARRA USE1 206 and USE3 models because 70 of the 100 largest investment managers use the 207

The fundamental prediction method of Barra starts by describing the company, see Rudd and Clasing (1982). The Barra USE1 Model estimated "descriptors," which are ratios that describe the fundamental condition of the company. These descriptors are grouped into six categories to indicate distinct sources of risk. In each case, the category is named so that a higher value is indicative of greater risk.

- 1. *Market variability*. This category is designed to capture the company as perceived by the market. If the market were completely efficient, then all information on the state of the company would be reflected in the stock price. Here the historical prices and other market variables are used in an attempt to reconstruct the state of the company. The descriptors include historical measures of beta and residual risk, nonlinear functions of them, and various liquidity measures.
- 2. *Earnings variability*. This category refers to the unpredictable variation in earnings over time, so descriptors such as the variability of earnings per share and the variability of cash flow are included.
- 3. Low valuation and unsuccess. How successful has the company been, and how is it valued by the market? If investors are optimistic about future prospects and the company has been successful in the past (measured by a low book-to-price ratio and growth in per share earnings), then the implication is that the firm is sound and that future risk is likely to be lower. Conversely, an unsuccessful and lowly valued company is more risky.
- 4. *Immaturity and smallness*. A small, young firm is likely to be more risky than a large, mature firm. This group of descriptors attempts to capture this difference.
- 5. Growth orientation. To the extent that a company attempts to provide returns to stockholders by an aggressive growth strategy requiring the initiation of new projects with uncertain cash flows rather than the more stable cash flows of existing operations, the company is likely to be more risky. Thus, the growth in total assets, payout and dividend policy, and earnings/price ratio is used to capture the growth characteristics of the company.
- 6. *Financial risk*. The more highly levered the financial structure, the greater is the risk to common stockholders. This risk is captured by measures of leverage and debt to total assets.

Finally industry in which the company operates is another important source of information. Certain industries, simply because of the nature of their business, are exposed to greater (or lesser) levels of risk (e.g., compare airlines versus gold stocks). Rosenberg and Marathe used indicator (dummy) variables for 39 industry groups as the method of introducing industry effects.

⁴ When an analyst forms a judgment on the likely performance of a company, many sources of information can be synthesized. For instance, an indication of future risk can be found in the balance sheet and the income statement; an idea as to the growth of the company can be found from trends in variables measuring the company's position; the normal business risk of the company can be determined by the historical variability of the income statement; and so on. The approach that Rosenberg and Marathe take is conceptually similar to such an analysis since they attempt to include all sources of relevant information. This set of data includes historical, technical, and fundamental accounting data. The resulting information is then used to produce, by regression methods, the fundamental predictions of beta, specific risk, and the exposure to the common factors.

BARRA USE3 Model.⁵ The BARRA USE1 Model predicted risk, which required the evaluation of the firm's response to economic events, which were measured by the company's fundamentals. Let us review the Barra prediction rules for the systematic risk and residual risk are expressed in terms of the descriptors, as discussed in Rudd and Clasing (1982). There are three major steps. First, for the time period during which the model is to be fitted, obtain common stock returns and company annual reports (for instance, from the COMPUSTAT database).⁶ In order to make comparisons across firms meaningful, the descriptors must be normalized

so that there is a common origin and unit of measurement, Table 6.1.

Table 6.1 Components of the risk indices

AU13

1	Index of market variability
1	Historical beta estimate
	Historical sigma estimate
	Share turnover, quarterly
	Share turnover, 12 months
	Share turnover, 5 years
	Trading volume/variance
	Common stock price (ln)
	Historical alpha estimate
	Cumulative range, 1 year
2	2. Index of earnings variability
	Variance of earnings
	Extraordinary items
	Variance of cash flow
	Earnings covariability
	Earnings/price covariability
3	3. Index of low valuation and unsuccess
	Growth in earnings/share
	Recent earnings change
	Relative strength
	Indicator of small earnings/price ratio
	Book/price ratio
	Tax/earnings, 5 years
	Dividend cuts, 5 years
	Return on equity, 5 years
4	. Index of immaturity and smallness
	Total assets (log)
	Market capitalization (log)
	Market capitalization
	Net plant/gross plant
	Net plant/common equity
_	(continued)

⁵ According to BARRA online advertisements.

⁶ The COMPUSTAT database is one of the databases collected by Investors Management Sciences, Inc., a subsidiary of Standard & Poor's Corporation.

Inflation adjusted plant/equity
Trading recency
Indicator of earnings history
Index of growth orientation
Payout, last 5 years
Current yield
Yield, last 5 years
Indicator of zero yield
Growth in total assets
Capital structure change
Earnings/price ratio
Earnings/price, normalized
Typical earnings/price ratio, 5 years
Index of financial risk
Leverage at book
Leverage at market
Debt/assets
Uncovered fixed charges
Cash flow/current liabilities
Liquid assets/current liabilities
Potential dilution
Price-deflated earnings adjustment
Tax-adjusted monetary debt

The listing of the USE1 risk index components, as was reported in Rudd and 217 Clasing (1982), was very informative. One wonders as to the weighting of the risk 218 index components. The reader can find the variable weights in the risk index 219 components in Rosenberg and Marathe (1976, see p 20). The Index of Market 220 AU14 Variability was primarily determined by the historic Beta and the historic standard 221 deviation of residual risk. The Index of Earnings Variability was primarily deter- 222 mined by the coefficient of variation of annual earnings per share in the last 5 years 223 and the typical proportion of earnings that are extraordinary items. The Index of 224 Unsuccess and Low Valuation was primarily determined by the measure of propor- 225 tional change in adjusted earnings per share in the past two fiscal years and the 226 "relative strength," the logarithmic rate of return, during the last year. The Index of 227 Immaturity and Smallness was primarily determined by the ratio of gross plant to 228 total equity and the logarithm of total assets. The Index of Growth Orientation was 229 primarily determined by the normal value of the dividend yield during the last 5 230 years and the 5-year asset growth rate. The Index of Financial Risk was primarily 231 determined by the total debt-to-assets ratio and the liquidity of the current financial 232 position. The equations that formed the Index weights in USE1 were proprietary 233 and undisclosed in USE2, USE3, and USE4. 234

In the Barra risk model, data is normalized. The normalization takes the follow- 235 ing form. First, the "raw" descriptor Values for each company are computed. 236 Next, the capitalization-weighted value of each descriptor for all the securities in 237

238 the S&P 500 is computed and then subtracted from each raw descriptor. The transformed descriptors now have the property that the capitalization-weighted 239 value for the S&P 500 stocks is zero. This step unambiguously fixes the "origin" 240 for measurement; however, the unit of "length" is still arbitrary. To standardize the 241 length, the standard deviation of each descriptor is calculated within a universe of 242 large companies (defined as having a capitalization of \$50 million or more). The 243 descriptor is now further transformed by setting the value +1 to be one standard 244 deviation above the S&P 500 mean (i.e., one unit of length corresponds to one 245 standard deviation). Rudd and Clasing (1982) write 246

$$ND = (RD - RD[S\&P])/STDEV[RD],$$
(6.7)

where ND is the normalized descriptor value; RD the raw descriptor value as computer from the data; RD[S&P] the raw descriptor value for the (capitalizationweighted) S&P 500; and STDEV[RD] the standard deviation of the raw descriptor value calculated from the universe of large companies.

At this stage each company is indentified by a series of descriptors which indicate its fundamental position. If a descriptor value is zero, then the company is "typical" of the S&P 500 (for this characteristic) because the S&P 500 and the company both have the same raw value. Conversely, if the descriptor value is nonzero, then the company is atypical of the S&P 500, and this information may he used to adjust the prior prediction in order to obtain a better posterior prediction of risk.

In the second step, one groups the monthly data by quarters, and assemble the 257 descriptors of each company as they would have appeared at the beginning of 258 the quarter. The prediction rule is then fitted by linear regression which relates each 259 monthly stock return in that quarter to the previously computed descriptors. These 260 261 adjustments are combined as follows. Initially, in the absence of any fundamental information, the beta is set equal to its historical value. Then each descriptor is 262 examined in turn, and if it is atypical, the corresponding adjustment to beta is made. 263 For example, if two companies with the same historical beta are identical except 264 that they have very different capitalizations, then one adjusts the risk of the large-265 capitalization company downward, relative to that of the small-capitalization com-266 267 pany, because large companies typically have less risk than small companies. The fundamental knowledge of additional information improves the prediction of risk. 268 The econometric prediction rule is similar; the prediction is obtained by adding the 269 adjustments for all descriptors, in addition to the industry effect, to the historical 270 beta estimate. The prediction rule for the beta of security *i*, in a given month, can be 271 272 written as follows:

$$\hat{\beta}_i = \hat{b}_o + \hat{b}_l d_{li} + \ldots + \hat{b}_J d_{Ji},$$
(6.8)

where $\hat{\beta}_i$ is the predicted beta; \hat{b}_j the estimated response coefficients in the prediction rule; d_{ji} the normalized descriptor values for security *i*; and *J* the total number of descriptors. In this prediction rule we can think of the first descriptor, d_{1i} , as the historical 276 beta, $H\hat{\beta}$. Thus, if only the first descriptor is used, the prediction rule is similar to the 277 specification of the Bayesian adjustment, (6.8). In this case, the linear regression 278 provides estimates for \hat{b}_o and \hat{b}_1 , which indicate the optimal adjustment to historical 279 beta for predictive purposes. Other descriptors in addition to historical beta are 280 employed and appear in the prediction rule as d_{2i} . In other words, the fundamental 281 predictions are direct generalizations of the "price only" predictions.

If the company is completely typical of market (i.e., the descriptors other than 283 historical beta are all zero), then there is no further adjustment to the Bayesian-284 adjusted historical beta. This is intuitive; if the company is in no sense "special," 285 then there is no reason to believe that the averaged true beta in the past will not 286 equal the true beta in the future. However, if the company is atypical, then not all 287 the descriptors (other than historical beta) will be zero. For simplicity, suppose that 288 only the first (historical beta) and second descriptors are nonzero, where the latter 289 has a value of one (i.e., this company is one standard deviation from the S&P 500 290 value). The prediction rule, (6.8), shows that the predicted beta is found by adding 291 the adjustment \hat{b}_2 to the Bayesian-adjusted historical beta. In general, the total 292 adjustment is the weighted sum of the coefficients in the prediction rule, where the 293 weights are the normalized descriptor values which indicate the company's degree 294 of deviance from the typical company.

In the third step, the Barra risk model estimates the company's exposure to each 296 of the common factors and the prediction of the residual risk components. The first 297 task is to form summary measures or indices of risk to describe all aspects of the 298 company's investment risk. These are obtained by forming the weighted average of 299 the descriptor values in each of the six categories introduced above, where the 300 weights are the estimated coefficients from the prediction rule, (6.8), for systematic 301 or residual risk. This provides six summary measures of risk, the risk indices, for 302 each company. Again, these indices are normalized so that the S&P 500 has a value 303 of zero on each index and a value of one corresponds to one standard deviation 304 among all companies with capitalization of \$50 million or more.

The prediction of residual risk is now found by performing a regression on the 306 cross section of all security residual returns as the dependent variable where the 307 independent variables are the risk indices.⁷ The form of the regression, in a given 308 month, is shown in (6.9): 309

$$r_i - \hat{\beta}_i r_{\rm M} = c_1 R I_{1i} + \ldots + c_6 R I_{6i} + c_7 I N D_{1i} + \ldots + c_{45} I N D_{39,i} + u_i, \qquad (6.9)$$

where r_i is the excess return on security i; $\hat{\beta}_i$, the predicted beta, from (6.9); and R_M , 310 the excess return on the market portfolio so that $r_i - \hat{\beta}_i r_M$ is the residual return on 311

⁷ See Barr Rosenberg and Vinay Marathe, "Common Factors in Security Returns: Microeconomic Determinants and Macroeconomic Correlates," *Proceedings of the Seminar on the Analysis of Security Prices*, University of Chicago, May 1976, pp. 61–115 and Rosenberg and Marathe (1979).

security *i*; RI_{1i} , ..., RI_{6i} are the six risk indices for security *i*, IND_{1i} , ..., $IND_{39,i}$ are the dummy variables for the 39 industry groups; u_i is the specific return for security *i*; and c_1 , ..., c_{45} are the 45 coefficients (factor returns) to be estimated.

The result from this cross-sectional regression is the specific return and specific risk on the security, together with the 45 coefficients. These estimated coefficients represent the returns that can be attributed to the factors in the month of the analysis.

The entire risk of the stock arises from two sources: the systematic or factor risk $\begin{pmatrix} b_j^2 \text{ Var } [f] \end{pmatrix}$, and the nonfactor risk $\begin{pmatrix} \sigma_j^2 \end{pmatrix}$, the variance of the residual. In this case, however, the nonfactor risk is completely specific risk since no risk arises from interactions with other stocks. In other words, under these assumptions the single factor, *f*, is responsible for the only commonality among stock returns; thus, the random return component that is not related to the factor must be specific to the individual stock, *j*.

If we form a portfolio, P, with weights $h_{P1}, h_{P2}, ..., h_{PN}$, from N stocks, then the random excess return on the portfolio for a single factor is given by

$$R_{\rm P} = \sum h_{\rm Pj} r_j = \sum h_{\rm Pj} b_j f + \sum h_{\rm Pj} u_j = b_{\rm P} f + \sum h_{\rm Pj} u_j, \qquad (6.10)$$

328 where $b_{\rm P} = \sum h_{\rm Pi} r_i$. The mean return and variance are

$$E[r_{\rm P}] = a_{\rm P} + b_{\rm P} E[f]$$

329 where $a_{\rm P} = \sum h_{{\rm P}j} a_j$, and

$$\operatorname{Var}[r_{\mathrm{P}}] = b_j^2 \operatorname{Var}[f] + \sum h_{\mathrm{P}}^2 \sigma_j^2, \qquad (6.11)$$

where we have made use of the fact that the security-specific risk is *specific*, i.e.,independent across stocks and independent of the factor return.

The market portfolio is just one particular portfolio. Let the security weights be $h_{M1}, h_{M2}, \dots, h_{MN}$, and notice that $b_M = \sum h_{Mj}b_j$. We can set b_M to any value, and so we choose to set $b_M = 1$.⁸ The market return statistics are then

$$E[r_{\rm M}] = a_{\rm M} + E[f]$$

335 and

$$\operatorname{Var}[r_{\mathrm{M}}] = \operatorname{Var}[f] + \sum h_{\mathrm{M}}^2 \sigma_j^2. \tag{6.12}$$

⁸ This step is equivalent to defining an origin for measurement.

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The regression coefficient of an individual stock's rate of return onto the market, 336 or beta, is given by 337

$$\beta_{j} = \operatorname{Cov}[r_{j}, r_{M}]/\operatorname{Var}[r_{M}]$$

$$= \operatorname{Cov}[b_{i}f + u_{j}, f + \sum h_{Mk}u_{k}]/\operatorname{Var}[r_{M}]$$

$$= \left(b_{j}\operatorname{Var}[f] + h_{Mj}\sigma_{j}^{2}\right)/\operatorname{Var}[r_{M}]$$

$$= \left(b_{j}\operatorname{Var}[f] + h_{Mj}\sigma_{j}^{2}\right) / \left(\operatorname{Var}[f] + \sum h_{Mj}^{2}\sigma_{j}^{2}\right)$$
(6.13)

so that

338

$$\beta_{\rm P} = \left(b_{\rm P} \operatorname{Var}[f] + \sum h_{\rm Mj} h_{\rm Pj} \sigma_j^2 \right) / \left(\operatorname{Var}[f] + \sum h_{\rm Mj}^2 \sigma_j^2 \right)^9.$$

Notice that the regression coefficient on the market and the regression coefficient 339 on the factor (i.e., b_j and β_j , and b_P and β_P) are close but not identical. The 340 difference lies in the last terms in the numerator and denominator in both cases. 341 Where a single security is concerned, (6.13), the two sensitivities can only be equal 342 when the market portfolio is composed of a single security; however, for a portfo-343 lio, the sensitivities will be close whenever the portfolio and market holdings are 344 approximately equal (i.e., whenever $\sum h_{Mj}h_{Pj}$ is close to $\sum h_{Mj}^2$). In other words, 345 for well-diversified portfolios (for instance, the majority of institutional portfolios) 346 we may approximate the portfolio beta by its regression coefficient on the factor. 347

This approximation is useful for the analysis of residual return. Recall that the 348 residual return of an individual portfolio (relative to the market portfolio) is equal to 349 the total portfolio excess return on an equal-beta-levered market portfolio. That is, 350 the residual return measures the return due to nonmarket strategy: 351

Residual return =
$$r_{\rm P} - \beta_{\rm P} r_{\rm M}$$
.

Thus, the residual variance is given by

352

$$w_{\rm P}^2 = \operatorname{Var}[r_{\rm P} - \beta_{\rm P} r_{\rm M}]$$

= $\operatorname{Var}\left[(b_{\rm P} - \beta_{\rm P})f + \sum (h_{\rm Pj} - \beta_{\rm P} h_{\rm Mj})u_j)\right]$
= $(b_{\rm P} - \beta_{\rm P})^2 \operatorname{Var}[f] + \sum (h_{\rm Pj} - \beta_{\rm P} h_{\rm Mj})^2 \sigma_j^2,$ (6.14)

since the nonfactor return, u_j , is uncorrelated with the factor return. Now, using the 353 approximation that $\beta_P = b_P$, it follows that 354

$$w_{\rm P}^2 \cong \sum \left(h_{\rm Pj} - \beta_{\rm P} h_{\rm Mj} \right)^2 \sigma_j^2 = \sum \delta_{\rm Pj}^2 \sigma_j^2, \qquad (6.15)$$

355 where $\delta_{P_i} = h_{P_i} - \beta_P h_{M_i}$. In other words, it is the discrepancy between portfolio and the holdings of the (equal-beta-levered) market portfolio that induces residual risk. 356 In this formulation it is correct to write the sensitivity to the market as β_i since, by 357 definition, a stock's beta is the exposure to the market. In addition, the nonmarket 358 return is the expectation plus a random term with zero mean; i.e., nonmarket return 359 is $\alpha_i + \varepsilon_i$, where $E[\varepsilon_i] = 0$, and α_i represents the expected abnormal rate of return, or 360 alpha. That is, according to the stated assumptions of the single-factor model, the 361 random nonmarket return on security *j* should be uncorrelated with the market 362 return and similar returns on all other securities. 363

The mean excess return and variance for stock j are given by

$$E[r_j] = \sum_{k=1}^{K} b_{jk} E[f_k] + E[u_j]$$

365 and

$$\operatorname{Var}[rj] = \sum_{k=1}^{K} \sum_{l=1}^{K} b_{jk} b_{jl} \operatorname{Cov}[f_k, f_l] + \sigma_j^2, \qquad (6.16)$$

where $\text{Cov}[f_k, f_l]$ is the covariance between the factors and equals $\text{Var}[f_l]$ if k = l. This multiple factor model is specified by the security factor loadings, b_{jk} , and the factors, f_k .

If we now form a portfolio, P, with weights $h_{P1}, h_{P2}, ..., h_{PN}$, from N stocks, then the random excess return is given by

$$r_{\rm P} = \sum_{j=1}^{N} h_{\rm Pj} r_j = \sum_{j=1}^{N} h_{\rm Pj} \sum_{k=1}^{K} b_{jk} f_k + \sum_{j=1}^{N} h_{\rm Pj} u_j$$
$$= \sum_{k=1}^{K} \sum_{j=1}^{N} h_{\rm Pj} b_{jk} f_k + \sum_{j=1}^{N} h_{\rm Pj} u_j$$
$$= \sum_{k=1}^{K} b_{\rm Pk} f_k + \sum_{j=1}^{N} h_{\rm Pj} u_j,$$
(6.17)

where we have written $b_{Pk} = \sum h_{Pj}b_{jk}$ as the portfolio loading onto the *k*th factor. Since the market portfolio is a portfolio, the random excess return on the market is given by (6.16), with M replacing P; i.e.,

$$r_{\rm M} = \sum_{k=1}^{K} b_{{\rm M}k} f_k + \sum_{j=1}^{N} h_{{\rm M}j} u_{j.}$$

Proceeding as before, the beta of the *j*th asset is given by

$$\beta_{j} = \operatorname{Cov}[r_{j}, r_{m}] / \operatorname{Var}[r_{M}]$$
$$= \left(\sum_{k=1}^{K} \sum_{l=1}^{K} b_{jk} b_{Ml} \operatorname{Cov}[f_{k}, f_{l}] + b_{Mj} \sigma_{j}^{2}\right) / \operatorname{Var}[r_{M}].$$
(6.18)

It would appear that this complex expression is devoid of meaning; however, this 375 is not the case. Consider the betas of the factors. In particular, for factor k 376

$$\beta_{fk} = \operatorname{Cov}[f_k, r_{\mathrm{M}}] / \operatorname{Var}[r_{\mathrm{M}}]$$
$$= \sum_{l=1}^{K} b_{\mathrm{M}l} \operatorname{Cov}[f_k, f_l] / \operatorname{Var}[r_{\mathrm{M}}]$$

and the beta of the specific component of return on the *j*th asset

$$\beta_{uj} = \operatorname{Cov}[u_j, r_{\mathrm{M}}] / \operatorname{Var}[r_{\mathrm{M}}].$$
$$= h_{\mathrm{M}} j \sigma_j^2 / \operatorname{Var}[r_{\mathrm{M}}].$$

That is, in the multiple factor model the security beta is a weighted average of 378 the factor betas and the beta of the specific return of the security, where the weights 379 are simply the factor loadings for the *j*th security. Notice that the beta of the stock's 380 specific return is nonzero only because the security return is a component of the 381 market return since the security is a part of the market. The intuition with which we 382 wish to leave readers is that, far from being the primitive parameter in finance, the 383 stock beta should be regarded as an average of a stock's exposures to a large 384 number of factors influencing its return. 385

Now the residual return, the return due to a nonmarket strategy, on portfolio P is 386 $r_{\rm P} - \beta_{\rm P} r_{\rm M}$. Hence, the portfolio residual variance, $w_{\rm P}^2$, is given by 387

$$w_{\rm P}^{2} = \operatorname{Var}[r_{\rm P} - \beta_{\rm P} r_{\rm M}]$$

= $\operatorname{Var}\left[\left\{\sum_{k=1}^{K} (b_{\rm Pk} - \beta_{\rm P} b_{\rm Mk})f_{k}\right\} + \left\{\sum_{j=1}^{N} (h_{\rm Pj} - \beta_{\rm P} h_{\rm Mj})u_{j}\right\}\right]$
= $\operatorname{Var}\left[\sum_{k=1}^{K} (\gamma_{\rm Pk} f_{k})\right] + \operatorname{Var}\left[\sum_{j=1}^{N} \delta_{\rm Pj} u_{j}\right],$ (6.19)

where γ is the Greek letter gamma and $\gamma_{Pk} = b_{Pk} - \beta_P b_{Mk}$ is the discrepancy in the 388 portfolio factor loading and the equal-beta-levered market portfolio factor loading; 389 δ_{Pj} is the discrepancy in the holdings, defined below (6.20), and the last step follows 390 because the specific returns are uncorrelated with the factors. 391

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Let the model for beta be given by

$$\beta_{nt} = b_0 + b_1 d_{1nt} + b_2 d_{2nt} + \ldots + b_J d_{Jnt}$$
(6.20)

393 for all time periods *t* and securities *n*, where the *b*'s are coefficients for the 394 systematic risk prediction rule and the *d*'s are the *J* descriptor values for the *n*th 395 company at time *t*. Further, let $E[\varepsilon_{nt}] = 0$ and $\text{Cov}[\varepsilon_{nt}, r_{Mt}] = 0$ for all *t*, and define 396 w_{nt}^2 to be the residual variance, i.e., $w_{nt}^2 = \text{Var}[\varepsilon_{nt}]$. The model for residual risk is 397 given by

$$w_{nt} = \bar{w}_t (s_0 + s_1 d_{1nt} + s_2 d_{2nt} + \ldots + s_J d_{Jnt}), \tag{6.21}$$

where \bar{w}_t is the typical cross-sectional residual standard deviation in month *t*. This prediction rule is rewritten in terms of the mean absolute residual return, v_{nt} , for security *n* in month *t* and the typical mean absolute residual return in month *t*, \bar{v}_t . Therefore, $v_{nt} = E(|\varepsilon_{nt}|)$ and

$$v_{nt} = \bar{v}_t (s_0 + s_1 d_{1nt} + s_2 d_{2nt} + \ldots + s_J d_{Jnt}).$$
(6.22)

The estimate approach proceeds by substituting the beta prediction rule, (6.24), and then performing a "market conditional" regression for beta. The dependent variable is r_{nt} , and the independent variables are $d_{jnt}r_{Mt}$, so the model is

$$r_{nt} = \alpha + b_0(r_{\mathrm{M}t}) + b_1(d_{lnt}r_{\mathrm{M}T}) + \ldots + b_J(d_{Jnt}r_{\mathrm{M}t}),$$

405 which provides preliminary estimates, $\hat{b}_0, \ldots, \hat{b}_j$. With these coefficients, the 406 preliminary prediction of residual return is

$$\hat{\varepsilon}_{nt} = r_{nt} - (\hat{b}_0 + \hat{b}_1 \, d_{1nt} + \ldots + \hat{b}_J d_{Jnt}) r_{\mathrm{M}t}.$$
(6.23)

407 The next regression is fitted to estimate residual risk. It takes the form

$$\hat{\varepsilon}_{nt}|=s_0(\hat{v}_t)+s_1(d_{1nt}\hat{v}_t)+\ldots+s_J(d_{Jnt}\hat{v}_t)$$

408 where

$$ar{v}_t = \sum_{n=1}^N h_{ ext{M}nt} |\hat{arepsilon}_{nt}|$$

409 and h_{Mnt} is the proportion of security *n* in the market portfolio at time *t*. This 410 regression provides estimates, $\hat{s}_0, \ldots, \hat{s}_J$.

The final step in this part of the analysis is to obtain prediction of systematic and residual risk by repeating these two regressions, but now using generalized least squares in order to correct for the different levels of residual risk across the

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securities.⁹ The next task is to decompose the residual return into two components: 414 specific return and the common factor return. This is achieved by a cross-sectional 415 generalized least squares regression where the dependent variable is the residual 416 return in month, t, $r_{nt} - \hat{\beta}_{nt} r_{Mt}$, and the independent variables are the risk indices 417 and industry dummy variables. In this regression, each variable is weighted 418 inversely to the predicted residual risk. 419

The statistically significant determinants of the security systematic risk became 420 the basis of the BARRA E1 Model risk indexes. The domestic BARRA E3 (USE3, 421 or sometimes denoted US-E3) model, with some 15 years of research and evolution, 422 uses 13 sources of factor, or systematic, exposures. The sources of extra-market 423 factor exposures are volatility, momentum, size, size nonlinearity, trading activity, 424 growth, earnings yield, value, earnings variation, leverage, currency sensitivity, 425 dividend yield, and non-estimation universe. The BARRA USE3 descriptors 426 are included in the appendix to this chapter. We use the Barra USE3 Model to 427 create portfolios using expected returns for equities in the United States for the 428 1980-2009 period. 429

Rudd and Clasing (1982) described the development and estimation of USE1. 430 AU15 The MSCI Barra Model used in this chapter is the USE3 Model. The method of 431 combining these descriptors into risk indices is proprietary to BARRA. There are 432 13 risk indexes or style factors in the USE3 Model. They are the following: 433

- 1. Volatility is composed of variables including the historic beta, the daily 434 standard deviation, the logarithm of the stock price, the range of the stock 435 return relative to the risk-free rate, the option pricing model standard deviation, 436 and the serial dependence of market model residuals. 437
- 2. Momentum is composed of a cumulative 12-month relative strength variable 438 and the historic alpha from the 60-month regression of the security excess 439 return on the S&P 500 excess return. 440
- 3. Size is the log of the security market capitalization. 441
- 4. Size Nonlinearity is the cube of the log of the security market capitalization. 442
- 5. Trading Activity is composed of annualized share turnover of the past 5 years, 443 12 months, quarter, and month, and the ratio of share turnover to security 444 residual variance. 445
- 6. Growth is composed of the growth in total assets, 5-year growth in earnings per 446 share, recent earnings growth, dividend payout ratio, change in financial 447 leverage, and analyst-predicted earnings growth. 448
- 7. Earnings Yield is composed of consensus analyst-predicted earnings to price 449 and the historic earnings-to-price ratios. 450 451
- 8. Value is measured by the book-to-price ratio.

⁹This is the statistically efficient approach, and it requires that each observation be weighted inversely to its residual variance.

- 452 9. Earnings Variability is composed of the coefficient of variation in 5-year
 453 earnings, the variability of cash flow, and the variability of analysts' forecasts
 454 of earnings to price.
- 455 10. Leverage is composed of market and book value leverage, and the senior debt456 ranking.
- 457 11. Currency Sensitivity is composed of the relationship between the excess return
- on the stock and the excess return on the S&P 500 Index. These regression residual returns are regressed against the contemporaneous and lagged returns
- 460 on a basket of foreign currencies.
- 461 12. Dividend Yield is the BARRA-predicted dividend yield.
- 462 13. Non-estimation Universe Indicator is a dummy variable which is set equal to
- zero if the company is in the BARRA estimation universe and equal to one if
- the company is outside the BARRA estimation universe.¹⁰

465 Stock Selection Modeling

This analysis builds upon Bloch et al. (1993) and Guerard et al. (2012). We use the 466 USER model described in Guerard et al. (2012). We refer the reader to these studies 467 for much of the underlying expected returns literature. There are many approaches to 468 security valuation and the creation of expected returns. The universe for all analysis 469 consists of all securities on Wharton Research Data Services (WRDS) platform from 470 which we download the CRSP database, I/B/E/S database, and the Compustat 471 database. The I/B/E/S database contains consensus analysts' earnings per share 472 forecast data and the Compustat database contains fundamental data, i.e., the 473 earnings, book value, cash flow, depreciation, and sales data, used in this analysis 474 for the December 1979–December 2007 time period. The stock selection model 475 estimated in this study, denoted as the United States Expected Returns, USER, is 476

$$TR_{t+1} = a_0 + a_1 EP_t + a_2 BP_t + a_3 CP_t + a_4 SP_t + a_5 REP_t + a_6 RBP_t + a_7 RCP_t + a_8 RSP_t + a_9 CTEF_t + a_{10} PM_t + e_t,$$
(6.24)

477 where EP = [earnings per share]/[price per share] = earnings-price ratio; BP =478 [book value per share]/[price per share] = book-price ratio; CP = [cash flow per479 share]/[price per share] = cash flow-price ratio; SP = [net sales per share]/[price480 per share] = sales-price ratio; REP = [current EP ratio]/[average EP ratio over the

¹⁰ The Barra US Equity Model (USE4) was introduced in September 2011. The USE4 Model contains 12 style factors: Beta, Momentum, Size, Earnings Yield, Residual Volatility, Growth, Dividend Yield, Book-to-Price, Leverage, Liquidity, Nonlinear Size, and Nonlinear Beta. Menchero and Orr (2012) hold that the sample covariance matrix under-predicts risk and improved risk forecasts, lower biases, are linked to biases in eigenportfolios (removing eigenportfolio biases). Better risk-adjusted performance of portfolios results from better covariance adjustments.
past 5 years]; RBP = [current BP ratio]/[average BP ratio over the past 5 years]; 481RCP = [current CP ratio]/[average CP ratio over the past 5 years]; RSP = [current 482SP ratio]/[average SP ratio over the past 5 years]; CTEF, consensus earnings-per-share483I/B/E/S forecast, revisions and breadth; PM, Price Momentum; and e, randomly485distributed error term.

The USER model is estimated cross-sectionally using a weighted latent root 486 regression, WLRR, analysis on (6.24) to identify variables statistically significant at 487 the 10% level; uses the normalized coefficients as weights; and averages the 488 variable weights over the past 12 months, as described in Chap. 4.

The information coefficient, IC, is estimated as the slope of a regression line in 490 which ranked subsequent returns are expressed as a function of the ranked strategy, 491 at a particular point of time. In terms of information coefficients the use of the 492 WLRR procedure produces the higher IC for the models during the 1998–2007 493 time period, 0.043, versus the equally weighted IC of 0.040, a result consistent with 494 the previously noted studies. The IC test of statistical significance can be referred to 495 as a Level I test. We have briefly surveyed the academic literature on anomalies and 496 find substantial evidence that valuation, earnings expectations, and price momen-497 tum variables are significantly associated with security returns. Further evidence on 498 the anomalies is found in Levy (1999).¹¹

- Residual Return is last month's residual stock return unexplained by the market.
- · Cash Flow-to-Price is the12-month trailing cash flow per share divided by the current price.
- Earnings-to-Price is the 12-month trailing earnings per share divided by the current price.
- Return on Assets is the 12-month trailing total income divided by the most recently reported total assets.
- · Residual Risk is the trailing variance of residual stock return unexplained by market return.
- 12-month Return is the total return for the stock over the trailing twelve months.
- Return on Equity is the12-month trailing earnings per share divided by the most recently reported book equity.
- Volatility is the 24-month trailing volatility of total stock return.
- Book-to-Price is the most recently reported book value of equity divided by the current market price.
- · Profit Margin is 12-month trailing earnings before interest divided by 12-month trailing sales.
- Three-month return is the total return for the stock over the trailing 3 months.
- Sales-to-Price is 12-month trailing sales per share divided by the market price.

The four measures of cheapness in the USER model: cash-to-price, earnings-to-price, book-toprice, and sales-to-price, all have significant positive payoffs. Haugen and Baker (2010) find statistically significant results for the four fundamental factors as did the previously studies we reviewed. The Haugen and Baker (2010) analysis and results are consistent with those of the Bloch et al. (1993) model.

¹¹ Haugen and Baker (2010) extended their 1996 study in a recent volume to honor Harry Markowitz. Haugen and Baker estimate their model using weighted least squares. They estimated the payoffs to a variety of firms and stock characteristics using a weighted least squares multiple regression in each month in the period 1963 through 2007. Haugen and Baker find that the most significant factors are the following:

500 Efficient Portfolio Construction Using the Barra Aegis System

The USER model can be input into the MSCI Barra Aegis system to create optimized portfolios. The equity factor returns f_k in the Barra United States Equity Risk Model, denoted USE3, are estimated by regressing the local excess returns r_n against the factor exposures, X_{nk} ,

$$r_n = \sum_{k=1}^{K_E} X_{nk} f_k + u_n.$$
(6.25)

The USE3 model uses monthly cross-sectional weighted regressions to estimate 13 (style) factors associated with extra-market covariances discussed earlier in the chapter. The USER model is our approximation of the expected return, or the forecast of active return, α , of the portfolio. Researchers in industry most often apply the Markowitz (1952) mean/variance framework to active management, as to described in Grinold and Kahn (2000):

$$U = \alpha h - \lambda \omega^2 h^2. \tag{6.26}$$

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Here α is the forecast of active return (relative to a benchmark which can be cash), 511 512 ω is the active risk, and h is the active holding (the holding relative to the benchmark holding). The risk aversion parameter, λ , captures individual investor 513 preference. By varying the tolerance or risk-aversion, λ , one can create the efficient 514 Frontier in the Barra model. A similar procedure is used in Bloch et al. (1993). They 515 created efficient portfolios by varying the pick parameter m which measured the 516 risk-aversion. Grinhold and Kahn (2000) use the Information Ratio, IR, as a 517 portfolio construction objective to be maximized, which measures the ratio of 518 residual return to residual risk: 519

$$IR \equiv \frac{\alpha}{\omega}.$$
 (6.27)

We construct an Efficient Frontier by varying the risk-aversion levels. The 520 portfolio construction process uses 8% monthly turnover, after the initial portfolio 521 is created, and 125 basis points of transaction costs each way. The USER-optimized 522 523 portfolios outperform the market, defined here as the Russell 3000 Growth, R3G. The portfolio that maximizes the Geometric Mean (Markowitz 1976) and asset 524 selection occurs at a risk-aversion level of 0.02. The Sharpe Ratio also is 525 maximized at a risk acceptance parameter, RAP, of 0.02 with 109 stocks in the 526 efficient portfolio.¹² A decreasing RAP implies that the more aggressive portfolios 527

¹² The regression-weighted USER outperforms the equally weighted model, EQ, in terms of maximizing the Sharpe Ratio, Information Ratio, Geometric Mean, and the *t*-value on Barra-estimated Asset Selection, a result consistent with Bloch et al. (1993), see Guerard et al. (2012).

have a greater negative size exposure and implies that the portfolios contain smaller 528 capitalized securities. A decreasing risk-aversion level produces a more concentrated 529 portfolio, having fewer securities than a higher RAP portfolio, with the securities 530 having smaller market capitalizations and higher exposures to momentum and 531 growth. The efficient Frontier uses the Barra USE3 Short Model. 532

The efficient USER portfolio at a risk-aversion level of 0.02 offers exposure to 533 MSCI Barra-estimated momentum, value, and growth exposures, see Table 6.2. 534 The reader is hardly surprised with these exposures, given the academic literature 535 and stock selection criteria and portfolio construction methodology employed. 536

The Guerard et al. (2012) USER analysis used the R3G benchmark, which began 537 in December 1996. In this analysis, we can create a USER trade-off curve that 538 covers the December 1979–December 2009 period by using the S&P as our 539 benchmark. We find that the portfolio characteristics of the longer period analysis, 540 1980–2009, are very consistent with the portfolio characteristics of the 1997–2009 541 period, see Table 6.3. We find that an RAP of 0.001 is preferred for the 1980–2009 542 period. 543

The asset selection of the USER model is highly statistically significant and the 544 risk index exposures are consistent with the shorter period.¹³ The USER Efficient 545 Frontier for the 1980-2009 period uses the Barra USE3L (United States Equity 546 Risk Model-Long) Risk Model. This chart shows the Frontier, reported in Miller 547 et al. (2012). 548



Chart 1: USER Efficient Frontier, 1980 – 2009

¹³ The statistical significance of USER in the 1980–2009 period is consistent with Bloch et al. (1993) and Stone and Guerard (2010b).

 Table 6.2 USER efficient Frontier portfolio characteristics, 1996–2009

Benchmark: Russe	ell 3000	Growth	(R3G)																	ĺ
Transaction costs:	125 bas	sis points	each wa	ly (
Risk acceptance																				
parameter			0.015				0.020				0.050				0.100				0.200	
Portfolio	Mean	Return	IR	t	Mean	Return	IR	t	Mean	Return	IR	. 1	Mean	Return	IR	t	X	r _]	R 1	
Average number of assets	102				109				139				171				220			
Risk indices		2.11	0.31	1.12		1.96	0.31	1.11		1.53	0.30	1.09		1.31	0.33	1.19		1.03	0.33	1.21
Industries		-0.84	-0.24	-0.85		-0.77	-0.23	-0.82		-0.74	-0.28	-1.00		-0.20	-0.11	-0.39		0.10	0.04	0.16
Asset selection		2.26	0.46	1.68		2.61	0.53	1.92		2.52	0.58	2.08		2.06	0.55	1.97		2.51	0.73	2.65
Transaction cost		-2.61				-2.62				-2.59				-2.58				-2.58		
Total active		0.91	0.16	0.58		1.18	0.19	0.70	_	0.73	0.16	0.56		0.59	0.15	0.55		1.06	0.26	0.95
Total managed		4.09				4.36				3.91				3.77				4.24		
Currency sensitivity	0.04	0.01	0.03	0.11	0.03	0.02	0.10	0.35	0.02	-0.01	-0.01	-0.02	0.00	0.00	0.02	0.06	-0.01	0.01	0.05	0.19
Earnings	0.39	-0.33	-0.33	-1.18	0.36	-0.31	-0.33	-1.20	0.26	-0.16	-0.24	-0.86	0.19	-0.07	-0.13	-0.46	0.13	-0.01	-0.03 -	-0.10
variation																				
Earnings yield	0.14	0.37	0.60	2.17	0.14	0.37	0.61	2.22	0.13	0.40	0.73	2.63	0.12	0.37	0.72	2.60	0.10	0.33	0.76	2.74
Growth	0.10	-0.14	-0.44	-1.61	0.10	-0.16	-0.52	-1.88	0.11	-0.16	-0.49	-1.78	0.10	-0.12	-0.36	-1.31	0.07	-0.07	-0.27	-0.97
Leverage	0.42	-0.03	-0.03	-0.12	0.40	-0.02	-0.03	-0.09	0.30	-0.02	-0.04	-0.14	0.22	0.01	-0.01	-0.02	0.15	0.01	-0.01	-0.04
Momentum	0.30	-0.58	-0.27	-0.96	0.29	-0.56	-0.27	-0.96	0.24	-0.52	-0.30	-1.08	0.20	-0.41	-0.28	-1.01	0.17	-0.30	-0.25 -	-0.90
Non-EST	0.44	-0.44	-0.14	-0.50	0.42	-0.42	-0.14	-0.50	0.32	-0.30	-0.13	-0.46	0.25	-0.22	-0.12	-0.43	0.18	-0.17	-0.12 -	-0.43
universe													. (
Size	-1.02	2.59	0.58	2.10	-0.94	2.42	0.58	2.11	-0.69	1.83	0.58	2.08	-0.52	1.34	0.55	2.00	-0.38	0.94	0.52	1.89
Size nonlinearity	-0.32	-0.02	-0.03	-0.10	-0.29	-0.01	-0.02	-0.08	-0.20	-0.02	-0.03	-0.12	-0.15	-0.02	-0.03	-0.12	-0.11	0.00	-0.01	-0.02
Trading activity	-0.64	0.70	0.25	0.91	-0.58	0.65	0.26	0.93	-0.42	0.47	0.25	0.92	-0.31	0.36	0.26	0.94	-0.22	0.26	0.26	0.94
Value	0.38	-0.18	-0.19	-0.67	0.36	-0.19	-0.21	-0.74	0.29	-0.12	-0.15	-0.55	0.25	-0.08	-0.13	-0.48	0.20	-0.08	-0.15 -	-0.53
Volatility	0.23	0.32	0.23	0.84	0.20	0.30	0.24	0.85	0.13	0.20	0.23	0.83	0.09	0.17	0.26	0.92	0.06	0.15	0.28	1.02
Yield	0.17	-0.15	-0.41	-1.49	0.16	-0.13	-0.39	-1.41	0.11	-0.05	-0.22	-0.79	0.09	-0.03	-0.15	-0.55	0.07	-0.03	-0.18 -	-0.65

 Table 6.3 USER efficient Frontier portfolio characteristics, 1980–2009

Benchmark: S&P 500																				
Transaction costs: 125 basis points																				
each way Risk		0.001				0.01				0.05				0.10				0.20		
acceptance		10000								200				210						
Inform	nation			Infor	nation			Inforn	nation			Inforn	nation			Informs	ation			
	Mean	Return	Coeffic- ient	T-stati- stic	Mean	Return	Coeffic- ient	T-stati- stic	Mean	Return	Coeffic- ient	T-stat- istic	Mean I	Return C	oeffic- T. ient	-stat- N istic	Aean R	etum	oeffi- T- cient	stat- istic
Average number of assets	61.4				69.2				96.9				116.1				139.9			
Risk indices		1.45	0.18	0.96		1.59	0.21	1.14		1.10	0.19	1.03		66.0	0.20	1.09		0.83	0.20	1.12
Industries A sset		-0.72	-0.17	-0.95		-0.55 4 31	-0.15	-0.80 4 22		-0.26	-0.08	-0.46 4 17		-0.02 2.70	-0.01	-0.04 3.54		0.13 2.62	0.06	0.31 3.80
selection		1410	10.0	70.1		Ĩ,	11.0	44.1		0000	0.0	i.		0.1	0.0	1		707	11.0	10.0
Transaction cost		-2.78				-2.76		2		-2.72				-2.70				-2.69		
Total active		3.10	0.32	1.76		2.50	0.30	1.62	(1.52	0.24	1.29		0.86	0.16	0.88		0.80	0.17	0.92
Total managed		14.27				13.67				12.69				12.04				11.97		
Barra risk indices										Q										
Currency sensi- tivity	0.06	0.03	0.08	0.46	0.06	0.02	0.07	0.36	0.05	0.01	0.04	0.19	0.05	0.01	0.03	0.15	0.04	0.01	0.05	0.27
Eamings variation	0.40	-0.33	-0.29	-1.57	0.31	-0.26	-0.30	-1.63	0.17	-0.12	-0.23	-1.26	0.11	-0.07	-0.18	-1.00	0.06	-0.04	-0.13	-0.70
Eamings yield	-0.03	-0.36	-0.60	-3.30	0.01	-0.04	-0.09	-0.48	0.03	0.09	0.20	1.10	0.03	0.07	0.20	1.10	0.03	0.06	0.20	1.10
Growth	0.43	-0.57	-0.49	-2.69	0.36	-0.44	-0.45	-2.48	0.26	-0.28	-0.41	-2.22	0.21	-0.22	-0.38	-2.10	0.16	-0.15	-0.34	-1.87
Leverage Momentum	0.47	-0.06	-0.07	-0.36	0.39	-0.05	-0.04	-0.22	0.26	-0.04	-0.04	-0.24	0.20	-0.03	10.04	-0.19	0.14	-0.02	-0.04	-0.21
Non-EST	0.45	-0.13	-0.04	-0.22	0.42	-0.24	-0.07	-0.40	0.31	-0.17	-0.07	-0.39	0.25	-0.11	-0.05	-0.30	0.20	-0.05	-0.04	-0.20
Size	-1.63	4.02	0.57	3.15	-1.42	3.41	0.56	3.06	-0.94	2.11	0.50	2.74	-0.74	1.65	0.48	2.65	-0.57	1.30	0.48	2.63
Size	-0.71	-0.58	-0.25	-1.39	-0.57	-0.36	-0.21	-1.16	-0.32	-0.14	-0.15	-0.80	-0.24	-0.09	-0.13	-0.69	-0.19	-0.09	-0.14	-0.76
non- linearity																				
Trading	-0.55	0.10	-0.03	-0.16	-0.56	0.11	-0.03	-0.15	-0.42	0.03	-0.05	-0.28	-0.35	0.05	-0.03	-0.16	-0.28	0.02	-0.04	-0.24
Value	0.15	-0.15	-0.16	-0.90	0.12	-0.15	-0.25	-1.36	0.06	-0.08	-0.21	-1.15	0.04	-0.08	-0.24	-1.33	0.03	-0.06	-0.22	-1.20
Volatility	0.58	-0.86	-0.12	-0.66	0.46	-0.70	-0.13	-0.72	0.26	-0.42	-0.14	-0.79	0.18	-0.31	-0.15	-0.80	0.13	-0.24	-0.16	-0.88
Yield	-0.39	0.42	0.35	1.94	-0.32	0.33	0.34	1.85	-0.20	0.20	0.31	1.68	-0.16	0.15	0.29	1.57	-0.14	0.10	0.23	1.28

The creation of portfolios with a multifactor model and the generation of excess returns will hereby be referred to as a Level II test of portfolio construction.¹⁴

One could ask if the USER model resulted from a seemingly infinite number of 551 variable tests and permutations. The USER was developed by the author in 1989 552 while at Drexel, Burnham, and Lambert in a consulting project for Continental 553 Bank. Guerard and Miller (1991) presented the initial model and the portfolio 554 excess returns at the Berkeley Program in Finance meeting in Santa Barbara, in 555 September 1990. Guerard worked for Harry Markowitz in the Global Portfolio 556 Research Department, GPRD, at the Daiwa Securities Trust Company. The Conti-557 nental Bank model was validated and expanded to test its use of 5-year relative 558 variables and four-quarter variable weights lags. The Continental Bank model was 559 560 validated in Bloch et al. (1993). Markowitz asked if the model could have been "in favor" or "unusually lucky" in its creation and initial implementation. Markowitz 561 and Xu (1994)'s Data Mining Corrections (DMC) proposed three models to evalu-562 ate the outperformance of the best investment methodology when all of the back 563 564 test data are available. It is human nature to be skeptical and wonder whether the best outperformance methodology is the result of "Data Mining." It has been 565 applied routinely in the quantitative researches, for example, Bloch et al. (1993) 566 and Guerard et al. (2010). This chapter follows previous papers doing the Data 567 Mining Correction calculations with the longer data. We refer to the application of 568 the Markowitz and Xu (1993) DMC test as a Level III test. 569

Fundamental factors like dividend-to-price (DP), earnings-to-price (EP) include 570 forecast earnings-to-prices (FEP1, FEP2), book-to-price (BP), cash-to-price ratio 571 (CP), sales-to-price ratio (SP), and none fundamental factors like size (EWC), price 572 momentums (PM71, PM, MQ) and financial analyst forecast earnings revisions 573 (BR1, BR2, RV1, RV2) are not only used in risk modeling, e.g., Rosenberg (1974), 574 575 but also used in stock selection models. Some researchers combine some simple factors into a composite factor to enhance forecast power like USER and CTEF 576 reported here. With the various expected return forecast model and risk model, 577 researchers can pick a target portfolio from efficient Frontier according to preset 578 investors' objectives. The excess returns of the portfolios created by the individual 579 variables are denoted by model i. Here is the summary table, Table 6.4, of target 580 581 portfolios generated by Barra Aegis optimization and portfolio management system, based on the previously discussed expected return "models," with the same 582 risk trade-off parameter and the same trading cost. 583

The Markowitz and Xu (1994) DMC models assume that the *T* period backtest returns were identically and independently distributed (i.i.d.), and it is assumed that future returns are drawn from the same population (also i.i.d.). Let y_{it} be the logarithm of one plus the return for the *i*th portfolio selection methodology in period *t*. Then y_{it} is of the form AU18

AU19

AU20

¹⁴ The eight-factor model generated statistically significant predictive power when used in the portfolio optimization and construction processes of Stone (1970, 1973, 2010a).

Table 6.4 US simulated returns: Jan 1980–Dec 2	.009
--	------

	Monthly excess return	
Portfolios	to S&P 500 in percent	t-Statics
USER	0.28	1.72
BR1	0.16	1.29
BR2	0.13	1.12
RV1	0.22	1.48
RV2	0.04	0.32
FEP1	0.02	0.09
FEP2	-0.19	-0.87
CTEF	0.27	2.40
EP	0.09	0.50
BP	0.07	0.33
СР	0.16	0.90
SP	0.34	1.81
DP	0.22	1.21
PM71	0.16	0.84
PM	0.16	0.70
EWC	0.14	0.80
MQ	0.39	2.44

$$y_{ti} = \mu_i + \varepsilon_{it}, \tag{6.28}$$

where μ_i is a portfolio selection method effect and ε_{it} is a random deviation. 589 The random deviation ε_{it} has a zero mean and is uncorrelated with μ_i , i.e., 590

$$E(\varepsilon_{it}) = 0 \tag{6.29}$$

$$\operatorname{cov}(\mu_i, \ \varepsilon_{jt}) = 0 \text{ for all } i, \ j \text{ and } t.$$
 (6.30)

The "best" linear unbiased estimate of the expected portfolio selection return 591 vector μ is 592

$$= E(\mu)e + \operatorname{Var}(\mu) \left[\frac{1}{T}C + \operatorname{Var}(\mu)I\right]^{-1} \times (\tilde{y} - E(\mu)e),$$
(6.31)

where C is the covariance matrix of random effect, i.e.,

$$C = \operatorname{cov}(\varepsilon_e, \ \varepsilon_j). \tag{6.32}$$

Markowitz and Xu (1994) refer to this as DMC Model III.594If one assumes that random effect is of form595

$$\varepsilon_{it} = z_t + \eta_{it} \tag{6.33}$$

where Z_t is the period effect it is assumed to be uncorrelated with random effect η . 596

593

597 The best estimate of μ_i of (6.31) will be simplified to

$$\hat{\mu} = \bar{r} + \beta \ (\bar{r}_i - \bar{r}), \tag{6.34}$$

598 where

$$\bar{r} = \sum_{i=1}^{T} r_i / n.$$
 (6.35)

AU21

That is the best estimate of means of return of portfolio selection i is not sample mean return, rather it is regressed back to the average return (the grand average). Markowitz and Xu (1994) refer to this as the DMC Model II and is the focus of their paper.

Model II can be used to test the null hypothesis that all these portfolios selected by different methods are equally good. If this hypothesis can be rejected, (6.35) gives the best estimate for each selected portfolio. In the above portfolios, the null hypothesis can be rejected with more than 90% confidence because the *F*-statistic equals 1.5 and β is estimated to be 0.33. Readers are referred to the original paper for detailed calculations.

609 DMC Model III Calculation

610 Instead of assuming that μ_i are random, Rao (1973) derived a formula for testing the

611 significance of the null hypothesis that all means of these portfolios are the same.612 The *F*-statistic is calculated by

$$F = \frac{T - n + 1}{n - 1} \times \frac{T}{T - 1} \times \left(\sum \sum c^{ij} \times \bar{r}_i \, \bar{r}_j - \frac{\left[\sum \sum c^{ij} (\bar{r}_i + \bar{r}_j) \right]^2}{4 \sum \sum c^{ij}} \right), \quad (6.36)$$

613 where (c^{ij}) is the inverse matrix of the *C*, the sample (estimated with T-1 D.F.) 614 dispersion matrix as defined in (6.32).

When applying formula (6.36) to above portfolios, F = 1.9. Thus, we can reject 616 the hypothesis with 95% confidence. The Bayesian estimate of means are the 617 following:

618	Portfolio	$\bar{r}_i - \bar{r}$	Bayesian estimate of $\bar{r}_i - \bar{r}$	Estimate-to-actual ratio
619	S&P500	-0.09	-0.08	0.96
620	USER	0.14	0.12	0.86
621	BR1	0.06	0.05	0.84
622	BR2	0.03	0.02	0.59
623	RV1	0.07	0.09	1.18
624	RV2	-0.10	-0.08	0.82
				(continued)

References

Portfolio	$\bar{r}_i - \bar{r}$	Bayesian estimate of $\bar{r}_i - \bar{r}$	Estimate-to-actual ratio	626
FEP1	-0.15	-0.09	0.59	627
FEP2	-0.40	-0.32	0.79	628
CTEF	0.16	0.16	0.95	629
EP	-0.05	-0.05	1.05	630
BP	-0.10	-0.10	1.01	631
СР	0.02	0.02	0.82	632
SP	0.18	0.17	0.94	633
DP	0.09	0.09	0.96	634
PM71	-0.02	-0.03	1.26	635
PM71	-0.08	-0.09	1.16	636
EWC	0.00	-0.01	1.30	637
MQ	0.24	0.21	0.91	638

DMC provides some statistical answers to the impossible question whether an 639 investment selection result is "lucky" or genuinely better. The DMC model III test 640 produces a higher test statistic than DMC model II. The Bayesian's estimates are 641 much closer to the simple sample estimates which ignore the other investment's 642 influence. DMC model II is simpler and more plausible. 643

Conclusions

644

In this case study, we demonstrated the effectiveness of the Barra Aegis system to 645 create investment management strategies to produce portfolios and attribute portfolio returns to the Barra multifactor risk model during the December 647 1979–December 2009 period. We find additional evidence to support the use of 648 MSCI Bara multifactor models for portfolio construction and risk control. We 649 report two results: (1) a composite model incorporating fundamental data, such as 650 earnings, book value, cash flow, and sales, with analysts' earnings forecast 651 revisions and price momentum variables to identify mispriced securities; (2) the 652 returns to a multifactor risk-controlled portfolio allow us to reject the null hypothe-653 sis that results are due to data mining. We develop and estimate three levels of 654 testing for stock selection and portfolio construction. The use of multifactor risk-655 controlled portfolio returns allows us to reject the null hypothesis that the results are 656 due to data mining. The anomalies literature can be applied in real-world portfolio 657 construction.

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Chapter No.: 6

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Chapter 71More Markowitz Efficient Portfolios Featuring2the USER Data and an Extension to Global Data3and Investment Universes4

In the previous chapter, we used the Barra Aegis system to create and measure 5 portfolios using the USER model. The Barra Model is referred as a fundamental 6 risk model because security fundamental data is used to create the risk, or style, 7 indexes. In this chapter, we create portfolios using statistically-based risk models in 8 the USA and global markets. In this chapter, we address several additional issues 9 in portfolio construction and management with Guerard et al. (2012) USER data. 10 First, we test the issue of whether Markowitz mean-variance, MV, portfolio 11 construction model (1956, 1959, 1987), with a fixed upper bound on security 12 weights, dominates the Markowitz enhanced index tracking, EIT, portfolio con- 13 struction model (1987) in which security weights are an absolute deviation from 14 the security weight in the index. We will refer to the absolute deviation from the 15 benchmark weight-enhanced index portfolio construction weight as the equal active 16 weighting, or EAW, portfolio construction model. Guerard, Krauklis, and Kumar 17 (2012) reported that MV portfolios produced higher Information Ratios and Sharpe 18 Ratios than EAW portfolios with weights less than EAW4. A newer approach to the 19 systematic risk optimization technique is the Systematic Tracking Error optimiza- 20 tion technique reported by Wormald and van der Merwe (2012). We will show the 21 effectiveness of the Systematic Tracking Error approach using Global Expected 22 Returns (GLER) data over the 2002–2011 period. Finally, we demonstrate using the 23 Axioma system and its Alpha Alignment Factor (AAF) analysis reported in Saxena 24

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AU1

and Stubbs (2012) that the AAF is appropriate for USER and GLER Data and that 25

the Axioma Statistical Risk Model dominates the Axioma Fundamental Model.¹ 26 The security weights are the primary decision variables to be solved in efficient 27 portfolios. Second, we test whether a (traditional) mean-variance optimization 28 technique using the portfolio variance as the relevant risk measure dominates 29 risk-return trade-off curve using the Blin-Bender APT Tracking Error at Risk 30 (TaR) optimization technique which emphasizes systematic, or market, risk. The 31 APT measure of portfolio risk, TaR, estimates the magnitude that the portfolio 32 return may deviate from the benchmark return over 1 year. Specifically, the TaR 33 optimization technique emphasizes systematic risk, rather than total risk, in portfo-34 lio optimization. A statistically-based principal components analysis (PCA) model 35 is used to estimate and monitor portfolio risk in the Blin and Bender TaR system. 36 To address these issues, we construct efficient portfolios with the USER data, 37

solving for security weights using mean-variance and equal active weighting 38 portfolio construction models for the 1997-2009 period. The MV portfolio con-39 40 struction model with fixed security upper bounds performs very well in comparison to EAW portfolio construction models. Mean-variance portfolios with a 4% secu-41 42 rity upper bound outperform EAW 1, 2, and 3% strategies. One must use an (at least) EAW 4% strategy to outperform the MV portfolio construction model 43 with a 4%, see Guerard, Krauklis, and Kumar (2012). Index-tracking portfolio 44 construction models are extremely useful if a manager is more concerned with 45 underperforming an index; however, the portfolio manager must be aggressive with 46 the EAW strategy to outperform a traditional mean-variance portfolio construction 47 analysis. 48

We employ mean-variance and TaR optimization techniques to test whether 49 equal active weighting strategies of 1, 2, 3, 4, and 5% (weight deviations from the 50 index, or benchmark, weights) outperform mean-variance strategies using 4 and 51 7% maximum security weights. We will show mean-variance portfolios using the 52 53

Tracking Error at Risk optimization technique outperform the mean-variance

¹ In Chap. 6, we reported that asset selection was statistically significant in the Barra Aegis system. We report similar results with Sungard APT and Axioma. The author's belief is that the three systems can be used to produce highly statistically significant asset selection and very good portfolio returns and great risk-return statistics. One needs to decide if one wants to set Lambda, as with Sungard APT, active risk, as with Axioma, and risk acceptance parameters, as with Barra. In the author's view, APT, the system that the author has used since 1989 is outstanding and very adequate. Many (intelligent) people choose active risk (tracking error targets). As long as you are statistically significant in asset selection with the USER variable (or other proprietary forms) and are man-enough to implement the model to maximize the Sharpe Ratio and Geometric Mean (having a negative size exposure and positive momentum, growth, and value exposures), then the choice of APT and Axioma (and Barra) is analogous to the man who is asked if he prefers blondes, brunettes, or redheads; one prefers great minds, strong wills, good looks, and the hair color, preferably natural, is a lesser concern. Not all risk models and optimizers work, as we found out in the McKinley Capital Horse Race and research seminars of 2009 and 2011. Some systems are more expensive and their portfolios are dominated by APT, Axioma, and Barra on a risk-return analysis. We found a decidedly negative correlation between cost and performance.

optimization technique during the 1997–2009 period. Both optimization techniques 54 produce statistically significant asset selection. We employ the Wormald and van 55 der Merwe (2012) Systematic Tracking Error optimization techniques and find 56 statistically significant asset selection. In this chapter, we examine two portfolio 57 construction models: mean–variance and equal active weighting models; and two 58 portfolio optimization techniques: mean–variance and Tracking Error at Risk, and 59 Systematic Tracking Error optimization techniques. 60

Lambda is a measure of the trade-off between expected returns and risk, as 61 measured by the portfolio standard deviation. Generally, the higher the lambda, 62 the higher is the expected ratio of expected return to standard deviation. That is, 63 creating portfolios with less than optimal lambdas produce portfolio excess returns 64 that are not statistically different from zero, whereas appropriate lambdas create 65 portfolios that are statistically significant. In the King's English, benchmark-66 hugging portfolio construction techniques can destroy significant asset selection. 67 We assume that the portfolio manager seeks to maximize the combination of 68 portfolio Geometric Mean (GM), Sharpe Ratio (ShR), and Information Ratio (IR), 69 and asset selection in the Barra attribution analysis. If a portfolio manager has 70 models that produce slightly different ordering on these criteria, we maximize the 71 Geometric Mean (Latane 1959; Vander Weide 2010) as the ultimate criteria, since it 72 is well known that risk is implicit in the Geometric Mean (Markowitz, Chap. 9). 73

Constructing Efficient Portfolios

74

In the previous chapter, we discussed the Barra Aegis system and its use in creating 75 efficient portfolios that produce statistically significant asset selection. Let us step 76 back for a moment and review six decades of portfolio construction and manage-77 ment. In the beginning, there was Markowitz (1952). The Markowitz portfolio 78 construction approach seeks to identify the efficient frontier, the point at which 79 returns are maximized for a given level of risk, or minimize risk for a given level of 80 return. The reader is referred to Markowitz (1959) for the seminal discussion of 81 portfolio construction and management. The portfolio expected return, $E(R_p)$, is 82 calculated by taking the sum of the security weights, *w*, multiplied by their 83 respective expected returns. The portfolio standard deviation is the sum of weighted 84 security covariances.

$$E(R_{\rm p}) = \sum_{i=1}^{N} w_i E(R_i),$$
(7.1)

$$\sigma_{\rm p}^2 = \sum_{i=1}^N \sum_{j=1}^N w_i w_j \sigma_{ij},$$
(7.2)

where $\sum_{i=1}^{N} w_i = 1$ the security weighting summing to one indicates that the portfolios are fully invested.

The Markowitz framework measured risk as the portfolio standard deviation, its measure of dispersion, or total risk. One seeks to minimize risk, as measured by the

90 covariance matrix in the Markowitz framework, holding constant expected returns.

91 Elton et al. (2007) write a more modern version of the traditional Markowitz 92 mean–variance problem as a maximization problem:

$$\theta = \frac{E(R_{\rm p}) - R_{\rm F}}{\sigma_{\rm p}^2},\tag{7.3}$$

93 where $\sum_{i=1}^{N} w_i = 1$ 94 and

$$\sigma_{\mathrm{p}}^{2} = \sum_{i=1}^{N} w_{i}^{2} \sigma_{i}^{2} + \sum_{i=1}^{N} \sum_{j=1}^{N} w_{i} w_{j} \sigma_{ij}, \quad i \neq j$$

95 and $R_{\rm F}$ is the risk-free rate (90-day treasury bill yield).

96 The optimal portfolio weights are given by:

 $\frac{\partial \theta}{\partial w_i} = 0.$

As in the initial Markowitz analysis, one minimizes risk by setting the partial derivative of the portfolio risk with respect to the security weights, the portfolio decision variables, to 0.

Modern portfolio theory evolved with the introduction of the Capital Asset Pricing Model, the CAPM. Implicit in the development of the CAPM by Sharpe (1964), Lintner (1965), and Mossin (1966) is that the investors are compensated for bearing systematic or market risk, not total risk. Systematic risk is measured by the stock beta. The beta is the slope of the market model in which the stock return is regressed as a function of the market return.² An investor is not compensated for bearing risk that may be diversified away from the portfolio.

107 The CAPM holds that the return to a security is a function of the security's beta.

$$R_{jt} = R_{\rm F} + \beta_j [E(R_{Mt}) - R_{\rm F}] + e_j, \qquad (7.5)$$

 $^{^{2}}$ Harry Markowitz often (always) reminds his audiences and readers that he discussed the possibility of looking at security returns relative to index returns in Chap. 4, footnote 1, page 100, of Portfolio Selection (1959).

where R_{jt} = expected security return at time *t*; $E(R_{Mt})$ = expected return on the 108 market at time *t*; $R_{\rm F}$ = risk-free rate; β_j = security beta; and e_j = randomly 109 distributed error term. 110

An examination of the CAPM beta, its measure of systematic risk, from the 111 Capital Market Line equilibrium condition follows. 112

$$\beta_j = \frac{\operatorname{Cov}(R_j, R_M)}{\operatorname{Var}(R_M)}.$$
(7.6)

The difficulty of measuring beta and its corresponding SML gave rise to extramarket measures of risk found in the work of Rosenberg (1974), Rosenberg and 114 Marathe (1979), Ross (1976), and Ross and Roll (1980).³ The fundamentally-based 115 domestic Barra risk model was developed in the series of studies by Rosenberg and 116 thoroughly discussed in Rudd and Clasing (1982) and Grinhold and Kahn (1999), 117 and as discussed in the previous chapter. 118

The total excess return for a multiple-factor model (MFM) in the Rosenberg 119 methodology for security j, at time t, dropping the subscript t for time, may be 120 written like this: 121

$$E(R_j) = \sum_{k=1}^{K} \beta_{jk} \tilde{f}_k + \tilde{e}_j.$$
(7.7)

The nonfactor, or asset-specific return on security j, is the residual risk of the 122 security after removing the estimated impacts of the K factors. The term f is the rate 123 of return on factor "k." A single-factor model, in which the market return is the only 124 estimated factor, is obviously the basis of the CAPM. Accurate characterization of 125 portfolio risk requires an accurate estimate of the covariance matrix of security 126 returns. An alternative to the fundamentally-based Barra risk model is a risk model 127 based on statistically-estimated (orthogonal) principal components, as described in 128 the APT model of Blin et al. (1997).

Extensions to the Traditional Mean–Variance Model

A second extension to the mean–variance approach involves the minimization of 131 the tracking error of an index. Markowitz (1987, 2000) rewrites the general 132 portfolio construction model variance, *V*, to be minimized as: 133

$$V = (X - W)^{T} C(X - W), (7.8)$$

130

³ The reader is referred to Chap. 2 of Guerard (2010) for a history of multi-index and multi-factor risk models.

where $W^T = (W_1, \ldots, W_n) =$ the weights of an index of returns, X are the portfolio weights, and $r^T = (r_1, \ldots, r_n) =$ security returns.

One creates portfolios by allowing portfolio weights to differ from index weights

137 by $\pm 1\%$, EAW1, 2%, EAW2, 3%, EAW3, 4%, EAW4, or 5%, EAW5. Obviously, 138 one can use an infinite set of EAW variations. We restrict this analysis to EAW1,

139 EAW2, EAW3, and EAW4 for simplicity.

Portfolio Construction, Management, and Analysis: An Introduction to Tracking Error at Risk

142 The USER simulation conditions are identical to those described in Guerard et al. (2012), in which we use monthly optimization with 8% turnover, 125 basis points, 143 each way, of transactions cost.⁴ We use the APT risk model and optimizer described 144 in Blin et al. (1997) to create portfolios during the 1997-2009 period by varying the 145 portfolio lambda. One seeks to maximize the Geometric Mean, Sharpe Ratios, and 146 Information Ratios of portfolios. However, what if one wants to be considered a 147 148 "concentrated portfolio manager" who does not hold 300-500 stocks. How many securities should one employ in portfolios using MV and EAW construction models 149 with a monthly set of 3,000 expected return and covariance data? Can a manager 150 construct efficient portfolios of 3,000 stock universes with fewer than 100 securities 151 in the portfolios? 152

Guerard (2012) demonstrated the effectiveness of APT and Sungard APT systems in portfolio construction and management. Let us review the APT approach to portfolio construction. The estimation of security weights, *x*, in a portfolio is the primary calculation of Markowitz's portfolio management approach, as we have discussed in several chapters. The issue of security weights will be now considered from a different perspective. As previously discussed, the security weight is the proportion of the portfolio's market value invested in the individual security.

$$x_s = \frac{\mathrm{MV}_s}{\mathrm{MV}_p},\tag{7.9}$$

⁴ Guerard (2012) decomposed the MQ variable into: (1) price momentum, (2) the consensus analysts' forecasts efficiency variable, CIBF, which itself is composed of forecasted earnings yield, EP, revisions, EREV, and direction of revisions, EB, identified as breadth, Wheeler (1991), and (3) the stock standard deviation, identified in Malkiel (1963) as a variable with predictive power regarding the stock price-earnings multiple. Guerard (1997) and Guerard and Mark (2003) found that the consensus analysts' forecast variable dominated analysts' forecasted earnings yield, as measured by I/B/E/S 1-year-ahead forecasted earnings yield, FEP, revisions, and breadth. Guerard reported domestic (US) evidence that the predicted earnings yield is incorporated into the stock price through the earnings yield risk index. Moreover, CIBF dominates the historic low price-to-earnings effect, or high earnings-to-price, PE.

where $x_s = \text{portfolio-weight}$ insecurity *s*, $MV_s = \text{value}$ of security *s* within the 160 portfolio, and $MV_p =$ the total market value of portfolio. 161

The active weight of the security is calculated by subtracting the security weight 162 in the (index) benchmark, b, from the security weight in the portfolio, p. 163

$$x_{s,p} - x_{s,b}$$
. (7.10)

Accordingly, if IBM has a 3% weight in the portfolio while its weight in the 164 benchmark index is 2 and $1\frac{1}{2}$ %, then IBM has a positive, 50 basis points active 165 weight in the portfolio. The portfolio manager has an active, positive opinion of 166 securities on which he or she has a positive active weight and a negative opinion of 167 those securities with negative active weights.

Markowitz analysis (1952, 1959) and its efficient frontier minimized risk for a 169 given level of return. Risk can be measured by a stock's volatility, or the standard 170 deviation in the portfolio return over a forecast horizon, normally 1 year. 171

$$\sigma_{\rm p} = \sqrt{E(r_{\rm p} - E(r_{\rm p}))^2}.$$
 (7.11)

Blin and Bender created an APT, Advanced Portfolio Technologies, Analytics 172 Guide (2005), which built upon the mathematical foundations of their APT system, 173 published in Blin et al. (1997). The following analysis draws upon the APT 174 analytics. Volatility can be broken down into systematic and specific risk: 175

$$\sigma_{\rm p}^2 = \sigma_{\beta \rm p}^2 + \sigma_{\varepsilon \rm p}^2, \tag{7.12}$$

where $\sigma_{\rm p}$ = total portfolio volatility, $\sigma_{\beta \rm p}$ = systematic portfolio volatility, and 176 $\sigma_{\varepsilon \rm p}$ = specific portfolio volatility.

Blin and Bender created a multifactor risk model within their APT risk model 178 based on forecast volatility. 179

$$\sigma_{\rm p} = \sqrt{52 \left(\sum_{c=1}^{c} \left(\sum_{i=1}^{s} x_i \beta_{i,c} \right)^2 + \sum_{i=1}^{s} x_i^2 \varepsilon_{i,x}^2 \right)}, \tag{7.13}$$

where σ_p = forecast volatility of annual portfolio return, C = number of statistical 180 components in the risk model, x_i = portfolio weight in security *i*, $\beta_{i,c}$ = the loading 181 (beta) of security *i* on risk component *c*, and $\varepsilon_{i,w}$ = weekly specific volatility of 182 security *i*. 183

The Blin and Bender (1995) systematic volatility is a forecast of the annual 184 portfolio standard deviation expressed as a function of each security's systematic 185 APT components.

182 7 More Markowitz Efficient Portfolios Featuring the USER Data and an Extension...

$$\sigma_{\beta p} = \sqrt{52 \sum_{c=1}^{c} \left(\sum_{i=1}^{s} x_i \beta_{i,c}\right)^2}.$$
 (7.14)

187 Portfolio-specific volatility is a forecast of the annualized standard deviation 188 associated with each security's specific return.

$$\sigma_{\varepsilon p} = \sqrt{52 \sum_{i=1}^{s} x_i^2 \varepsilon_{i,x}^2}.$$
(7.15)

Tracking error, te, is a measure of volatility applied to the active return of funds
(or portfolio strategies) indexed against a benchmark, which is often an index.
Portfolio tracking error is defined as the standard deviation of the portfolio return
less the benchmark return over 1 year.

$$\sigma_{\rm te} = \sqrt{E(((r_{\rm p} - r_{\rm b}) - E(r_{\rm p} - r_{\rm b}))^2)},$$
(7.16)

193 where σ_{te} = annualized tracking error, r_{p} = actual portfolio annual return, and 194 r_{b} = actual benchmark annual return.

The APT-reported tracking error is the forecast tracking error for the current portfolio versus the current benchmark for the coming year.

$$\sigma_{\rm te} = \sqrt{52 \left(\sum_{c=1}^{c} \left(\sum_{i=1}^{s} x_{i,\rm p} - x_{i,\rm b}\right) \beta_{i,c}\right)^2 + \sum_{i=1}^{s} \left(x_{i,\rm p} - x_{i,\rm b}\right)^2 \varepsilon_{i,\rm x}^2},\tag{7.17}$$

197 where $x_{i,p} - x_{i,b}$ = portfolio active weight.

Systematic Tracking Error of a portfolio is a forecast of the portfolio's active annual return as a function of the securities' returns associated with APT risk model components.

$$\sigma_{\beta te} = \sqrt{52 \sum_{c=1}^{c} \left(\sum_{i=1}^{s} (x_{i,p} - x_{i,b}) \beta_{i,c}^2 \right)}.$$
 (7.18)

201 Portfolio-specific tracking error can be written as a forecast of the annual 202 portfolio active return associated with each security's specific behavior.

$$\sigma_{\text{ete}} = \sqrt{52 \sum_{i=1}^{s} (x_{i,\text{p}} - x_{i,\text{b}})^2 \varepsilon_{i,x}^2}.$$
 (7.19)

The marginal volatility of a security, or the measure of the sensitivity of portfolio volatility, is relative to the change in the specific security weight. Portfolio Construction, Management, and Analysis: An Introduction to...

$$\partial_s = \frac{\partial \sigma_p}{\partial x_s},\tag{7.20}$$

where $\partial_s =$ marginal risk of security *s*.

$$\partial_s = \beta_{sp} \sigma_p. \tag{7.21}$$

The portfolio Value-at-Risk (VaR) is the expected maximum loss that a portfolio 206 could produce over 1 year. 207

$$VaR = v_p = \tilde{V}_T \text{ given prob}(V_T < \tilde{V}_T) = c, \qquad (7.22)$$

where V_T = actual potential portfolio value in 1 year, \tilde{V}_T = potential portfolio 208 value in 1 year, and c = desired confidence level for VaR (i.e., 95%). 209

If a portfolio return is assumed to be generated from a normal distribution, then 210

$$v_{\rm p} = \sqrt{2} {\rm erf}^{-1} (2_x - 1) \sigma_{\rm p} V_0,$$
 (7.23)

where $\operatorname{erf}^{-1}(x) = \operatorname{inverse}$ error function and $V_0 = \operatorname{current}$ portfolio value. 211 The APT calculated VaR is written like this: 212

$$v_{\rm p} = \sqrt{2} {\rm erf}^{-1} (2_x - 1) \left(\sqrt{52 \left(\sum \left(\sum x_i \beta_{i,c} \right)^2 + \sum x_i^2 \varepsilon_{i,x}^2 \right)} \right) V_0.$$
(7.24)

The APT measure of portfolio risk estimating the magnitude that the portfolio 213 return may deviate from the benchmark return over 1 year is referred to as TaR, or 214 Tracking-at-Risk[™]. 215

$$T_{\rm p}^{\rm V} = \sqrt{\left(\frac{1}{\sqrt{1-x}}\sigma_s\right)^2 + \left(\sqrt{2}{\rm erf}^{-1}(x)\sigma_\varepsilon\right)^2},\tag{7.25}$$

where $T_p^V = \text{TaR}^{\text{TM}}$, $x = \text{desired confidence level of TaR}^{\text{TM}}$, $\sigma_s = \text{portfolio}_{216}$ Systematic Tracking Error, $\text{erf}^{-1}(x) = \text{inverse error function, and } \sigma_{\varepsilon} = \text{portfolio-}_{217}$ specific tracking error.

Blin and Bender (1987–1997) estimated a 20-factor beta model of covariances219based on two-and-one-half years of weekly stock returns data. The Blin and Bender220 AU2Arbitrage Pricing Theory (APT) model followed the Ross factor modeling theory,221but Blin and Bender estimated betas from at least 20 orthogonal factors. Blin and222Bender never sought to identify their factors with economic variables.223

Guerard et al. (2010) found that the APT-TaR estimation procedure helped in 224 creating 130/30 portfolios relative to traditional Markowitz mean-variance and 225 equal active weighting portfolios. Guerard (2012) reported very similar results in 226

205

183



Char. 7.1 USER Tracking Error at Risk (TaR) MV, EAW strategies, January 1997 to December 2009

construct equal active weighting (EAW2 with 2% deviations), mean-variance (MV 227 with a 4% maximum weight) and Mean–Variance Tracking Error at Risk (MVTaR) 228 portfolios for January 1997 to December 2009 using 8% monthly turnover, after the 229 initial portfolio is created, and 150 basis points of transactions costs each way with 230 USA and Global Expected Returns series. Comparing EAW, MV, and MV TaR 231 provides support for the MVTaR procedure in the USA, as TaR maximizes the 232 Geometric Mean, Sharpe Ratio, and Information Ratio relative to EAW and MV. In 233 the global universe, MVTaR maximizes the Geometric Mean and Sharpe Ratio. 234 EAW maximizes the Information Ratio in global markets over this time period. 235

Reported that APT-TaR estimation procedures were very successful in 236 237 maximizing Information Ratios and Sharpe Ratios relative to MV and EAW techniques with the USER data. 238

Guerard, Krauklis, and Kumar (2012) reported that mean-variance dominated 239 240 EAW1, EAW2, and EAW3 strategies with the USER data. One had to use an EAW4 to perform as well as mean-variance efficient frontier (Char. 7.1). 241

The USER EAW1 curve showed no risk-return trade-off. An investor would be 242 243 hard-pressed to outperform if he or she used an EAW1 strategy (unless he or she managed an index-enhanced product). 244

Guerard, Krauklis, and Kumar (2012) reported great APT-TaR portfolio results 245 with the USER data. Let us review some of the Guerard, Krauklis, and Kumar 246 247 (2012) results, shown in Table 7.1.

Ņ	USER analy	sis						
1.3	January 199	8 to December 2009						
4.		Mean-Variance (M	V)			Mean-Variance Tra	tcking Error at Risk	(MVTaR)
1.5	Lambda	Geometric Mean (GM)	Sharpe Ratio (ShR)	Information Ratio (IR)	Lambda	Geometric Mean (GM)	Sharpe Ratio (ShR)	Information Ratio (IR)
1.6	500	5.80	0.116	0.47	500	6.49	0.144	0.590
1.7	200	5.94	0.123	0.55	200	6.58	0.148	0.630
H.8	100	4.49	0.061	0.36	100	5.60	0.106	0.520
t1.9	50	4.54	0.065	0.43	50	4.77	0.072	0.490
t1.10	10	4.54	0.069	0.53	10	4.57	0.069	0.450
H.11	Benchmark	1.73	-0.074		Benchmar	ik 1.73	-0.074	

186 7 More Markowitz Efficient Portfolios Featuring the USER Data and an Extension...

t2.1	Table 7.2 Average number	USER analysis							
t2.2	or securities in optimal portfolios	January 1997 to December 2009							
t2.3	F	Lambda	EAW1	EAW2	EAW3	EAW4	MV		
t2.4		Tracking error at risk optimization							
t2.5		500	118.1	85.4	74.7	68.6	64.8		
t2.6		200	122.6	92.2	82.5	77.4	77.8		
t2.7		100	125.6	100.0	92.2	90.5	90.5		
t2.8		50	131.3	111.7	105.0	103.5	103.4		
t2.9		10	147.3	137.4	133.7	133.2	136.2		
t2.10		Traditiona	l optimizati	on					
t2.11		500	127.1	100.5	91.8	88.7	87.1		
t2.12		200	131.2	108.4	101.4	96.6	99.7		
t2.13		100	138.3	119.5	115.4	110.6	114.0		
t2.14		50	141.2	122.2	118.1	124.5	118.6		
t2.15		10	161.6	157.9	156.4	155.0	159.8		

The Geometric Means, Sharpe Ratios, and Information Ratios for the mean-variance and Mean-Variance Tracking Error at Risk support the use of lambda 200 and the MVTaR approach.

It is well known that as one raises the portfolio lambda, the expected return of 251 portfolio rises and the number of securities in the optimal portfolios fall, see Blin 252 et al. (1997). Lambda, a measure of risk-aversion, the inverse of the risk-aversion 253 acceptance level of the Barra system, is a decision variable to determine the optimal 254 number of securities in a portfolio. Guerard et al. (2010) report a lambda of 200 255 maximized the Geometric Mean in Non-USA growth portfolios. Guerard, Krauklis, 256 and Kumar (2012) reported that the lambda of 200 is a necessary lambda with MV, 257 EAW3, and EAW4 portfolio construction model for the USER data to create 258 portfolios with fewer than 100 securities (Table 7.2). 259

Does the use of the TaR optimization technique produce a higher or lower number of average securities in portfolios than the MV optimization technique? A lambda of 200 implies optimal portfolios of 99.7 (100) stocks with mean-variance, MV, whereas MVTaR requires only 77.8 (78) stocks. The Blin and Bender TaR optimization procedure allows a manager to use fewer stocks in his or her portfolios than a traditional mean-variance optimization technique manager for a given lambda.

The reader notes that EAW1, EAW2, and EAW3 Tracking Error at Risk 267 portfolios require more stocks than MVTaR and are statistically dominated in the 268 risk-return trade-off curve, or Frontier, see Guerard, Krauklis, and Kumar (2012). In 269 spite of the Markowitz mean-variance portfolio construction and management 270 analysis being six decades old, it does very well in maximizing the Sharpe Ratio, 271 Geometric Mean, and Information Ratio relative to newer approaches. The 272 Markowitz Efficient Frontier (1952, 1956, 1959) methodology has performed 273 well with the USER data. Guerard, Krauklis, and Kumar (2012) reported that one 274 must move to an EAW4 and EAW5 strategies to outperform Mean-Variance 275 Tracking Error at Risk models. 276

AU3

Portfolio Construction, Management, and Analysis: An 277 Introduction to Systematic Tracking Error Optimization 278

It has been recognized for many years that sample covariance matrices are not the 279 most suitable for portfolio optimization (Chopra and Ziemba (1993)). When the 280 objective is to create a minimum variance portfolio, there are a series of shrinkage 281 techniques which have been proposed to modify the sample covariance matrix 282 TS2 V_{sample} (Ledoit and Wolf 2003, 2004), where the need for shrinkage is the estima-283 tion errors in the sample covariance matrix that may most likely render 284 mean-variance optimizer less efficient. In its place, we suggest using the matrix 285 obtained from the sample covariance matrix through a transformation called 286 shrinkage. This tends to pull the most extreme coefficients towards more central 287 values, systematically reducing estimation error. 288

Wormald and van der Merwe (2012) searched, via shrinkage techniques, for a 289 better estimate $V_{\text{est}} \neq V_{\text{sample}}$ for the covariance matrix to be used within an 290 optimization, and in particular one which provides a more robust estimator of 291 out-of-sample portfolio variances when used with quite general sets of expected 292 return estimates.⁵ Wormald and van der Merwe considered the advantages of using 293 a factor model representation of the estimated covariance matrix V_{est} which appears 294 in the Markowitz objective function for optimizing active (benchmark-relative) 295 portfolios when expected returns (alphas) are available for every stock. 296

That Markowitz objective function takes the general form, in terms of the vector 297 of weights w 298

$$U[\boldsymbol{w}] = -\lambda \boldsymbol{w}^{\mathrm{T}} \cdot \boldsymbol{a} + \frac{1}{2} \boldsymbol{w}^{\mathrm{T}} \cdot \boldsymbol{V}_{\mathrm{est}} \cdot \boldsymbol{w}, \qquad (7.26)$$

where λ is called the risk trade-off parameter, and *a* is the vector of expected 299 returns. A general factor decomposition of the covariance matrix V_{est} may be made 300 in terms of asset exposures to factors X, the covariance matrix F of the factors 301 themselves, and the diagonal residual or specific term Δ^2 302

$$\boldsymbol{V}_{\text{est}} = \boldsymbol{V}_{\text{factor}} = \boldsymbol{X}^{\mathrm{T}} \boldsymbol{F} \boldsymbol{X} + \Delta^{2}. \tag{7.27}$$

The particular factor model representation we will consider is that provided by 303 an orthonormalized Principal Components Analysis (PCA) factor model, such that 304 the principal components factor covariances are all zero for different factors, and 305 factor variances take the value 1. 306

187

⁵ There is a large literature on the application of optimization to portfolio construction, starting with Markowitz (1952, 1959) and reviewed in Fabozzi et al. (2002a). A recent comprehensive overview can be found in the volume edited by Guerard (2010). An alternative approach might be pursued using ultrametrics and spanning trees rather than correlation shrinkage, see Onnela et al. (2003) for more on this approach.

307 Then we have, for these particular PCA factor exposures B

$$F = I$$
.

In this case, we can express the estimated asset covariance matrix in the special form

$$\boldsymbol{V}_{\text{est}} = \boldsymbol{V}_{\text{PCA}} = \boldsymbol{B}^{\mathrm{T}}\boldsymbol{B} + \Delta^{2}, \qquad (7.28)$$

where **B** is the matrix of asset exposures to the orthonormalized factors and Δ^2 is the diagonal matrix of asset-specific risks in the model.

For Wormald and van der Merwe (2012), a key insight into the justification for 312 factor modeling of risk is that it can be understood as an example of shrinkage 313 techniques applied to the sample covariance matrix V_{sample} , and has been widely 314 accepted as an effective way of improving the risk characteristics of optimized 315 portfolios, as described in Chan et al. (1999) and Fabozzi et al. (2002b). A parallel 316 317 series of studies has focussed on the role of constraints in portfolio optimization, including contributions from Jagannathan and Ma (2003) and DeMiguel et al. 318 (2008) who developed this line of inquiry and showed that many kinds of 319 constraints applied in portfolio optimization can be understood as equivalent to 320 statistically-sensible shrinkage of the sample covariance matrix. DeMiguel et al. 321 (2008) focused on a detailed comparison of a set of portfolio strategies which are 322 specified entirely by particular constraints defined in terms of the norm of the 323 portfolio-weight vector, and provide a moment-shrinkage interpretation for the 324 action of the constraint. In particular those authors prove analytically that quadratic 325 constraints such as constraints on norms constructed from portfolio-weight vectors 326 provide solutions which have a one-to-one correspondence with the portfolios 327 proposed via the covariance shrinkage technique discussed in Ledoit and Wolf 328 (2004). The empirical evidence they provide demonstrates that norm-constrained 329 portfolios often have a higher Sharpe Ratio than less-constrained portfolio 330 strategies and those considered by Jagannathan and Ma (2003) and Ledoit and 331 Wolf (2003, 2004). 332

The issue of how best to apply shrinkage to the covariance matrix is also 333 considered by Disatnik and Benninga (2007) who pay special attention to the use 334 of shrinkage estimators and portfolios of estimators, a concept closely related to 335 risk factor modeling. Their work, which is only concerned with the problem of 336 constructing risk-minimized portfolios, suggests that short-sales constraints make a 337 substantial difference in reducing the ex-post portfolio risk, compared to uncon-338 strained global minimum solutions, and that it is quite difficult to obtain statistically 339 significant differences from the ex-post risk for similarly-constrained solutions with 340 differing covariance matrix estimators. This difficulty is one which also prevails 341 when looking at the evidence for improved ex-post risk-adjusted performance when 342 optimizing with an alpha model, which is the empirical case considered in the 343 present study. When the objective is to create a portfolio with maximal alpha for a 344

given risk (with either risk or alpha constrained to lie within bounds), there has been 345 considerable attention paid to the question of whether the utility function should be 346 modified to reflect the distinction between spanned and orthogonal alpha. The 347 problem has been set out explicitly in Lee and Stefek (2008). The emphasis on 348 treating spanned alpha (explained by the systematic factors of the risk model) and 349 orthogonal alpha (not explained by those factors) differently within the utility 350 function is motivated by very similar considerations to those treated in the literature 351 on shrinkage approaches, where both the process of estimating expected asset 352 return correlations via a model based on factors and the subsequent placing of 353 constraints on portfolio norms (DeMiguel et al. 2008) have been shown to be 354 effective in generating portfolios with significant out-of-sample improvement in 355 risk characteristics. 356

Let us review the Wormald and van der Merwe (2012) distinctions between 357 systematic and specific parts of the risk, since it is this distinction which underlies 358 the concern that spanned alpha should be treated differently from orthogonal alpha 359 within an optimization. The portfolio variance may in general be decomposed into a 360 factor (systematic or spanned) part and a residual (specific or orthogonal) part: 361

$$\sigma_{\text{total}}^2 = \sigma_s^2 + \sigma_e^2. \tag{7.29}$$

The first part of the risk term, defined in terms of the portfolio-weight vector w as 362

$$\sigma_s^2 = \boldsymbol{w}^{\mathrm{T}} \cdot (\boldsymbol{B}^{\mathrm{T}} \boldsymbol{B}) \cdot \boldsymbol{w}, \qquad (7.30)$$

the factor risk of the portfolio, while the second part of the risk term, defined as 363

$$\sigma_e^2 = \boldsymbol{w}^{\mathrm{T}} \cdot \boldsymbol{\Delta}^2 \cdot \boldsymbol{w}, \tag{7.31}$$

the specific risk of the portfolio.

364

Wormald and van der Merwe (2012) demonstrated via the USER strategy 365 simulation how the APT optimizer can be useful in implementing portfolio construction. Solutions which are constrained to be bounded on both systematic and 367 specific risk terms require a second-order cone solver for efficient solutions, as 368 described in Kolbert and Wormald (2010). 369

A great advantage in having efficient methods available to generate these 370 solutions is that the investor's intuition can be tested and extended as the underlying 371 utility or the investment constraints are varied. We present an analysis of the effects 372 of the systematic risk constraint on various style exposures including momentum 373 within the strategy simulation. 374

The objective function, to be minimized, for the optimization is now defined in 375 terms of the *active* weight vector *w* of the portfolio, is given by exact analogy in: 376

$$U[\mathbf{w}] = -\lambda \mathbf{w}^{\mathrm{T}} \cdot \mathbf{a} + \frac{1}{2} \mathbf{w}^{\mathrm{T}} \cdot (\mathbf{B}^{\mathrm{T}} \mathbf{B} + \Delta^{2}) \cdot \mathbf{w}, \qquad (7.32)$$

377 where λ is the risk trade-off parameter and *a* is the vector of MQ alphas.

The covariance matrix is given by the APT factor model representation of (7.5):

$$V_{\rm pca} = \boldsymbol{B}^{\rm T} \boldsymbol{B} + \Delta^2, \tag{7.33}$$

where **B** is the matrix of asset exposures to the APT factors and Δ^2 is the diagonal matrix of asset-specific risks in the model. In the empirical results set out here, we are concerned with active risk measures, and so we introduce the terminology of tracking error (TE) rather than variance for describing the factor and non-factor parts of the active risk. The effects of shrinkage in factor model estimation are demonstrated by considering the 2-part form of the total active risk (tracking error squared) term; we write, following the analogy with (7.32):

$$\sigma_{A \text{ total}}^2 = \sigma_{As}^2 + \sigma_{Ae}^2. \tag{7.34}$$

386 The first part of the risk term, defined as

$$\sigma_{As}^2 = \boldsymbol{w}^{\mathrm{T}} \cdot (\boldsymbol{B}^{\mathrm{T}} \boldsymbol{B}) \cdot \boldsymbol{w}, \qquad (7.35)$$

the active systematic risk (or systematic TE squared) of the portfolio, while thesecond part of the risk term, defined as

$$\sigma_{Ae}^2 = \boldsymbol{w}^{\mathrm{T}} \cdot \boldsymbol{\Delta}^2 \cdot \boldsymbol{w}, \tag{7.36}$$

the active specific risk (or specific TE squared) of the portfolio. Wormald and van der Merwe (2012) demonstrated the effects of shrinkage implied by optimization constraints within the empirical results, by putting separate constraints on the total TE and the systematic TE during the optimized USER simulations.

Wormald and van der Merwe (2012) implemented three strategies. The three 393 strategies are very similar, except for differences in systematic active risk 394 constraints. The first strategy constructs portfolios without any constraints on 395 Systematic Tracking Error (TE), and is referred to as NoRiskConst. Another 396 strategy places a mild constraint on systematic TE and is referred to as 397 *MildRiskConst.* The mild constraint level reflects a level of systematic TE slightly 398 lower than the average of the observed values in NoRiskConst. In MildRiskConst 399 systematic TE is constrained to be below 2.3%. The third strategy constrains 400 systematic TE to be below 1.5% and is called StrongRiskConst. Wormald and 401 van der Merwe (2012) reported USER simulation results suggesting that applying 402 a mild Systematic TE constraint leads to slight outperformance in the long run 403 compared to other strategies. All three strategies outperform the benchmark. The 404 Systematic Tracking Error methodology of Wormald and van der Merwe (2012) 405 406 offered statistically significant asset selection and effective portfolio construction and management. 407

Table 7.3	Mild, strong, and	no risk controls	in a global unive	erse. January 20	02 to December 2011	t3.1
	initia, ou ong, and		in a grootar ann i t	5100, 0 mildai j =0		

Geometric Mean	Sharpe Ratio	Information Ratio	STD
14.16	0.53	0.65	23.20
13.75	0.49	0.59	24.18
11.08	0.41	0.54	22.71
4.56	0.16		13.23
	Geometric Mean 14.16 13.75 11.08 4.56	Geometric Mean Sharpe Ratio 14.16 0.53 13.75 0.49 11.08 0.41 4.56 0.16	Geometric Mean Sharpe Ratio Information Ratio 14.16 0.53 0.65 13.75 0.49 0.59 11.08 0.41 0.54 4.56 0.16

We use an All Country World Growth (ACWG) index and its constituents for the 408 January 2002 to December 2011 period. We use a lambda of 200 and employ the 409 Wormald and van der Merwe (2012) risk parameters. We find that the No Risk 410 Control and Mild Risk Control simulations dominate the Strong Risk Control 411 simulation, a result consistent with Wormald and van der Merwe. The three risk 412 models work well, producing at least 700 basis points of outperformance, 413 subtracting 150 basis points of transactions costs, each way, please see Table 7.3. 414

Markowitz Restored: The Alpha Alignment Factor Approach 415

Several academics and practitioners, decided to perform a postmortem analysis of 416 the mean-variance portfolios, attempted to understand the reasons for the deviation 417 of ex-post performance from ex-ante targets and used their analysis to suggest 418 enhancements to Markowitz's original approach. Lee and Stefek (2008) and Saxena 419 and Stubbs (2012) have worked on optimization models to "restore" a better 420 relationship between ex-ante and ex-post risk model estimates. One of the funda- 421 mental contributions was the development of linear factor models to capture the 422 sources of systematic risk and characterize the key drivers of excess returns. While 423 predicting expected returns is exclusively a forward looking activity, risk prediction 424 also focuses on explaining cross-sectional variability of the returns process, mostly 425 by using historical data. The first moment of the equity returns process drives 426 expected return modelers while the second moment is the focus of risk modelers. 427 These differences in the ultimate goals inevitably introduce certain "misalignment" 428 between the factors used to forecast expected returns and risk. While expected 429 return and risk models are indispensable components of any active strategy, there is 430 a third component, namely, the set of constraints used to build a portfolio. 431 Constraints play an important role in determining the composition of the optimal 432 portfolio. Most real-life quantitative strategies have constraints that model desirable 433 characteristics of the optimal portfolio. While some of these constraints may be 434 mandatory, for example, a client's reluctance to invest in stocks that benefit from 435 alcohol, tobacco or gambling activities on ethical grounds, other constraints are the 436 result of best practices in practical portfolio management. A turnover constraint 437 may create a factor misalignment, as we will find shortly in the USER analysis. 438

439 Saxena and Stubbs (2012) summarize, quantitative equity portfolio construction 440 entails complex interaction between factors used for forecasting expected returns, 441 risk, and the constraints. Problems that arise due to mutual discrepancies between 442 these three entities are collectively referred to as Factor Alignment Problems (FAP) 443 and constitute the emphasis of the current paper. Our key contributions are 444 summarized below:

1. The differences in the approaches that are used to build expected return forecast
and risk models manifest themselves as misalignment between the alpha and risk
factors.

448 2. Using an optimization tool to construct the optimal holdings has the unintended
effect of magnifying sources of misalignment. The optimize underestimates the
systematic risk of the portion of the expected returns which is not aligned with

450 systematic risk of the portion of the expected returns which is not aligned with 451 the risk model. Consequently, it overloads the portion of the expected returns

452 which is uncorrelated with all the user risk factors.

453 3. Our empirical results on a test-bed of real-life active portfolios based on client 454 data clearly refute the validity of the assumption that the portion of alpha that is 455 uncorrelated with all the risk factors has no systematic risk, and suggest the 456 existence of systematic risk factors which are missing from the risk model.

457 4. We propose augmenting the risk model with an additional auxiliary factor to 458 account for the effect of the missing risk factors in the risk model. The 459 augmenting factor is constructed dynamically and takes a holistic view of the 460 portfolio construction process involving the alpha model, the risk model, and 461 the constraints. We provide analytical evidence to attest the effectiveness of the 462 proposed approach.

463 5. Alternatively, the risk model can be augmented by adding the factors that are
464 used to compute expected returns, and which are not represented in the risk
465 model. The addition of these factors will provide full alignment between the risk
466 model and the expected returns, but not necessarily handle any misalignment

issues due to the use of constraints.

Quantitative strategies are typically based on three key components, namely, 468 expected returns (or alphas), a risk model, and the constraints. The risk model is 469 470 geared towards explaining cross-sectional variability in the historical and predicted returns. The efficacy of a risk model is judged by its ability to capture systematic 471 risk factors and the correlation structure between their respective factor returns. The 472 disparity in their respective objectives naturally affects the factors that are used in 473 the linear models that are used in their construction, and introduces misalignment. 474 With its primary focus on explaining the cross-sectional variability of the return 475 476 process, a risk model can often make do with ballpark estimates and gains little, if at all, from razor sharp estimation of accounting entries. In the King's English, 477 expected returns and risk modelers have different beliefs about the possible impact, 478 or lack thereof, of various economic events on their respective mandates, and the 479 misalignment between the alpha and risk factors is simply an inevitable manifesta-480 tion of their diverse beliefs. 481

Second, expected returns and risk model developers can at times take a 482 completely different view on the issue of earnings potential altogether. For 483 instance, some alpha construction techniques use alternative valuation metrics 484 such as different definitions of operating earnings and free cash flow for good 485 reasons. These different measurement choices of the same underlying fundamental 486 metric, namely earnings potential, lead to misalignment between the alpha and risk 487 factors. Another source of misalignment arises from the use of book-to-price (B/P) 488 ratio. Roughly speaking, book value is the accounting profession's estimate of the 489 company's value; it reflects what the company paid for the assets except intangible 490 assets such as goodwill developed internally, but it includes goodwill of subsidiary 491 companies acquired by purchase. This "cost basis" is then adjusted downward by 492 depreciation and amortization in a highly stylized and rigid attempt to reflect the 493 economic depreciation that actually befalls (most) assets. Off balance-sheet items 494 are ignored.

Saxena and Stubbs (2012) applied their AAF methodology to the USER model, 496 running a monthly backtest based on the above strategy in 2001–2009 time period 497 for various values of σ chosen from {0.5%, 0.6%, ..., 3.0%}. For each value of σ , 498 Saxena and Stubbs (2012) ran the backtest in two setups that were identical in all 499 respects except one, namely, only the second setup used the AAF methodology 500 (AAF = 20%). Saxena and Stubbs (2012) used Axioma's fundamental medium 501 horizon risk model (US2AxiomaMH) to model the active risk constraint. Saxena 502 and Stubbs (2012) reported the time series of the misalignment coefficient of alpha, 503 implied alpha, and the optimal portfolio and found that almost 40-60% of the alpha 504 is not aligned with the risk factors. The alignment characteristics of implied alpha 505 are significantly better than that of alpha. Among other things, this implies that the 506 constraints of the above strategy, especially the long-only constraint, play a proac- 507 tive role in containing the misalignment issue. Saxena and Stubbs (2012) reported 508 that the orthogonal component of both alpha and implied alpha not only has 509 systematic risk but the magnitude of the systematic risk is comparable to the 510 systematic risk associated with a median risk factor in US2AxiomaMH. To sum- 511 marize, the primary purpose of portfolio optimization is to create a portfolio having 512 an optimal risk-adjusted expected return. If a portion of the risk in a portfolio 513 derived from the orthogonal component of implied alpha is not accounted for, then 514 the resulting risk-adjusted expected return cannot be optimal. Saxena and Stubbs 515 (2012) showed the predicted and realized active risk for various risk target levels, 516 noting the significant downward bias in risk prediction when the AAF methodology 517 is not employed.⁶ Saxena and Stubbs (2012) showed the realized risk-return frontier 518

⁶ The Bias statistic, shown is a statistical metric which is used to measure the accuracy of risk prediction; if the ex-ante risk prediction is unbiased, then the bias statistic should be close to 1.0 (see Saxena and Stubbs 2010 for more details). Clearly, the bias statistics obtained without the aid of the AAF methodology are significantly above the 95% confidence interval thereby showing that the downward bias in the risk prediction of optimized portfolios is statistically significant. The AAF methodology recognizes the possibility of inadequate systematic risk estimation and guides the optimizer to avoid taking excessive unintended bets.

and reported that using the AAF methodology not only improves the accuracy of
risk prediction but also moves the ex-post frontier upwards thereby giving ex-post
performance improvements. The distinguishing feature of quantitative investing as
a profession is its belief in generating optimal risk-adjusted returns.

Saxena and Stubbs (2012) held that an approach that cannot predict the risk of 523 the portfolio correctly cannot be expected to produce portfolios that are optimal in 524 the ex-post sense. In other words, such an approach compromises the greater goal of 525 Markowitz MV efficiency and yields suboptimal portfolios. The AAF approach, on 526 the other hand, recognizes the possibility of missing systematic risk factors and 527 528 makes amends to the extent possible without complete recalibration of the risk model that explicitly accounts for the latent systematic risk in alpha factors. In the 529 530 process of doing so, AAF approach not only improves the accuracy of risk prediction but also partly repairs the lack of efficiency in the optimal portfolio. 531

Saxena and Stubbs (2012) acknowledged that the AAF approach has three key 532 limitations. First, the AAF construct is based on the assumption that the factor 533 returns associated with the missing factors are uncorrelated with the factor returns 534 associated with the regular factors in the user risk model. The fact that the AAF is 535 orthogonal to the regular factors, by itself, does not imply lack of correlation of 536 factor returns. To see this, note that even though the industry factors derived from 537 the GICS classification scheme are mutually orthogonal, the corresponding factor 538 returns are often correlated. By being correlation agnostic, the AAF approach fails 539 to capture the interaction between factor returns that can be attributed to missing 540 factors and the user risk factors. Second, the AAF approach requires calibration of 541 the volatility parameter which presents additional practical problems. Furthermore, 542 the temporal stationarity of the mentioned volatility parameter is not guaranteed, 543 which introduces additional complications related to dynamic estimation of the 544 545 volatility parameter. Third, the AAF approach does not use historical data to improve its representation of the missing factors. In other words, it is agnostic to 546 the nature of residual returns which might have useful information regarding 547 missing factors. A natural way to circumvent these problems is to recalibrate the 548 user risk model taking into account the possible sources of latent systematic risk. 549 Saxena and Stubbs (2012) hold that Custom Risk Models (CRM) accomplish 550 551 exactly that goal. CRM are derived from the user risk model, referred to as the base model, by introducing additional factors with the intent to eliminate various 552 sources of misalignment. The additional factors are referred to as custom risk 553 factors, and the resulting risk models are said to be customized. Construction of 554 CRM involves complete recalibration of the covariance matrix by re-running the 555 556 cross-sectional regressions, recomputing factor returns attributed to the user and 557 custom risk factors, and using the resulting time series of factor and residual returns to compute the factor-factor covariance matrix and specific risk. To summarize, 558 Saxena and Stubbs (2012) believe that a combination of CRM and AAF approach 559 offers a practical and holistic approach to FAP. 560

Let us take a final look at the USER data and portfolios using Axioma. If one uses the Axioma Medium Horizon Fundamental Risk Model for analyzing the APT-constructed ($\lambda = 200$) results reported in Guerard et al. (2012), one finds that asset selection dominates the portfolio returns; factor-based returns are -5.6 564 (%) whereas specific returns for 16.3%. The asset selection (active) of the APT- 565 estimated USER model is 9.7% with an Information Ratio of 1.12 and a *t*-statistic of 566 3.68, see Table 7.4. The IRs and *t*-statistics are similar to those reported in Guerard 567 et al. (2012). Furthermore, what about testing the USER model using higher 568 targeting tracking errors in the Axioma system? We report, in Table 7.5, that the 569 Geometric Means and Sharpe Ratios increase with higher targeted tracking errors 570 while the Information Ratios fall (tracking errors increase more then realized 571 portfolio returns) with USER in the Axioma system. The Geometric Means and 572

Table 7.4 Axioma Fundamental Risk Model attribution of APT Lambda = 200 Portfolio Returnst4.1(USER data, January 1999 to December 2009)

Total returns								
Portfolio Benchmark Active						2	5	0.095 -0.012 0.107
Local returns	Return	Risk	IR	T-Stat	Beg # of	assets	End #	of assets
Portfolio (Benchmark Active ().095 -0.012 0.107	0.221 0.221 0.096	n/a n/a 1.115	n/a n/a 3.683	94 1854 1898		92 1878 1922	
Factor/specific cor	tribution I	breakdown		0				
Factor contribution Specific return cor Active return	ı ıtribution		Č	0				-0.056 0.163 0.107
Return decomposi	tion			D .		D 1		
Risk-free rate Portfolio		5	0.03	96 95		1000		1 5
Benchmark return			-0.01	2				
Active return			0.10)7		0.096	1.115	3.683
Marke tin	et ning			0.000)	n/a	n/a	n/a
Special ret	fic turn			0.163	5	0.063	2.567	8.483
Factor co	r ntribution			-0.056	Ď	0.072	-0.778	-2.571
	U	S2Axioma MH.Style	e		-0.045	0.068	-0.659	-2.178
	U	S2Axioma MH. Industry			-0.011	0.032	-0.334	-1.103
		(Contributio	n	HR	Risk	IR	T-Stat
							(co	ontinued)

t4.26 Table 7.4 (continued)

t4.27		Contribution	Avg. Wtd. Exp.	HR	Risk	IR	T-Stat
			Avg. Wtd. Exp.				
t4.26	Contributors to active return by US	2AxiomaMH.	Style				
t4.27	US2AxiomaMH.Style		•				
t4.28	US2AxiomaMH.Size	0.042	-1.053	0.557	0.047	0.881	2.911
t4.29	US2AxiomaMH.Medium-Term Momentum	0.026	0.486	0.748	0.021	1.232	4.071
t4.30	US2AxiomaMH.Value	0.010	0.433	0.710	0.008	1.286	4.248
t4.31	US2AxiomaMH.Market Sensitivity	0.000	0.063	0.550	0.012	0.019	0.063
t4.32	US2AxiomaMH.Exchange Rate Sensitivity	0.000	-0.357	0.580	0.007	0.027	0.090
t4.33	US2AxiomaMH.Growth	-0.001	-0.044	0.443	0.002	-0.682	-2.252
t4.34	US2AxiomaMH.Short-Term Momentum	-0.007	0.055	0.405	0.010	-0.735	-2.428
t4.35	US2AxiomaMH.Leverage	-0.011	0.351	0.458	0.008	-1.298	-4.288
t4.36	US2AxiomaMH.Liquidity	-0.046	-1.148	0.351	0.036	-1.269	-4.194
t4.37	US2AxiomaMH.Volatility	-0.057	0.399	0.244	0.022	-2.591	-8.560
t4.38	US2AxiomaMH.Industry						
t4.39	US2AxiomaMH.Computers & Peripherals	0.009	-0.047	0.473	0.016	0.528	1.744
t4.40	US2AxiomaMH.Communications Equipment	0.008	-0.040	0.458	0.013	0.621	2.050
t4.41	US2AxiomaMH.Pharmaceuticals	0.005	-0.062	0.496	0.016	0.307	1.014
t4.42	US2AxiomaMH.Metals & Mining	0.004	0.022	0.618	0.010	0.343	1.135
t4.43	US2AxiomaMH.Media	0.003	-0.006	0.565	0.005	0.758	2.505
t4.44	US2AxiomaMH.Energy Equipment & Services	0.003	-0.017	0.473	0.007	0.485	1.603
t4.45	US2AxiomaMH.Industrial Conglomerates	0.002	-0.044	0.450	0.012	0.193	0.637
t4.46	US2AxiomaMH.Multiline Retail	0.002	-0.016	0.542	0.006	0.383	1.266
t4.47	US2AxiomaMH.Food & Staples Retailing	0.002	-0.020	0.527	0.005	0.443	1.465
t4.48	US2AxiomaMH.Specialty Retail	0.002	0.011	0.611	0.007	0.306	1.011
t4.49	US2AxiomaMH.Aerospace & Defense	0.002	-0.013	0.450	0.005	0.436	1.441
t4.50	US2AxiomaMH.Beverages	0.002	-0.020	0.504	0.006	0.335	1.108
t4.51	US2AxiomaMH.Oil, Gas & Consumable Fuels	0.002	0.018	0.542	0.007	0.232	0.768
t4.52	US2AxiomaMH.Machinery	0.002	-0.002	0.534	0.003	0.523	1.730
t4.53	US2AxiomaMH.Household Products	0.002	-0.020	0.466	0.005	0.340	1.122
t4.54	US2AxiomaMH.IT Services	0.001	-0.014	0.473	0.004	0.307	1.014
t4.55	US2AxiomaMH.Tobacco	0.001	-0.008	0.489	0.003	0.292	0.966
t4.56	US2AxiomaMH.Hotels, Restaurants & Leisure	0.001	-0.003	0.519	0.004	0.252	0.831
t4.57	US2AxiomaMH.Electrical Equipment	0.001	-0.005	0.527	0.002	0.460	1.520
						(co	ntinued)
197							

t4.58

		Avg.					
	Contribution	Wtd. Exp.	HR	Risk	IR	T-Stat	t4.59
US2AxiomaMH.Biotechnology	0.001	0.014	0.527	0.006	0.128	0.424	t4.60
US2AxiomaMH.Personal Products	0.001	-0.005	0.534	0.001	0.637	2.105	t4.61
US2AxiomaMH.Road & Rail	0.001	-0.003	0.450	0.002	0.292	0.964	t4.62
US2AxiomaMH.Independent Power	0.001	-0.002	0.443	0.001	0.589	1.947	t4.63
Producers & Energy Traders							
US2AxiomaMH.Construction & Engineering	0.000	0.003	0.443	0.002	0.277	0.917	t4.64
US2AxiomaMH.Diversified Consumer Services	0.000	0.000	0.489	0.002	0.135	0.447	t4.65
US2AxiomaMH.Containers & Packaging	0.000	0.001	0.481	0.002	0.119	0.395	t4.66
US2AxiomaMH.Gas Utilities	0.000	0.001	0.496	0.001	0.140	0.461	t4.67
US2AxiomaMH.Health Care Technology	0.000	0.000	0.382	0.000	0.674	2.227	t4.68
US2AxiomaMH.Air Freight & Logistics	0.000	-0.006	0.473	0.002	0.058	0.190	t4.69
US2AxiomaMH.Chemicals	0.000	0.007	0.573	0.003	0.030	0.099	t4.70
US2AxiomaMH.Water Utilities	0.000	0.000	0.481	0.000	0.088	0.292	t4.71
US2AxiomaMH.Transportation Infrastructure	0.000	0.000	0.076	0.000	0.481	1.589	t4.72
US2AxiomaMH.Electric Utilities	0.000	0.009	0.496	0.005	-0.001	-0.004	t4.73
US2AxiomaMH.Semiconductors & Semiconductor Equipment	0.000	-0.030	0.473	0.013	-0.006	-0.019	t4.74
US2AxiomaMH.Office Electronics	0.000	-0.001	0.412	0.001	-0.171	-0.565	t4.75
US2AxiomaMH.Consumer Finance	0.000	-0.005	0.481	0.004	-0.032	-0.107	t4.76
US2AxiomaMH.Airlines	0.000	0.008	0.489	0.005	-0.028	-0.094	t4.77
US2AxiomaMH.Construction Materials	0.000	0.000	0.489	0.001	-0.252	-0.833	t4.78
US2AxiomaMH.Diversified Financial Services	0.000	-0.002	0.450	0.002	-0.139	-0.458	t4.79
US2AxiomaMH.Food Products	0.000	0.008	0.565	0.004	-0.057	-0.189	t4.80
US2AxiomaMH.Professional Services	0.000	-0.001	0.443	0.001	-0.346	-1.144	t4.81
US2AxiomaMH.Distributors	0.000	0.001	0.527	0.000	-0.779	-2.575	t4.82
US2AxiomaMH.Multi-Utilities	0.000	0.007	0.473	0.004	-0.130	-0.429	t4.83
US2AxiomaMH.Software	-0.001	-0.033	0.450	0.010	-0.057	-0.190	t4.84
US2AxiomaMH.Life Sciences Tools & Services	-0.001	-0.001	0.435	0.001	-0.538	-1.779	t4.85
US2AxiomaMH.Building Products	-0.001	0.003	0.489	0.002	-0.265	-0.876	t4.86
US2AxiomaMH.Thrifts & Mortgage Finance	-0.001	0.003	0.489	0.004	-0.151	-0.499	t4.87
US2AxiomaMH.Marine	-0.001	0.000	0.389	0.000	-1.207	-3.990	t4.88
US2AxiomaMH.Real Estate Investment Trusts (REITs)	-0.001	0.013	0.473	0.008	-0.080	-0.266	t4.89

(continued)

t4.90 Table 7	.4 (continued)
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			Avg.				
t4.91		Contribution	Wtd. Exp.	HR	Risk	IR	T-Stat
t4.92	US2AxiomaMH.Health Care	-0.001	0.002	0.443	0.004	-0.179	-0.591
	Equipment & Supplies						
t4.93	US2AxiomaMH.Commercial Services & Supplies	-0.001	0.011	0.519	0.004	-0.180	-0.595
t4.94	US2AxiomaMH.Leisure Equipment & Products	-0.001	0.002	0.405	0.002	-0.474	-1.565
t4.95	US2AxiomaMH.Trading Companies & Distributors	-0.001	0.016	0.511	0.004	-0.223	-0.738
t4.96	US2AxiomaMH.Capital Markets	-0.001	-0.006	0.443	0.004	-0.244	-0.805
t4.97	US2AxiomaMH.Real Estate Management & Development	-0.001	0.004	0.504	0.001	-0.782	-2.583
t4.98	US2AxiomaMH.Auto Components	-0.001	0.000	0.405	0.001	-1.115	-3.684
t4.99	US2AxiomaMH.Health Care Providers & Services	-0.001	0.016	0.565	0.006	-0.211	-0.696
t4.100	US2AxiomaMH.Paper & Forest Products	-0.002	0.001	0.489	0.002	-0.995	-3.287
t4.101	US2AxiomaMH.Commercial Banks	-0.002	0.037	0.496	0.014	-0.149	-0.492
t4.102	2 US2AxiomaMH.Insurance	-0.003	0.013	0.427	0.007	-0.363	-1.199
t4.103	US2AxiomaMH.Household Durables	-0.003	0.021	0.481	0.008	-0.366	-1.210
t4.104	US2AxiomaMH.Textiles, Apparel & Luxury Goods	-0.003	0.025	0.511	0.008	-0.359	-1.187
t4.105	US2AxiomaMH.Internet & Catalog Retail	-0.004	0.003	0.412	0.003	-1.363	-4.504
t4.106	US2AxiomaMH.Automobiles	-0.004	0.023	0.458	0.008	-0.497	-1.643
t4.107	VUS2AxiomaMH.Wireless Telecommunication Services	-0.004	0.022	0.511	0.006	-0.644	-2.126
t4.108	BUS2AxiomaMH.Diversified Telecommunication Services	-0.006	0.049	0.489	0.012	-0.552	-1.824
t4.109	US2AxiomaMH.Electronic Equipment, Instruments & Components	-0.009	0.039	0.534	0.014	-0.677	-2.237
t4.110	US2AxiomaMH.Internet Software & Services	-0.016	0.018	0.405	0.013	-1.174	-3.880
t4.111	US2AxiomaMH.Sectors						
t4.112	2 US2AxiomaMH.Consumer Staples-S	0.007	-0.065	0.466	0.015	0.481	1.589
t4.113	BUS2AxiomaMH.Energy-S	0.005	0.001	0.542	0.007	0.689	2.277
t4.114	US2AxiomaMH.Industrials-S	0.005	-0.034	0.466	0.016	0.317	1.046
t4.115	5 US2AxiomaMH.Health Care-S	0.003	-0.032	0.550	0.014	0.240	0.793
t4.116	US2AxiomaMH.Materials-S	0.002	0.031	0.595	0.011	0.186	0.615
t4.117	US2AxiomaMH.Utilities-S	0.000	0.015	0.565	0.006	0.041	0.135
t4.118	US2AxiomaMH.Consumer	-0.007	0.061	0.527	0.023	-0.294	-0.973
	Discretionary-S	01007	01001	0.027	0.020	0.27 .	01270
t4.119	US2AxiomaMH.Information	-0.008	-0.108	0.405	0.035	-0.225	-0.743
	Technology-S						
t4.120	US2AxiomaMH.Financials-S	-0.009	0.058	0.466	0.024	-0.360	-1.190
t4.121	US2AxiomaMH.Telecommunication Services-S	-0.010	0.071	0.496	0.016	-0.654	-2.160

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t5.1

t5.2	USER m	lodel											
t5.3	Universe	:: R3000											
t5.4	Simulatio	on period:	January 199	99 to Marci	h 2009								
t5.5	Transacti	ions costs:	125 basis p	oints each	way								
t5.6				NoAAF	•	(Y			AAF				
	Return	Risk	Tracking	Sharpe	Information	Ann. active	Ann. active		Sharpe	Information	Ann. active	Ann. active	
t5.7	model	model	Error	Ratio	Ratio	return (%)	risk (%)	Ν	Ratio	Ratio	return (%)	risk (%)	Ν
t5.8	USER	STAT	4	0.48	1.83	13.26	7.24	160	0.48	2.20	12.81	5.83	241
t5.9			5	0.52	1.72	14.71	8.57	130	0.52	1.98	14.22	7.16	190
t5.10			9	0.52	1.56	15.27	<i>TT</i> -9	110	0.54	1.79	15.10	8.45	157
t5.11			7	0.55	1.52	16.47	10.84	97	0.55	1.64	15.93	9.72	131
t5.12			8	0.55	1.39	16.89	12.13	86	0.58	1.58	17.08	10.82	110
t5.13		FUND	4	0.40	2.03	11.12	5.49	139	0.42	2.44	11.48	4.70	215
t5.14			5	0.45	1.89	12.53	6.64	119	0.46	2.15	12.66	5.89	170
t5.15			9	0.48	1.75	13.59	7.78	106	0.49	1.91	13.53	7.08	144
t5.16			7	0.48	1.56	13.95	8.93	96	0.50	1.73	14.19	8.19	123
t5.17			8	0.47	1.38	14.25	10.31	89	0.50	1.58	14.71	9.33	107

573 Sharpe Ratios are higher in the Axioma 20-factor principal components estimated 574 Statistical Risk Model than in the Axioma Fundamental Risk Model.

An Global Expected Returns Model: Why Everyone Should Diversify Globally, 1998–2009

Guerard et al. (2012) extended a stock selection model originally developed and 577 estimated in Guerard and Takano (1991) and Bloch et al. (1993), adding a Brush-578 based price momentum variable, taking the price at time t - 1 divided by the price 579 12 months ago, t - 12, denoted PM, and the consensus (I/B/E/S) analysts' earnings 580 forecasts and analysts' revisions composite variable, CTEF, to the stock selection 581 model. Guerard et al. (2012) referred to the stock selection model as a United States 582 Expected Returns (USER) model. We can estimate an expanded stock selection 583 model to use as an input of expected returns in an optimization analysis. The 584 universe for all analysis consists of all securities on Wharton Research Data 585 Services (WRDS) platform from which we download the I/B/E/S database, and 586 the Global Compustat databases. The I/B/E/S database contains consensus analysts' 587 earnings per share forecast data and the Global Compustat database contains 588 fundamental data, i.e., the earnings, book value, cash flow, depreciation, and sales 589 data, used in this analysis for the January 1990 to December 2009 time period. The 590 information coefficient, IC, is estimated as the slope of a regression line in which 591 ranked subsequent returns are expressed as a function of the ranked strategy, at a 592 particular point of time. The high fundamental variables, earnings, bookvalue, cash 593 flow, and sales produce higher ICs in the global universe than in the USA universe 594 where USER was estimated, see Table 7.6. Moreover, analysts' 1-year-ahead and 2-595 year ahead revisions, RV1 and RV2, respectively, were much lower in global 596 markets, than USA market. Breadth, BR, and forecasted earnings yields, FEP, 597 were positive but less than in the USA market. The ICs on the analysts' forecast 598 variable, CTEF, and price momentum variable, PM, were lower than in the USA 599 universe. 600

The stock selection model estimated in this study, denoted as Global Expected Returns, GLER, is:

$$TR_{t+1} = a_0 + a_1EP_t + a_2BP_t + a_3CP_t + a_4SP_t + a_5REP_t + a_6RBP_t + a_7RCP_t + a_8RSP_t + a_9CTEF_t + a_{10}PM_t + e_t,$$
(7.37)

where EP = [earnings per share]/[price per share] = earnings-price ratio; BP = [book value per share]/[price per share] = book-price ratio; CP = [cash flow pershare]/[price per share] = cash flow-price ratio; SP = [net sales per share]/[priceper share] = sales-price ratio; REP = [current EP ratio]/[average EP ratio over thepast 5 years]; RBP = [current BP ratio]/[average BP ratio over the past 5 years];RCP = [current CP ratio]/[average CP ratio over the past 5 years]; RSP = [current

Table	7.6	Global composi	t
model	com	ponent ICs	

January 1990 to September 200	9	t6.1
Variable	IC	t6.2
EP	0.048	t6.3
BP	0.019	t6.4
CP	0.042	t6.5
SP	0.008	t6.6
DP	0.058	t6.7
RV1	0.011	t6.8
RV2	0.019	t6.9
BR1	0.026	t6.10
BR2	0.024	t6.11
FEP1	0.034	t6.12
FEP2	0.029	t6.13
CTEF	0.023	t6.14
PM	0.022	t6.15
EWC	0.043	t6.16
GLER	0.042	t6.17

SP ratio]/[average SP ratio over the past 5 years]; CTEF = consensus earnings per 609 share I/B/E/S forecast, revisions and breadth; PM = price momentum; and e = 610 randomly distributed error term. 611

The GLER model also is estimated using a weighted latent root regression, 612 WLRR, analysis on (7.1) to identify variables statistically significant at the 10% 613 level; uses the normalized coefficients as weights; and averages the variable 614 weights over the past 12 months. The 12-month smoothing is consistent with the 615 four-quarter smoothing in Guerard and Takano (1991) and Bloch et al. (1993). 616 While EP and BP variables are significant in explaining returns, the majority of the 617 forecast performance is attributable to other model variables, namely the relative 618 earnings-to-price, relative cash-to-price, relative sales-to-price, price momentum, 619 and earnings forecast variables. The consensus earnings forecasting variable, 620 CTEF, and the price momentum variable, PM, dominate the composite model, as 621 is suggested by the fact that the variables account for 48% of the model average 622 weights, slightly higher than the two variables combining for 44% of the weights in 623 the USER model. The time-average value of estimated coefficients: 624

 a_1 a_5 a_2 a_3 a_4 a_6 a_7 a_8 a_9 a_{10} 0.048 0.069 0.044 0.047 0.050 0.032 0.039 0.086 0.216 0.257

In terms of information coefficients, ICs, the use of the WLRR procedure 625 produces a virtually identical IC for the models during the 1980–2009 time period, 626 0.042, versus the equally-weighted IC of 0.043. The GLER model, has compared to 627 the USER model in Guerard et al. (2012) has approximately the same ICs. The IC 628 test of statistical significance can be referred to as a Level I test. Further evidence on 629 the anomalies is found in Levy (1999). 630

We report that in the Axioma GLER simulations, as with USER, the Axioma 631 Statistical Model dominates the Axioma Fundamental Model and AAF dominates 632 the non-AAF Frontiers in terms of Geometric Means and Sharpe Ratios with the 633 GLER Model (see Table 7.7).⁷ Moreover, in Table 7.8, lower turnover (4%, 634 monthly) allows the AAF factor to increase. An AAF of 30% is preferred to AAF 635 levels of 10 or 70%, for most tracking errors and turnover. The GLER model risk-636 return frontier demonstrates the effectiveness of the USER analysis in global 637 markets. Finally, if one graphs portfolio excess returns relative to portfolio tracking 638 errors, one sees in Chap. 7.2 that the Axioma Statistical Risk Model frontier with 639 640 AAF = 30% dominates the Axioma Statistical Risk Model frontier without AAF. Furthermore, the Axioma Statistical Risk Model frontier dominates the Axioma 641 642 Fundamental Risk Model frontier (with and without AAF).

643 Global Investing in the World of Business, 1999–2011

In the world of business, one does not access academic databases annually, or even 644 quarterly. Most industry analysis uses FactSet database and the Thomson Financial 645 (I/B/E/S) earnings forecasting database. We can estimate (7.37) for all securities on 646 the Thomson Financial and FactSet databases, some 46,550 firms in December 647 2011. We can decompose this universe into USA, Non-USA, and global securities. 648 We can refer to these universes as the USER, NUSER, and GLER databases, 649 respectively. One can estimate (7.37) models for index constituents in the three 650 growth universes: the Russell 3000 Growth (R3G) universe; the MSCI All Country 651 World ex USA Growth (ACWexUSG) universe; and the All Country World Growth 652 (ACWG) universe. The R3G analysis is shown in Table 7.9; the ACWexUSG 653 analysis is reported in Table 7.10; and ACWG universe analysis is shown in 654 Table 7.11. The GLER conclusions are confirmed: (1) the Axioma Statistical 655 Model dominates the Axioma Fundamental Model and (2) AAF dominates the 656 non-AAF Frontiers in terms of Information Ratios and Sharpe Ratios with the 657 658 models.⁸ An examination of Tables 7.9, 7.10, and 7.11, shows that Non-USA and global models produce higher Sharpe Ratios and higher Information Ratios than the 659 USER model in the 1999–2011 period. Non-USA and global stocks are more 660 inefficient than USA stocks, a result reported in Guerard (2012). If we graph the 661 USER, NUSER, and GLER active risks and active returns, we find that GLER and 662

⁷ The author worked on the GLER analysis with Anureet Saxena. Any errors remaining in this section are the sole responsibility of the author.

⁸ It is interesting to note that initial Axioma analysis suggests that purchasing AWCG constituents produce similar Information Ratios and Sharpe Ratios to purchasing FactSet and Thomson Financial securities (with at least two analysts covering the stocks, a universe exceeding index constituents by a factor of 5–6 times). The similar Sharpe Ratios and IRs are very interesting given the very illiquid composition of many securities (trading volume of less than \$15 MM USD, daily).

t7.1	Table 7.7	An AAF	' analysis of t	the Global I	Expected Returns	(GLER) mod	el						
t7.2	Initial Ax	ioma WRI	DS GLER Ba	icktest									
t7.3	GLER mc	odel-glob	al variation c	of USER	C								
t7.4	Universe:	ACWG			5								
t7.5	Simulatio	n period: J	anuary 1999	to March 2	600								
t7.6	Transactic	ons costs:	150 basis poi	ints each wa	iy, respectively								
t7.7				No AAF		Q			AAF				
	Return	Risk	Tracking	Sharpe	Information	Ann. active	Ann. active		Sharpe	Information	Ann. active	Ann. active	
t7.8	model	model	Error	Ratio	Ratio	return	risk	Ν	Ratio	Ratio	return	risk	Ν
t7.9	GLER	STAT	4	0.448	1.247	8.72	6.99	216	0.290	1.159	4.79	4.14	516
t7.10			5	0.511	1.119	10.52	8.77	204	0.359	1.230	6.37	5.18	442
t7.11			9	0.516	1.089	11.02	10.12	188	0.397	1.145	7.43	6.49	383
t7.12			7	0.552	1.074	12.29	11.44	185	0.464	1.179	9.09	7.71	340
t7.13			8	0.605	1.111	14.14	12.73	177	0.532	1.236	10.94	8.86	304
t7.14		FUND	4	0.286	0.882	4.97	5.63	221	0.230	1.009	3.53	3.50	488
t7.15			5	0.320	0.841	5.84	6.94	199	0.269	0.971	4.45	4.59	414
t7.16			9	0.356	0.827	6.91	6.91	196	0.306	0.952	5.39	5.66	357
t7.17			7	0.414	0.885	8.45	8.45	188	0.344	0.946	6.36	6.72	318
t7.18			8	0.427	0.845	8.99	8.99	182	0.407	1.012	7.97	7.88	291
										¢ O			

 \geq active Ann. 3.66 4.71 7.12 8.25 3.77 4.79 7.13 8.32 3.77 4.85 5.87 risk 5.845.95 7.24 8.42 10.06 active 4.29 6.24 7.37 9.33 10.84 4.53 4.22 5.67 return Ann. Information Ratio 1.289 1.335 1.310 1.315 1.203 1.198 1.170 1.261 1.232 1.181 1.222 1.241 AAF = 70Sharpe Ratio 0.355 0.4760.279 0.3930.435 0.2630.328 0.287 0.397 0.531 0.342 0.501 \geq active 5.668.38 9.80 8.37 9.72 6.94 11.00 5.65 6.98 6.74 5.4310.81Ann. risk active return 6.39 9.88 11.59 13.12 6.35 7.96 7.64 9.35 10.61 12.67 13.50 7.96 Ann. Information
 Table 7.8
 An AAF/turnover analysis of the Global Expected Returns (GLER) model
 Ratio 1.249 1.147 1.3861.267 1.3041.129 1.178 1.182 1.193 1.122 1.141 1.407AAF = 30Sharpe 444 0.413 522 0.479 Ratio 0.413 637 0.519 0.6090.3530.419 214 0.597 0.4940.5540.351 0.591 228 193 195 401 177 203 211 2 active 8.19 risk 9.84 8.19 6.29 10.03 11.35 12.22 6.88 8.25 6.71 8.43 Ann. Transactions costs: 150 basis points each way, respectively active return 9.37 10.68 11.90 12.87 8.14 9.65 11.07 12.31 13.94 7.86 9.47 Simulation period: January 1999 to December 2011 Ann. Information GLER model-global variation of USER Initial Axioma WRDS GLER Backtest Ratio 1.217 1.187 1.215 l.146 l.104 1.084I.142 1.147 1.141 1.491 1.291 AAF = 10Axioma Statistical Risk Model Sharpe Ratio 0.569 0.597 0.426 0.519 0.555 0.615 0.413 0.476 0.475 $0.490 \\ 0.531$ DNC Tracking Universe: ACWG Error $TO = 4 \quad 4$ S 0 2 8 4 S 9 \sim ∞ 4 Combo10F TO = 12TO = 8Return model

DNC did not converge

 ∞

7.07 8.25

1.147

0.424

0.459

11.85

13.22

0.601

12.24

14.16

5.91

6.95 8.11 9.09

1.177

0.381

8.36 9.78

9.82

1.175 1.198 1.197

0.4930.559

163 162 171

9.66 10.90

11.51

1.192 1.176 1.157

0.554

S S 0.581 0.622

12..82

0.418

11.72



Char. 7.2 Dominance of the Statistical Risk Model and Alpha Alignment Factors relative to Fundamental Risk Models and No Alpha Alignment Factors in the United States Equity Market, 1999–2009

NUSER dominate USER (see Char. 7.3). NUSER dominates GLER at an 8% 663 tracking error. 664

Let us take a closer look at the application at the Systematic Tracking Error 665 (STE) optimization technique reported in Wormald and van der Merwe (2012). Let 666 us take the FactSet and Thomson Financial universe for the 1990-2011 period and 667 reduce it by requiring at least two analysts to cover stocks. The universe goes from 668 466,550 to approximately 7,500 stocks. We will refer to this universe as the 669 GLER2012 universe. If one runs STE optimization with (1) No Risk Constraints; 670 (2) 8% monthly turnover; (3) 150 basis points of transactions costs, each way; (4) a 671 threshold position weight of 35 basis points; (5) and a maximum security weight of 672 4%; (5) long-only portfolio such that the minimum weight is 0; and one uses lambda 673 values of 500 and 200, then one produces portfolios producing higher Geometric 674 Means, Sharpe Ratios, and Information Ratios than the universe benchmark (see 675 Table 7.12). The Axioma attribution reveals statistical significant active return 676 (see Table 7.13). The FactSet GLER regression weights are graphed in Char. 7.4. 677 In the FactSet universe, CTEF and PM amount to only 38% of the GLER model 678 weights. PM has the largest weight, at about 24%. 679

There should be three results from the USER data analysis. An asset manager 680 should set tracking errors at 8% to maximize the Geometric Mean, Sharpe Ratio, 681 and Information Ratio; higher lambdas are preferred to lower lambdas (use at least 682 an APT lambda of 100); and the Alpha Alignment Factor is most appropriate. 683

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t9.1	Table 7.5	Axioma	analysis of R	tussell 3000	erveth constitution	ents							
t9.2	Initial Ax	ioma Rank	ced USA Bac	ktest									
t9.3	USER mo	ləbc											
t9.4	Universe:	R3G			C								
t9.5	Simulatio	n period: J	fanuary 1999	to Decembe	er 2011								
t9.6	Transacti	ons costs:	150 basis poi	nts each wa	y, respectively								
t9.7				NoAAF					AAF				
0	Return	Risk	Tracking	Sharpe	Information	Ann. active	Ann. active		Sharpe	Information	Ann. active	Ann. active	
t9.8	model	model	Error	Katio	Katio	return	rısk	N	Katio	Katio	return	rısk	S
t9.9	USER model	STAT	4	0.303	0.734	5.49	7.49	177	0.300	0.842	5.20	6.18	317
t9.10			5	0.309	0.650	5.78	8.90	138	0.336	0.835	6.07	7.29	242
t9.11			6	0.288	0.548	5.50	10.05	109	0.343	0.767	6.41	8.40	192
t9.12			7	0.301	0.536	6.04	11.25	91	0.345	0.700	6.70	9.59	156
t9.13			8	0.338	0.586	7.12	12.14	LL	0.345	0.640	6.83	10.64	128
t9.14		FUND	4	0.239	0.643	4.09	6.35	188	0.252	0.767	4.27	5.55	323
t9.15			5	0.276	0.646	5.01	7.75	148	0.275	0.715	4.84	6.77	257
t9.16			9	0.311	0.657	5.96	9.08	122	0.305	0.720	5.65	7.84	205
t9.17			7	0.298	0.598	5.88	10.15	106	0.305	0.644	5.81	9.03	202
t9.18			8	0.301	0.547	6.16	11.26	91	0.327	0.645	6.49	10.07	140
										Ś			

t10.1	Table 7.1	0 Axiom	a analysis of :	all ex USA	growth index co	onstituents							
t10.2	Initial Axi	ioma Rank	ted NUSG Ba	acktest									
t10.3	NUSER n	nodelNo	m-USA varia	tion of USE	3R								
t10.4	Universe:	ACWexU	SG		C								
t10.5	Simulation	n period: J	anuary 1999	to Decembe	ar 2011								
t10.6	Transactic	ons costs:	150 basis poir	nts each wa	y, respectively								
t10.7				RANKEL									
t10.8				NoAAF					AAF				
	Return	Risk	Tracking	Sharpe	Information	Ann. active	Ann. active		Sharpe	Information	Ann. active	Ann. active	
t10.9	model	model	Error	Ratio	Ratio	return	risk	Ν	Ratio	Ratio	return	risk	Ν
t10.10	NUSER	STAT	4	0.487	1.245	8.15	6.55	133	0.446	1.380	7.01	5.08	242
t10.11			5	0.546	1.228	9.79	7.97	102	0.501	1.377	8.43	6.12	182
t10.12			9	0.679	1.471	13.07	8.88	81	0.537	1.312	9.48	7.22	140
t10.13			7	0.719	1.450	14.53	10.02	99	0.618	1.394	11.56	8.29	113
t10.14			8	0.782	1.514	16.41	10.84	55	0.718	1.538	14.22	9.24	91
t10.15		FUND	4	0.445	1.271	6.68	5.25	153	0.405	1.331	5.79	4.35	244
t10.16			5	0.473	1.133	7.57	6.68	118	0.470	1.351	7.25	5.37	240
t10.17			9	0.557	1.232	9.66	7.84	95	0.518	1.340	8.42	6.43	152
t10.18			7	0.652	1.378	11.99	8.70	78	0.572	1.309	9.83	7.51	121
t10.19			8	0.725	1.465	14.06	9.60	66	0.640	1.374	11.74	8.54	100
										\$			
										•			

t11.1	Table 7.1	1 Axiom	a analysis of a	all country	world growth in	dex constituent.	s						
t11.2	Initial Axi	ioma Rank	ted Global Bé	icktest									
t11.3	GLER mo	del-glob	al variation o	f USER									
t11.4	Universe:	ACWG			C								
t11.5	Simulation	n period: J	anuary 1999	to Decembe	er 2011								
t11.6	Transactic	ons costs: 1	150 basis poii	nts each wa	iy, respectively								
t11.7				RANKEI									
t11.8				NoAAF		C			AAF				
	Return	Risk	Tracking	Sharpe	Information	Ann. active	Ann. active		Sharpe	Information	Ann. active	Ann. active	
t11.9	model	model	Error	Ratio	Ratio	return	risk	Ν	Ratio	Ratio	return	risk	Ν
t11.10	GLER	STAT	4	0.554	1.475	9.99	6.78	144	0.489	1.507	8.51	5.65	261
t11.11			5	0.602	1.385	11.38	8.24	110	0.554	1.521	10.09	6.63	197
t11.12			9	0.656	1.409	13.25	9.40	87	0.614	1.502	11.65	7.76	153
t11.13			7	0.715	1.454	14.94	10.28	70	0.638	1.415	12.63	8.93	120
t11.14			8	0.748	1.451	16.20	11.16	58	0.672	1.385	14.00	10.11	95
t11.15		FUND	4	0.382	1.091	6.08	5.57	163	0.373	1.231	5.82	4.73	272
t11.16			5	0.460	1.151	7.73	6.72	129	0.438	1.260	7.19	5.71	210
t11.17			9	0.521	1.158	9.33	8.06	104	0.492	1.255	8.40	69.9	167
t11.18			7	0.582	1.217	11.02	9.06	83	0.563	1.294	10.08	7.79	137
t11.19			8	0.647	1.281	12.75	9.95	71	0.602	1.265	11.36	8.99	110
										C			



Char. 7.3	It paid to	be an	International	Investor,	1999–201
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Table 7.12 FOLIOIO CILICITA IOI IIO IISK CONSITAILIS STE POLIOIK	Table 7.12	Portfolio cr	iteria for no	risk constrai	nts STE	portfolios
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	Geometric Means	Sharpe Ratios	Information Ratios	Tracking Errors	t12.2
Lambda = 500	17.96	0.67	0.92	14.69	t12.3
Lambda $= 200$	14.16	0.53	0.65	14.63	t12.4
ACWG benchmark	4.56	0.16			t12.5

Table 7.13 Po	rtfolio GLE	R L500 re	sults			
Portfolio			V		VA_NoRC	GLER_McKinley
Benchmark					MSCI WO	RLD GROWTH
Attribution peri	od				01/31/2003	to 01/31/2012
Frequency					Monthly	
Risk model					WW21Axi	omaMH
Bayesian half li	ife				2.0	
Realized marke	t return (1/y	/ear)			0	
Return type					Geometric	
Risk scaling					Annualized	ł
Risk type					PREDICTI	ED_RISK
Report date					06/29/2012	!
Base currency					USD	
Total returns						
Portfolio						0.187
Benchmark						0.080
Active						0.107
Local returns	Return	Risk	IR	T-Stat	Beg # of assets	End # of assets
Portfolio	0.187	0.232	n/a	n/a	108	123
Benchmark	0.080	0.192	n/a	n/a	528	965
Active	0.107	0.093	1.148	3.443	633	1075

t12.1

t13.22 Factor/specific contribution breakdown

10.22 I actor/specific contribution break	uo wn							
t13.23 Factor contribution								0.042
t13.24 Specific return contribution								0.065
t13.25 Active return								0.107
t13.26 Contributor	Retu	rn	Return	Return	Ri	sk	IR	T-Stat
t13.27 Return decomposition								
t13.28 Risk-free rate	0.024	1						
t13.29 Portfolio return	0.187	7						
t13.30 Benchmark return	0.080)						
t13.31 Active return	0.107	7			0.0	093	1.148	3.443
t13.32 Market timing			0.000		n/a	a	n/a	n/a
t13.33 Specific return			0.065		0.0	060	1.082	3.246
t13.34 Factor contribution			0.042		0.0	071	0.588	1.763
t13.35 WW21AxiomaMH.Style				0.014	0.0	059	0.233	0.698
t13.36 WW21AxiomaMH.Market				0.000	0.0	000	0.558	1.673
t13.37 WW21AxiomaMH.Local				0.002	0.0	007	0.285	0.855
t13.38 WW21AxiomaMH.Industry				0.001	0.0	017	0.066	0.198
t13.39 WW21AxiomaMH.Currency				0.009	0.0	016	0.571	1.712
t13.40 WW21AxiomaMH.Country				0.015	0.0	025	0.600	1.799
				Δνσ				
t13.41		Contri	ibution	Wtd. Exp.	HR	Risk	IR	T-Stat
t13.42 WW21AxiomaMH.Style								
t13.43 WW21AxiomaMH.Medium-Tern	ı	0.04	.5	0.321	0.741	0.017	2.573	7.718
Momentum			X	\mathbf{O}				
t13.44 WW21AxiomaMH.Size		0.01	4	-0.894	0.565	0.044	0.324	0.972
t13.45 WW21AxiomaMH.Value		0.01	0	0.436	0.620	0.011	0.898	2.694
t13.46 WW21AxiomaMH.Liquidity		0.00	3	0.137	0.556	0.005	0.688	2.065
t13.47 WW21AxiomaMH.Growth		0.00	3	0.314	0.583	0.004	0.783	2.348
t13.48 WW21AxiomaMH.Exchange Rat	e	-0.00	1	0.083	0.444	0.002	-0.269	-0.806
Sensitivity								
t13.49 WW21AxiomaMH.Leverage		-0.00	4	0.090	0.426	0.002	-2.312	-6.935
t13.50 WW21AxiomaMH.Short-Term		-0.01	4	0.106	0.380	0.012	-1.183	-3.550
Momentum								
t13.51 WW21AxiomaMH.Volatility		-0.04	-3	0.630	0.380	0.049	-0.879	-2.636
t13.52 Contributors to Active Return	by W	W21A	xiomal	MH.Market	t			
t13.53 WW21AxiomaMH.Market								
t13.54 WW21AxiomaMH.Global Marke	t	0.00	0	0.000	0.602	0.000	0.558	1.673
t13.55 Contributors to Active Return	by W	W21A	xiomal	MH.Local				
t13.56 WW21AxiomaMH.Local								
t13.57 WW21AxiomaMH.Domestic Chi	na	0.00	2	0.009	0.222	0.007	0.285	0.855
t13.58 Contributors to Active Return	by W	W21A	xiomal	MH.Industr	·у			
t13.59 WW21AxiomaMH.Industry								
t13.60 WW21AxiomaMH.Metals & Min	ning	0.00	4	0.043	0.556	0.006	0.632	1.897
t13.61 WW21AxiomaMH.Media		0.00	2	-0.013	0.630	0.001	1.859	5.577
t13.62 WW21AxiomaMH.Real Estate		0.00	2	0.026	0.528	0.003	0.567	1.701
Investment Trusts (REITs)								
t13.63 WW21AxiomaMH.Pharmaceutic	als	0.00	2	-0.052	0.481	0.005	0.334	1.003
							(co	ntinued)

Table 7.13	(continued)

Table 7.15 (continued)						
	Contribution	Avg. Wtd. Exp.	HR	Risk	IR	T-Stat
WW21AxiomaMH.Communications Equipment	0.001	-0.018	0.519	0.002	0.507	1.521
WW21AxiomaMH.Wireless Telecommunication Services	0.001	0.031	0.565	0.002	0.497	1.492
WW21AxiomaMH.Health Care Providers & Services	0.001	0.008	0.537	0.003	0.291	0.874
WW21AxiomaMH.Thrifts & Mortgage Finance	0.001	0.001	0.481	0.001	0.974	2.923
WW21AxiomaMH.Transportation Infrastructure	0.001	0.009	0.509	0.001	0.869	2.607
WW21AxiomaMH.Internet & Catalog Retail	0.001	0.001	0.500	0.001	0.580	1.741
WW21AxiomaMH.Internet Software & Services	0.001	-0.003	0.537	0.001	0.594	1.782
WW21AxiomaMH.Electronic Equipment, Instruments & Components	0.000	-0.006	0.519	0.001	0.793	2.380
WW21AxiomaMH.Consumer Finance	0.000	-0.001	0.519	0.001	0.547	1.642
WW21AxiomaMH.Diversified Telecommunication Services	0.000	0.022	0.481	0.002	0.157	0.471
WW21AxiomaMH.Containers & Packaging	0.000	0.003	0.574	0.001	0.533	1.598
WW21AxiomaMH.Professional Services	0.000	0.001	0.537	0.001	0.432	1.297
WW21AxiomaMH.Health Care Technology	0.000	0.007	0.315	0.001	0.254	0.761
WW21AxiomaMH.Aerospace & Defense	0.000	-0.007	0.481	0.001	0.180	0.539
WW21AxiomaMH.Commercial Banks	0.000	0.003	0.472	0.001	0.161	0.484
WW21AxiomaMH.Office Electronics	0.000	-0.005	0.528	0.000	0.420	1.260
WW21AxiomaMH.Hotels, Restaurants & Leisure	0.000	0.005	0.583	0.001	0.165	0.494
WW21AxiomaMH.Software	0.000	-0.033	0.463	0.003	0.053	0.159
WW21AxiomaMH.Computers & Peripherals	0.000	-0.017	0.463	0.002	0.057	0.171
WW21AxiomaMH.Textiles, Apparel & Luxury Goods	0.000	-0.002	0.593	0.001	0.215	0.646
WW21AxiomaMH.Construction & Engineering	0.000	-0.004	0.472	0.000	0.296	0.889
WW21AxiomaMH.Food Products	0.000	-0.010	0.491	0.001	0.103	0.308
WW21AxiomaMH.Construction Materials	0.000	0.000	0.509	0.000	0.138	0.414
WW21AxiomaMH.Multiline Retail	0.000	0.001	0.472	0.001	0.039	0.116
	0.000	-0.008	0.519	0.001	0.048	0.143

t13.91 Table 7.13 (continued)

		Avg.				
t13.92	Contribution	Wtd. Exp.	HR	Risk	IR	T-Stat
WW21AxiomaMH.Air Freight &						
Logistics						
t13.91 WW21AxiomaMH.Water Utilities	0.000	0.001	0.380	0.000	0.012	0.037
t13.92 WW21AxiomaMH.Household	0.000	0.002	0.509	0.001	0.005	0.016
Durables						
t13.93 WW21AxiomaMH.Semiconductors	0.000	-0.011	0.509	0.002	-0.018	-0.054
& Semiconductor Equipment						
t13.94 WW21AxiomaMH.Building	0.000	0.004	0.500	0.001	-0.121	-0.363
Products						
t13.95 WW21AxiomaMH.Leisure	0.000	0.000	0.546	0.000	-0.246	-0.739
Equipment & Products						
t13.96 WW21AxiomaMH.Electrical	0.000	-0.007	0.481	0.000	-0.189	-0.568
Equipment						
t13.97 WW21AxiomaMH.Trading	0.000	0.002	0.435	0.000	-0.244	-0.733
Companies & Distributors						
t13.98 WW21AxiomaMH.Independent	0.000	0.002	0.417	0.000	-0.267	-0.802
Power Producers & Energy						
Traders						
t13.99 WW21AxiomaMH.Diversified	0.000	-0.001	0.509	0.000	-0.389	-1.167
Consumer Services						
t13.100WW21AxiomaMH.Industrial	0.000	-0.013	0.463	0.001	-0.177	-0.531
Conglomerates						
t13.10 ¹ WW21AxiomaMH.Personal Products	0.000	-0.006	0.481	0.000	-0.329	-0.986
t13.102WW21AxiomaMH.Health Care	0.000	0.003	0.472	0.001	-0.126	-0.377
Equipment & Supplies						
t13.103WW21AxiomaMH.Energy	0.000	-0.009	0.481	0.002	-0.083	-0.250
Equipment & Services						
t13.104WW21AxiomaMH.Gas Utilities	0.000	-0.001	0.481	0.000	-0.880	-2.641
t13.105WW21AxiomaMH.Distributors	0.000	0.010	0.435	0.001	-0.265	-0.795
t13.106WW21AxiomaMH.Household	0.000	-0.017	0.565	0.002	-0.160	-0.480
Products						
t13.107WW21AxiomaMH.Life Sciences	0.000	0.000	0.241	0.001	-0.377	-1.131
Tools & Services						
t13.108WW21AxiomaMH.Multi-Utilities	0.000	-0.006	0.556	0.001	-0.416	-1.247
t13.109WW21AxiomaMH.Automobiles	0.000	-0.004	0.537	0.001	-0.280	-0.839
t13.110WW21AxiomaMH.Diversified	0.000	0.015	0.500	0.001	-0.261	-0.783
Financial Services						
t13.111WW21AxiomaMH.Commercial	0.000	0.009	0.528	0.001	-0.437	-1.311
Services & Supplies						
t13.112WW21AxiomaMH.IT Services	0.000	-0.007	0.509	0.001	-0.288	-0.865
t13.113WW21AxiomaMH.Insurance	0.000	0.032	0.491	0.003	-0.128	-0.383
t13.114WW21AxiomaMH.Chemicals	0.000	0.005	0.463	0.001	-0.341	-1.023
t13.115WW21AxiomaMH.Oil, Gas &	0.000	0.000	0.407	0.003	-0.123	-0.370
Consumable Fuels						
t13.116WW21AxiomaMH.Capital Markets	0.000	-0.005	0.463	0.001	-0.463	-1.389
t13.117WW21AxiomaMH.Road & Rail	0.000	-0.010	0.444	0.001	-0.505	-1.514
					(co	ntinued)
						/

Table 7.13 (continued)

t1	3.	1	1	8

		Avg.				
	Contribution	Wtd. Exp.	HR	Risk	IR	T-Stat
WW21AxiomaMH.Airlines	-0.001	0.031	0.444	0.005	-0.120	-0.361
WW21AxiomaMH.Specialty Retail	-0.001	-0.004	0.463	0.002	-0.368	-1.104
WW21AxiomaMH.Real Estate	-0.001	0.010	0.519	0.001	-0.708	-2.125
Management & Development						
WW21AxiomaMH.Beverages	-0.001	-0.022	0.407	0.002	-0.566	-1.697
WW21AxiomaMH.Biotechnology	-0.001	0.033	0.509	0.005	-0.206	-0.619
WW21AxiomaMH.Machinery	-0.001	-0.009	0.343	0.001	-1.589	-4.767
WW21AxiomaMH.Auto	-0.001	0.002	0.509	0.001	-1.237	-3.712
Components						
WW21AxiomaMH.Marine	-0.001	0.016	0.426	0.004	-0.276	-0.828
WW21AxiomaMH.Paper & Forest	-0.001	0.006	0.556	0.001	-0.799	-2.396
Products						
WW21AxiomaMH.Food & Staples	-0.001	-0.025	0.500	0.002	-0.596	-1.789
Retailing						
WW21AxiomaMH.Electric Utilities	-0.001	0.005	0.463	0.001	-1.008	-3.025
WW21AxiomaMH.Tobacco	-0.001	-0.011	0.407	0.001	-1.051	-3.153



Char. 7.4 Relative global model component weights, 1990-2011

Conclusions

684

We addressed several issues in portfolio construction and management with the 685 Guerard et al. (2012) USER data. First, we report that the Markowitz 686 mean-variance (MV) optimization technique dominates the Enhanced Index- 687 Tracking optimization technique at most security weight ranges. Second, we report 688

that the Systematic Tracking Error optimization technique reported Wormald and 689 van der Merwe (2011) is very effective in USA and global markets. Finally, we 690 report that the Saxena and Stubbs (2012) Axioma Alpha Alignment Factor (AAF) is 691 appropriate for USER and GLER Data and that the Axioma Statistical Risk Model 692 dominates the Axioma Fundamental Model. The Markowitz approach to portfolio 693 construction and management is 60 years old and remains an integral tool of 694 investment research. Earnings forecasts play a very important role in identifying 695 mispriced securities. 696

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Chapter 8 Forecasting World Stock Returns and Improved Asset Allocation

1 2 3

There is little evidence in the literature on whether predictability of stock returns 4 leads to improved asset allocation and performance (Handa and Tiwari 2006). 5 Handa and Tiwari (2006) found fixed results for forecasting 1-month-ahead results 6 in the USA for 1954–2002 period; the past-returns model worked well from 1974 to 7 1988 and poorly from 1959 to 1973 and 1989 to 2002. There are mixed academic 8 results for many financial tests. In this report, we show that it is possible to improve 9 performance of a naïve "60/40" model of equity and debt to a "60/40" model with 10 Global Timing (GT). We create a Global Timing signal based on the 12-month 11 moving average of the differential between the LIBOR rate and the All World 12 Country (ACW) index. If the predicted return signal, the differential of the 12- 13 AU1 month average returns on the ACW, exceeds LIBOR by a statistically significant 14 difference (one standard deviation), then a "buy" signal is created. If the predicted 15

J.B. Guerard, Jr., *Introduction to Financial Forecasting in Investment Analysis*, 217 DOI 10.1007/978-1-4614-5239-3_8, © Springer Science+Business Media New York 2013 return signal is less than -1.645, one standard deviation, then a "sell" decision is made. A neutral position exists in the signal and no change is made.¹

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As with Handa and Tiwari (2006), we restrict our investment choices to a 18 relatively riskless asset, LIBOR, or an investment in ACWG securities. We test 19 the model on ACW index and implement on the ACW or ACWG indexes. We are a 20 growth manager and use the constituent securities in the ACWG index. The 21 asset allocation benchmark is a "60/40" portfolio invested in 60 percent in a passive 22 basket of ACW securities. If the Tactical Asset Allocation (TAA) signal exceeds 23 1.645, then we buy. If the TAA signal is less than -1.645, then we sell. How can we 24 implement such a strategy in a long-only investment portfolio? As with the 25 McKinley Capital Management (MCM) "Global Alpha-Engineering a Dynamic 26 27 Momentum" strategy, we may vary the portfolio lambda, the measure of the return-risk preference of the asset manager. If the TAA signal exceeds 0.645, 28

$$L_{t} = \frac{LEI(t) - LEI(t-1)}{LEI(t-1)}.$$
(8.1)

The lagged correlation between the GEM2 factor return and the LEI return is

$$\rho_k^m = corr(f_{kt}^P, L_{t-m}), \tag{8.2}$$

where f_{kt}^{P} is the pure return to factor k over period t, and m is the number of lags in months.

Optimal portfolios are created using the MSCI Barra GEM2 risk model, the premier institutional asset manager portfolio management, and control system. The GEM2 model, described in Menchero et al. (2010), estimates a multifactor risk model composed of eight factors: the world, value, growth, momentum, liquidity, size, size nonlinearity, and leverage. The GEM2 Model is the global equivalent of the USE3 model used in Chap. 6. The Barra model allows the asset manager to specifically target desired portfolio exposures to accommodate client needs and expectations, such as having an exposure to momentum and not necessarily having other exposures. Simple factor portfolios have unit exposure to the particular factor, and nonzero exposure to other factors. Pure factor portfolios have unit exposure to the particular factor, and zero exposure to all other factors. Optimal factor portfolios have the minimum risk portfolio with unit exposure to the factor. Menchero et al. (2012) reported the strongest positive correlation that suggests a positive relationship between changes in the LEI and corresponding changes in Momentum six months later. A momentum-timing signal is created in which if an increase in 6-month average change in LEI exceeds 1.50 standard deviations, then one becomes aggressive with respective to momentum. One sells momentum if the 6-month average change in momentum is less than 1.50 standard deviations. We also present the cumulative performance of the pure Momentum factor, as well as the Euro LEI series. The momentum timing returns have been scaled to have the same realized volatility as the pure momentum factor over the 13-year period. Menchero et al. (2012) reported that the momentum timing strategy greatly outperforms the pure momentum strategy over this sample period, with the former climbing more than 60 %, compared to only 20 % return for the pure factor.

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¹ A similar signal was developed to investigate the relationship between Euro LEI and the GEM2 factor returns. For instance, suppose that a rise in the LEI one month could be associated with a rise in a GEM2 factor return three months later. An investor might then profit by taking a long position in the factor whenever the three-month lagged LEI were positive. One can use the Euro area Leading Economic indicator, LEI, series published by The Conference Board (TCB). Let LEI(t) be the LEI level at the end of month *t*. Generally, these values are published with a 1- or 2-month lag. The "return" to the LEI over month *t* is then given by

Table 8.1 Attribution report of the TAA signal portfolios, 1/2002–10/2011

Annualized contributions to total return				
Source of return	Contribution (% return)	Risk (% std. dev.)	Info ratio	T-stat
1. Risk free	1.86			
2. Total benchmark	4.67	17.46		
3. Currency selection	3.67	3.52	1.09	3.40
4. Cash-equity policy	0.00	0.00		
5. Risk indices	6.16	4.36	1.23	3.86
6. Industries	-0.38	2.56	-0.14	-0.44
7. Countries	0.97	5.07	0.19	0.61
8. World equity	0.00	0.00	C .	
9. Asset selection	1.16	3.22	0.41	1.29
10. Active equity	7.91	7.60	0.96	3.02
[5+6+7+8+9]				
11. Trading				
12. Transaction cost	-4.25			
13. Total active	7.63	8.22	0.93	2.91
[3 + 4 + 10 + 11 + 12]				
14. Total managed [2 + 13]	12.29	19.77		

Table 8.2 Strategy summary, January 2002–October 2011			
Strategy	Cumulative Wealth ratio	Mean Monthly return	Sharpe ratio
"60/40"	3.804	1.185	1.143
ACWG index	1.566	0.506	0.88
"60/40" GT	5.826	1.567	1.367

then we implement a portfolio lambda of 200, leading to an aggressive return-to- 29 risk portfolio. If the TAA signal is less than -1.645, then we implement a lambda of 30 10, indicating a relatively passive return-to-risk portfolio. If the TAA signal is 31 neutral, then we use a lambda of 75. We use MQ, a quantitative-based strategy 32 described in the MCM "Global Alpha" research report, as the portfolio expected 33 return.

An investor can purchase instruments or ETFs to produce a "60/40" return for 35 the February 1997–October 2011 period. We ran the simulations from January 1997 36 to October 2011, varying the portfolio returns using monthly signals and targeting 37 the All Country World Growth (ACWG) Index. We measure the performance of the 38 simulations from January 2002 to October 2011, the period of the Global (GEM2) 39 Model. The TAA signals portfolio produces statistically significant total active 40 returns, see Table 8.1. 41

Had an investor invested in a "60/40" strategy, the mean monthly return of 1.185 42 percent for January 2002–October 2011 exceeds the ACWG Index return of 0.506 43

t1.1

44 for the corresponding period. The "60/40"GT strategy produces a monthly return of

45 1.567 (including transactions costs of 150 basis points each way). The TAA signals

46 portfolio outperforms the market and the "60/40" strategy in producing higher

47 Sharpe Ratios. Thus, the TAA portfolios produce higher returns for a given level

48 of risk than the "60/40" strategy and the ACWG index (Table 8.2).



49 Summary and Conclusions

50 Stock return expectations can be used to vary the aggressiveness of equity

51 portfolios that can lead to Tactical Asset Allocation decisions that can outperform

52 a naïve "60/40" strategy.

53 **References**

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Chapter 9 Summary and Conclusions

1 2

The forecasting of earnings per share, eps, is a most important input to an investment 3 strategy. There is a tremendous literature regarding forecasting of corporate eps and 4 whether the forecasts are more accurate than a random walk or a random walk with 5 drift. Much of the literature can be summarized as follows: (1) analysts' forecasts are 6 not statistically different from a random walk with drift model; that is, analysts' 7 forecasts can be approximated with a first-order exponential smoothing model 8 forecast; (2) analysts' forecasts are biased; analysts' forecasts are optimistic; (3) 9 analysts' forecast revisions and the direction of their revisions are more highly 10 correlated with stock returns than earnings forecasts themselves; (4) earnings 11 forecasts are highly statistically significant in forecasting total stock returns; (5) 12 earnings forecasts, revisions, and direction of revisions can be combined with 13 fundamental data, such as earnings, book value, cash flow, sales, these variables 14 relative to their histories, and price momentum strategies to identify mispriced 15 stocks; (6) smaller capitalized stocks are more mispriced than larger capitalized 16 stocks; and (7) international and global stocks are more mispriced than the US 17 stocks. 18

We introduced the reader to regression models and various estimation 19 procedures. We have illustrated regression estimations by modeling consumption 20 functions and the relationship between real GDP and The Conference Board 21 Leading Economic Indicators (LEI). We estimated regressions using EViews, 22 SAS, and automatic modeling in Oxmetrics. There are many advantages with the 23 various regression software with regard to ease of use, outlier estimations, collin- 24 earity diagnostics, and automatic modeling procedures. 25

We introduced reader to the time series work of Professors box and Jenkins and 26 examined the predictive information in The Conference Board LEI for the USA, the 27 UK, Japan, and France. We find that The Conference Board LEI and FIBER short- 28 term LEI are statistically significant in modeling the respective real GDP changes 29 during the 1970-2000 period. One rejects the null hypothesis of no association 30 between changes in the LEI and changes in real GDP in the USA, and the G7 31 nations. If one uses a rolling 32 quarter estimation period and a one-period-ahead 32

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forecasting root mean square error calculation, the LEI forecasting errors are not
 significantly lower than the univariate ARIMA model forecasts.

We used two case studies to illustrate the effectiveness of regression modeling. 35 Regression analysis offered marginal improvement in the case of combining GNP 36 forecasts, but offered substantial improvement in identifying financial variables 37 associated with security returns. We introduced the reader to a stock selection 38 model that combined earnings forecasts, fundamental variables derived from bal-39 ance sheet and income statement analysis, and price momentum variables. The 40 regression-based United States Expected Returns (USER) Model was highly statis-41 tically significant in construction. Regression techniques addressing outliers and 42 multicollinearity problems in the USER Model outperformed equally weighted 43 44 strategies in stock selection modeling.

A case study of mergers was introduced so that the reader could examine Granger causality testing in detail. Mergers were modeled as a function of the LEI and stock prices. We found causality in the Chan and Lee (1990) test in that LEI and stock prices caused mergers.

The Barra Aegis system has been the industry standard for portfolio construc-49 50 tion, management, and measurement for almost 40 years. We demonstrated the effectiveness of the Barra Aegis system to create investment management strategies 51 to produce portfolios and attribute portfolio returns to the Barra multifactor risk 52 model during the December 1979-2009 period. We find additional evidence to 53 support the use of MSCI Bara multifactor models for portfolio construction and risk 54 control. We report two results: (1) a composite model incorporating fundamental 55 data, such as earnings, book value, cash flow, and sales, with analysts' earnings 56 forecast revisions and price momentum variables to identify mispriced securities; 57 (2) the returns to a multifactor risk-controlled portfolio allow us to reject the null 58 hypothesis that the results are due to data mining. We develop and estimate three 59 levels of testing for stock selection and portfolio construction. The use of multifac-60 tor risk-controlled portfolio returns allows us to reject the null hypothesis that the 61 results are due to data mining. The anomalies literature can be applied in real-world 62 portfolio construction. 63 We addressed several additional issues in portfolio construction and manage-64 65 ment with the USER data. First, we report that the Markowitz Mean-Variance (MV) optimization technique dominates the Enhanced Index-Tracking optimization tech-66 nique at most security weight ranges. Second, we report that the Systematic 67 Tracking Error optimization technique reported by Wormald and van der Merwe 68

69 (2012) is very effective in the US and Global markets. Finally, we report that 70 the Saxena and Stubbs (2012) Axioma Alpha Alignment Factor (AAF) is appropri-

71 ate for USER and global (GLER) Data and that the Axioma Statistical Risk Model

72 dominates the Axioma Fundamental Model. The Markowitz approach to portfolio

73 construction and management is sixty years old and remains an integral tool of

⁷⁴ investment research. Earnings forecasts play a very important role in identifying

75 mispriced securities.

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Summary and Conclusions

Finally, stock return expectations can be used to vary the aggressiveness of 76 equity portfolios that can lead to Tactical Asset Allocation decisions that can 77 outperform a naïve "60/40" strategy.

Forecasting earnings is an integral component to stock selection modeling and 79 investment analysis.

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